

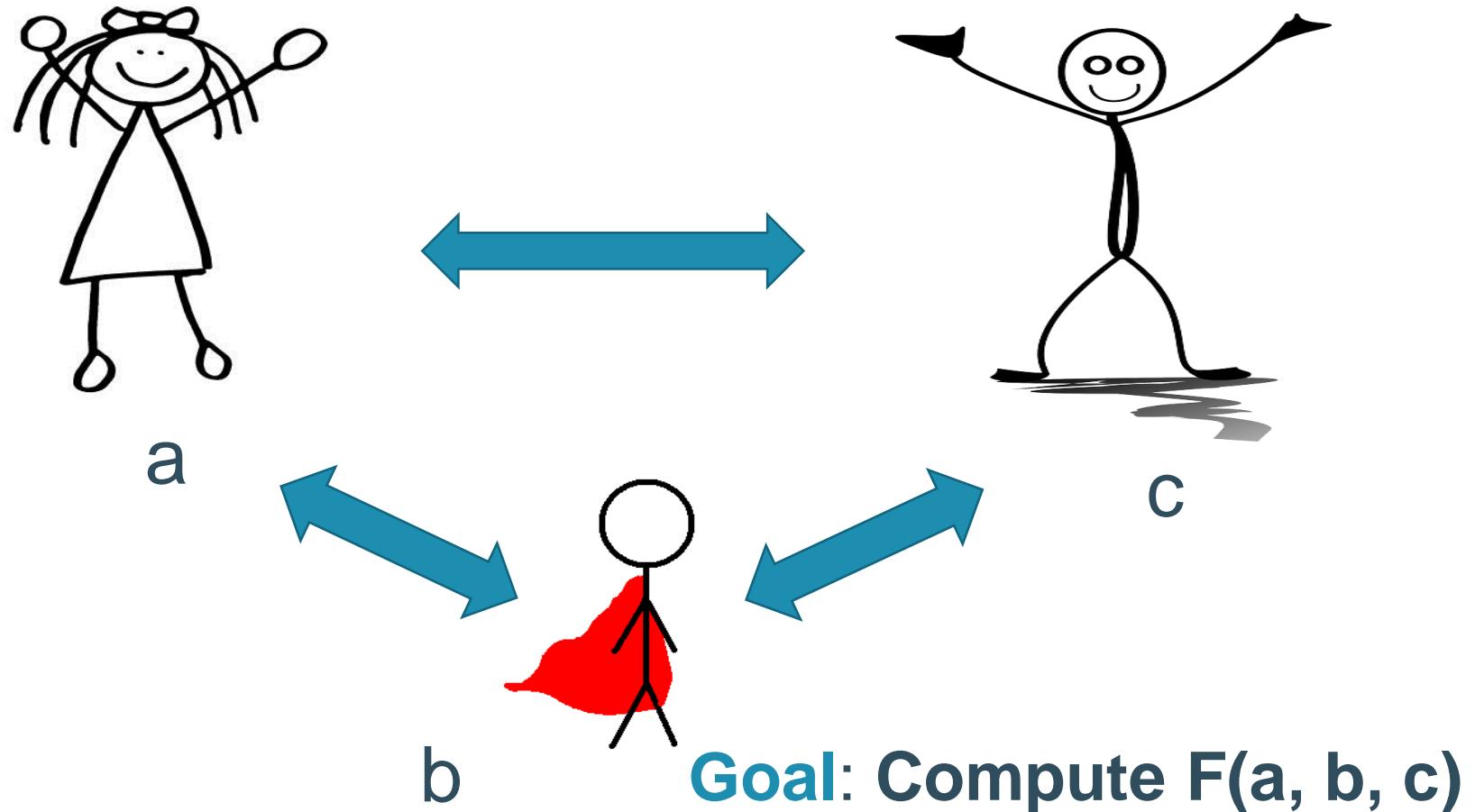
FSE 2018

# Modes of operations for computing on encrypted data

Dragos Rotaru, N.P. Smart, and Martijn Stam

KU Leuven, University of Bristol

# Multiparty computation hijacks FSE'18



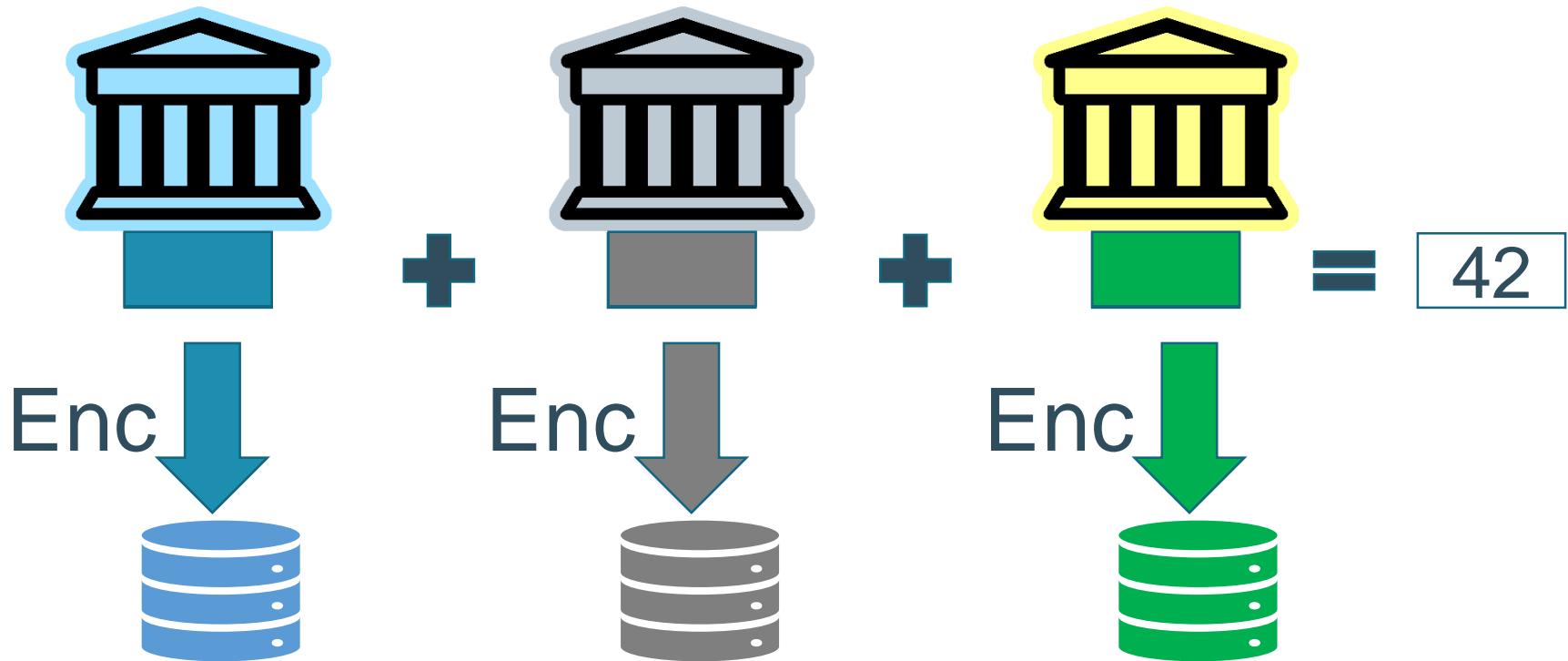
# What is the problem?



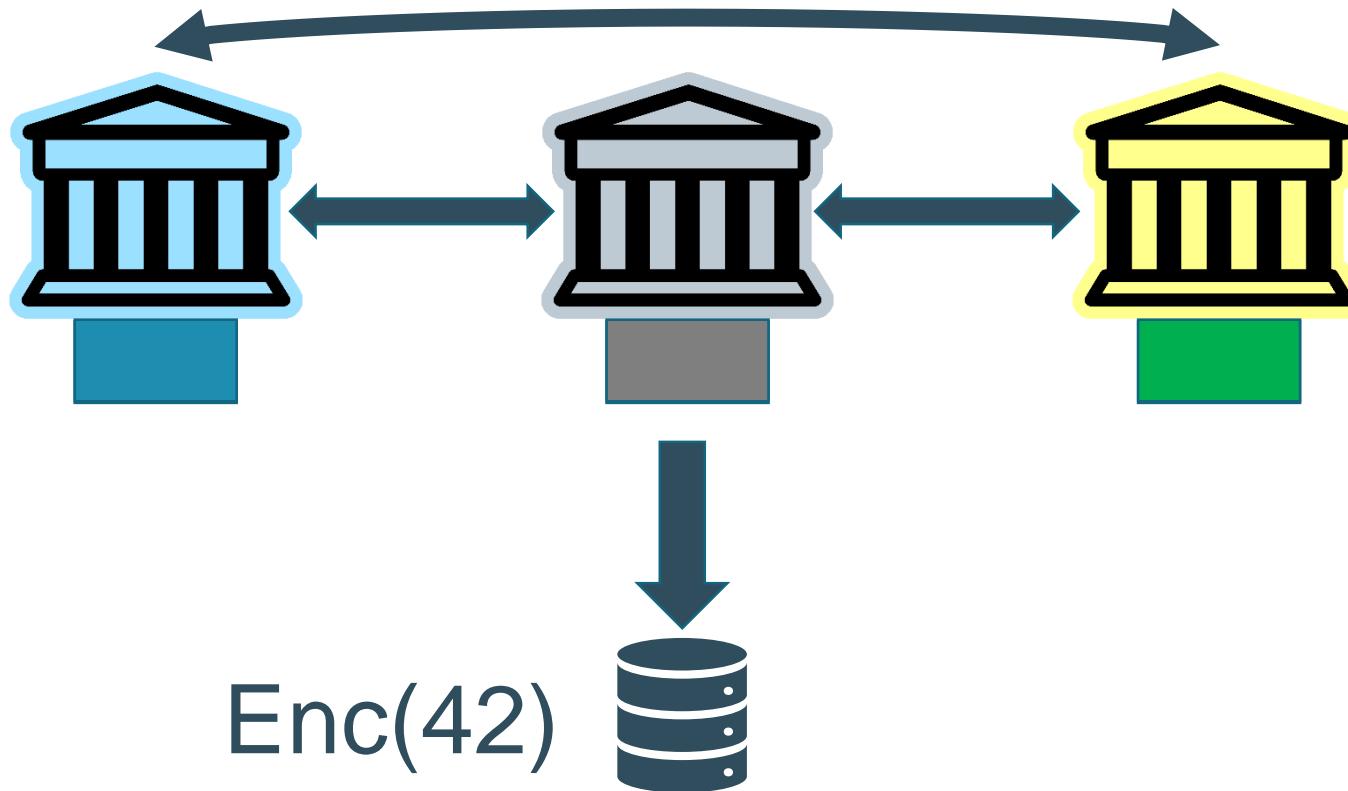
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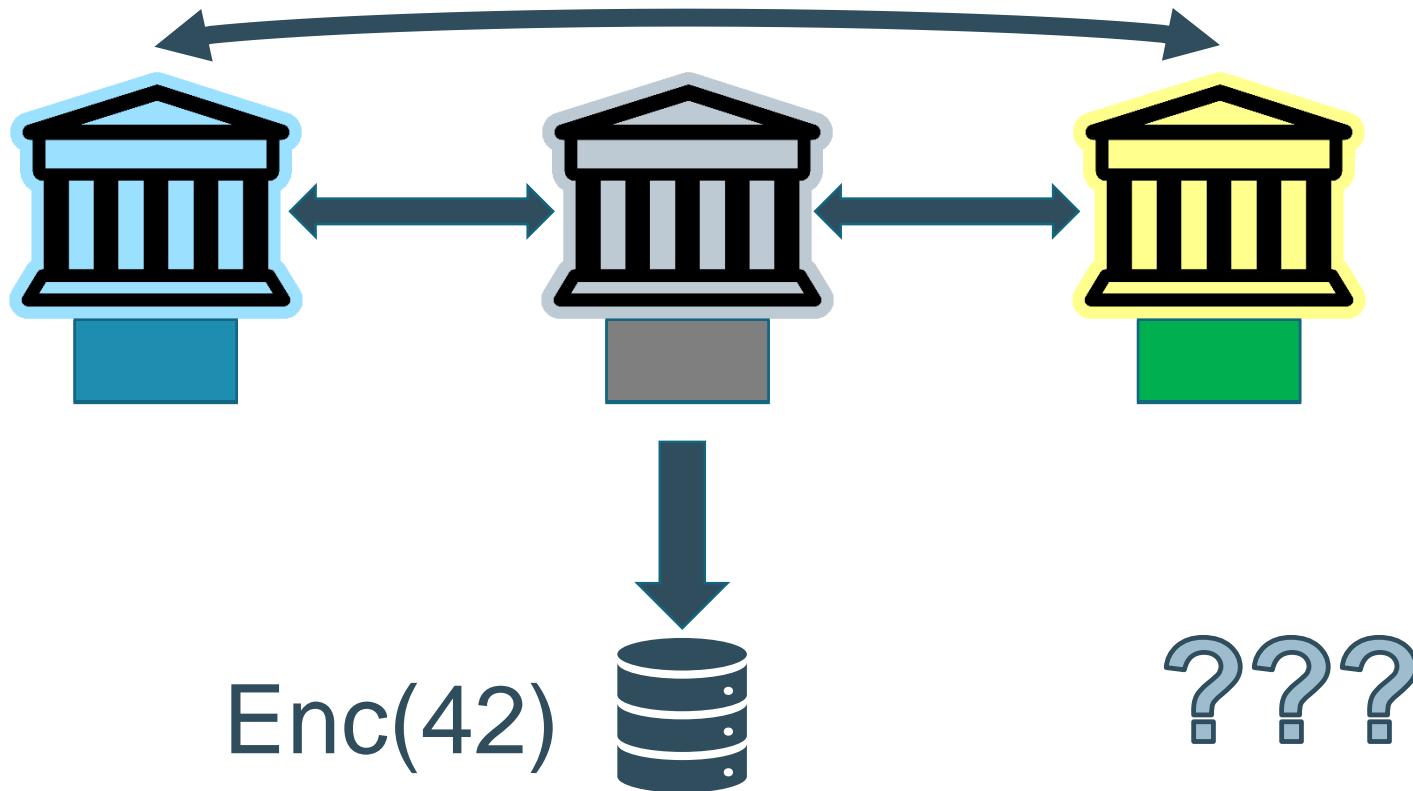
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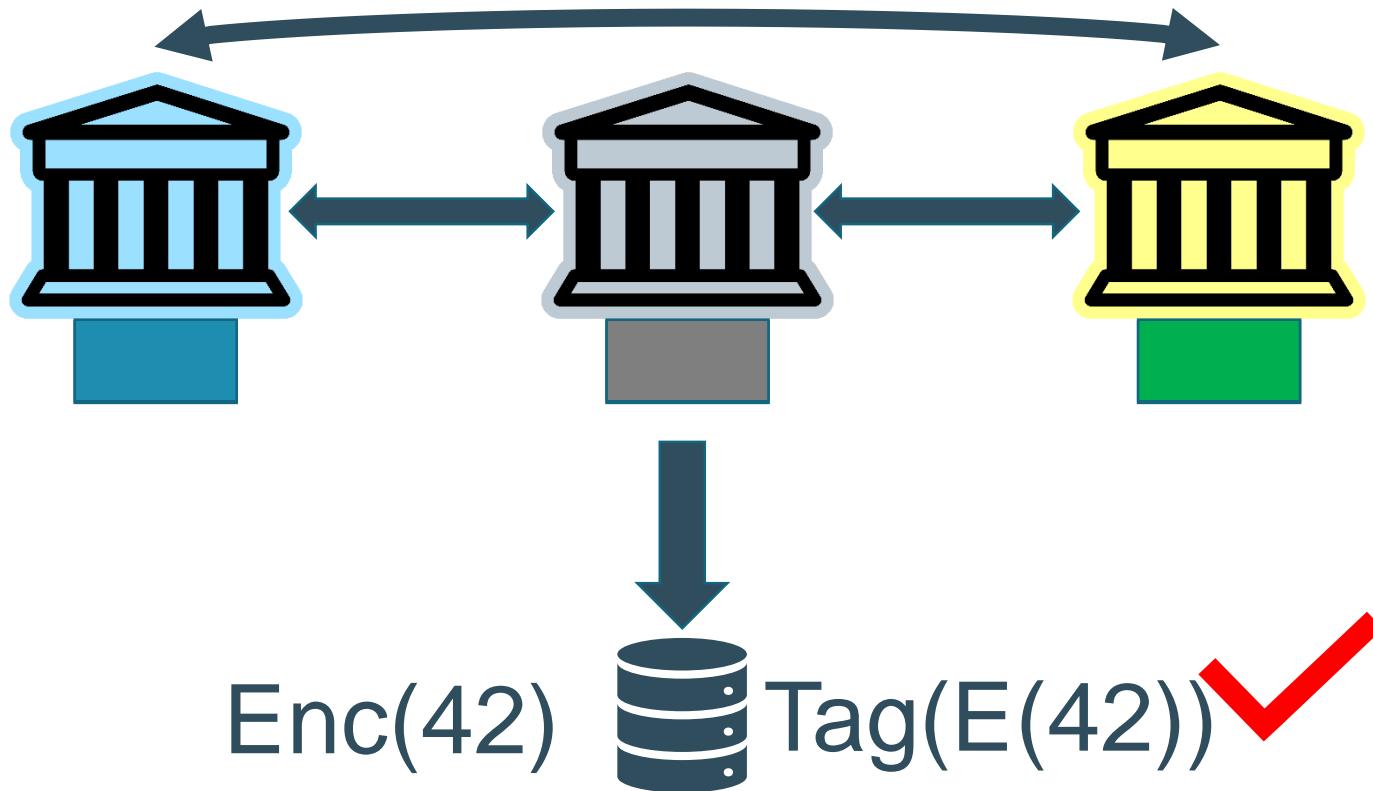
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**For free: detect malicious encryption keys.**

Enc(42)  Tag(E(42)) 

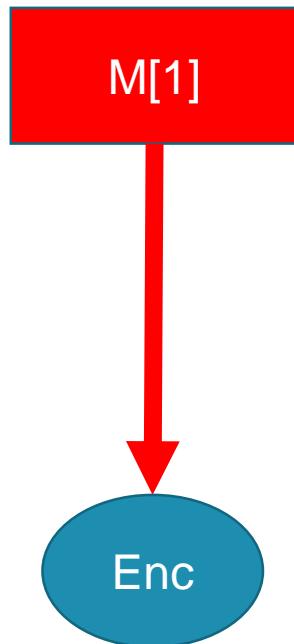
# Prior work – PRFs in MPC (CCS'16)

Enc(42)  Tag(Enc(42))

- MiMC
- Legendre PRF

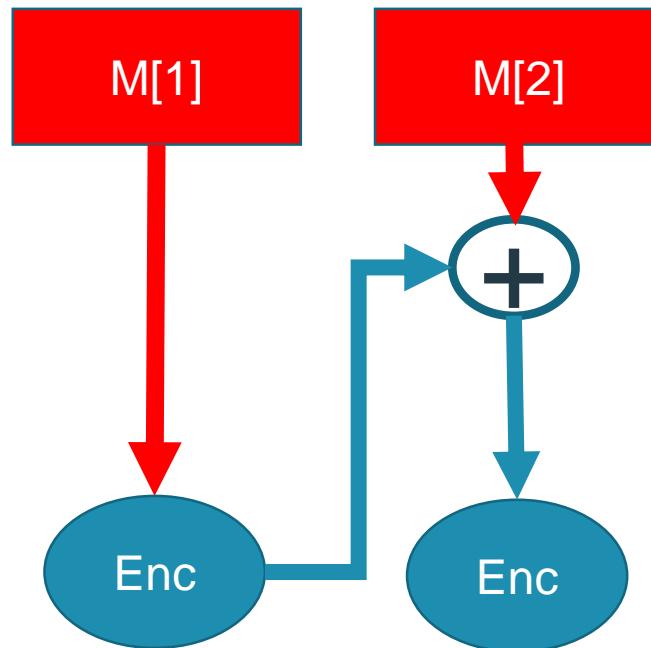
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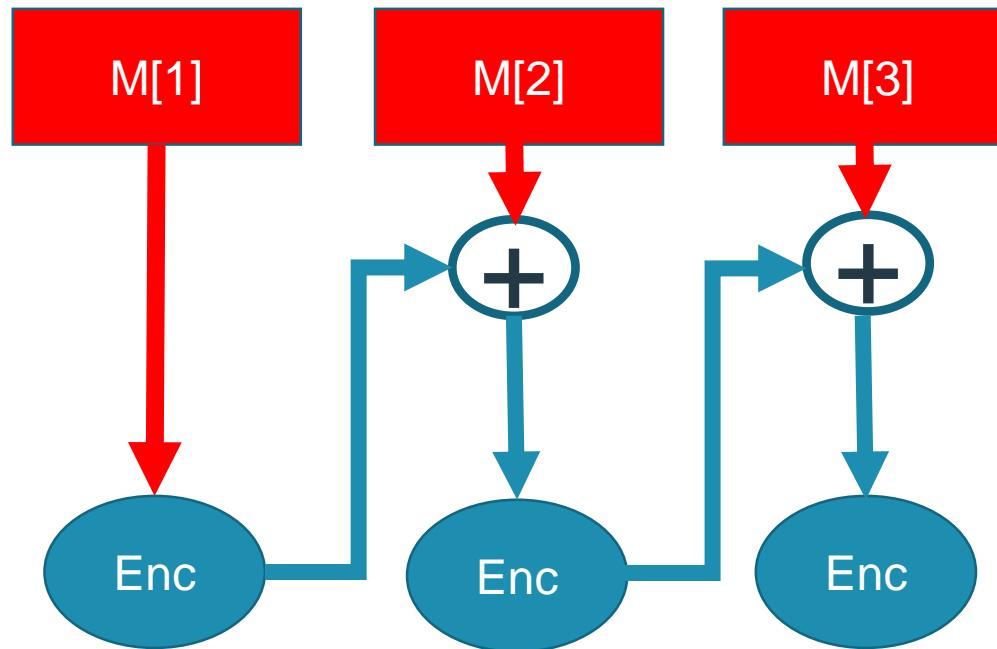
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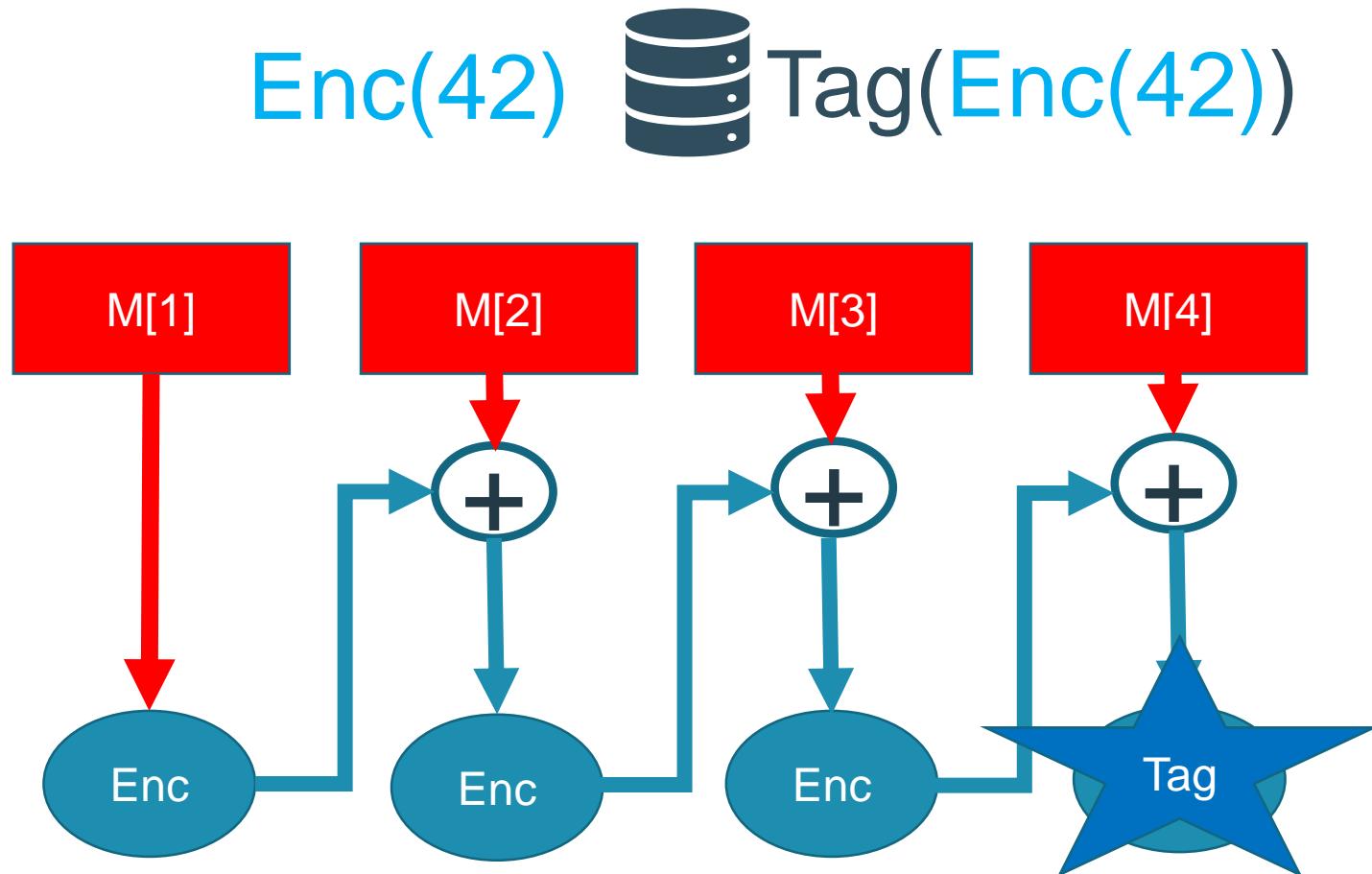


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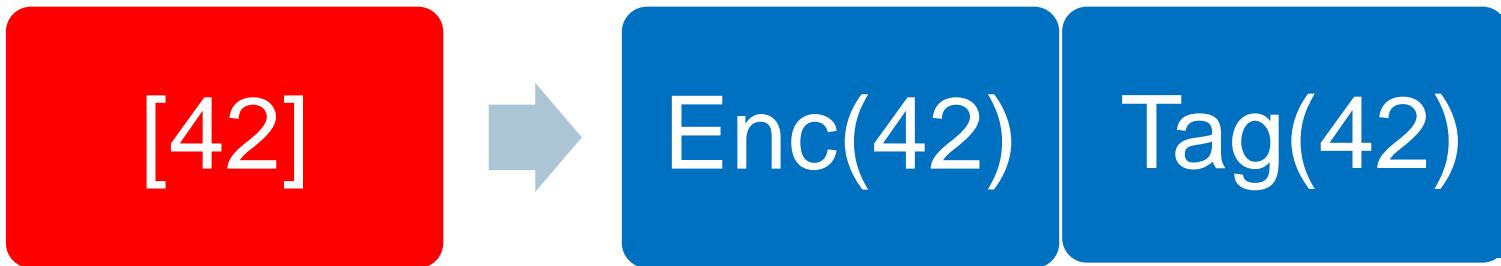
Enc(42)  Tag(Enc(42))



# Prior work – PRFs in MPC (CCS'16)



# What we have done



- Analyze AE in Multiparty Computation (MPC).
- Useful MPC happens in  $\mathbb{F}_p \Rightarrow$  Need AE and PRFs modp.
- Look for parallel AE: CTR+PMAC, OTR.

# The story



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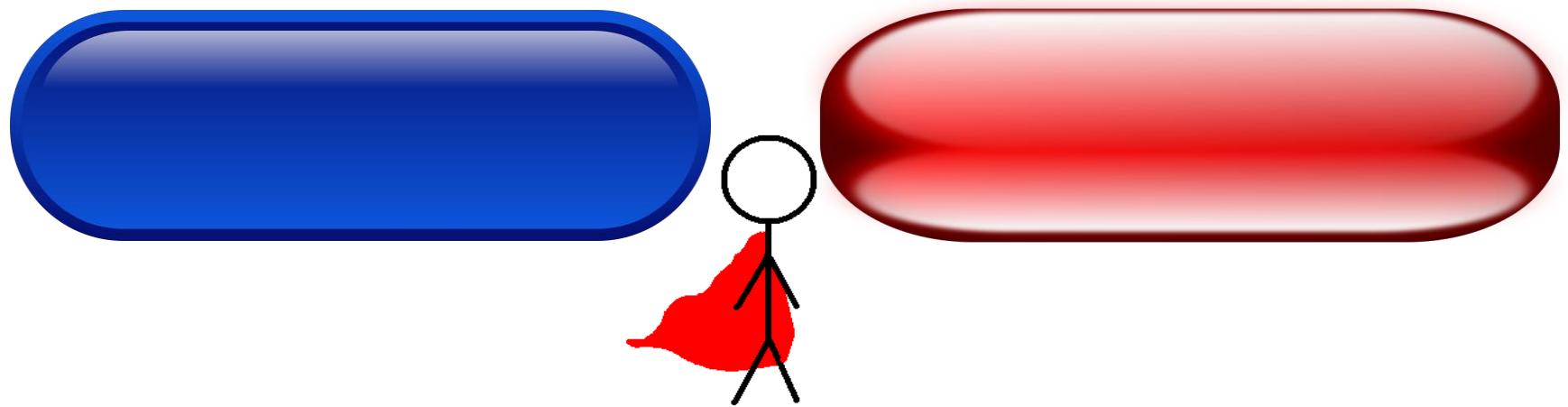
# The story



‘You take the blue pill—the story ends, you wake up in your bed and believe whatever you want to believe.

You take the *red* pill—you stay in Wonderland, and I show you how deep the rabbit hole goes.’

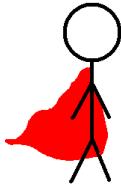
# The story



‘You take the blue pill—the story ends, you wake up in your bed and believe whatever you want to believe.

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# Down the rabbit hole - MPC with Secret Sharing



$$x = x_1 + \dots + x_n$$

Each  $P_i$  has  $[x] \leftarrow x_i$



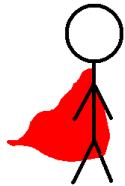
$$[x] \leftarrow x_2$$

$$[x] \leftarrow x_1$$



$$[x] \leftarrow x_3$$

# MPC Preprocessing Phase



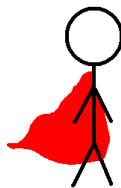
**Generate triples**  
 **$[c] = [a][b]$**

# MPC Preprocessing Phase



**Generate triples**  
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# MPC Preprocessing Phase



# MPC Online Phase

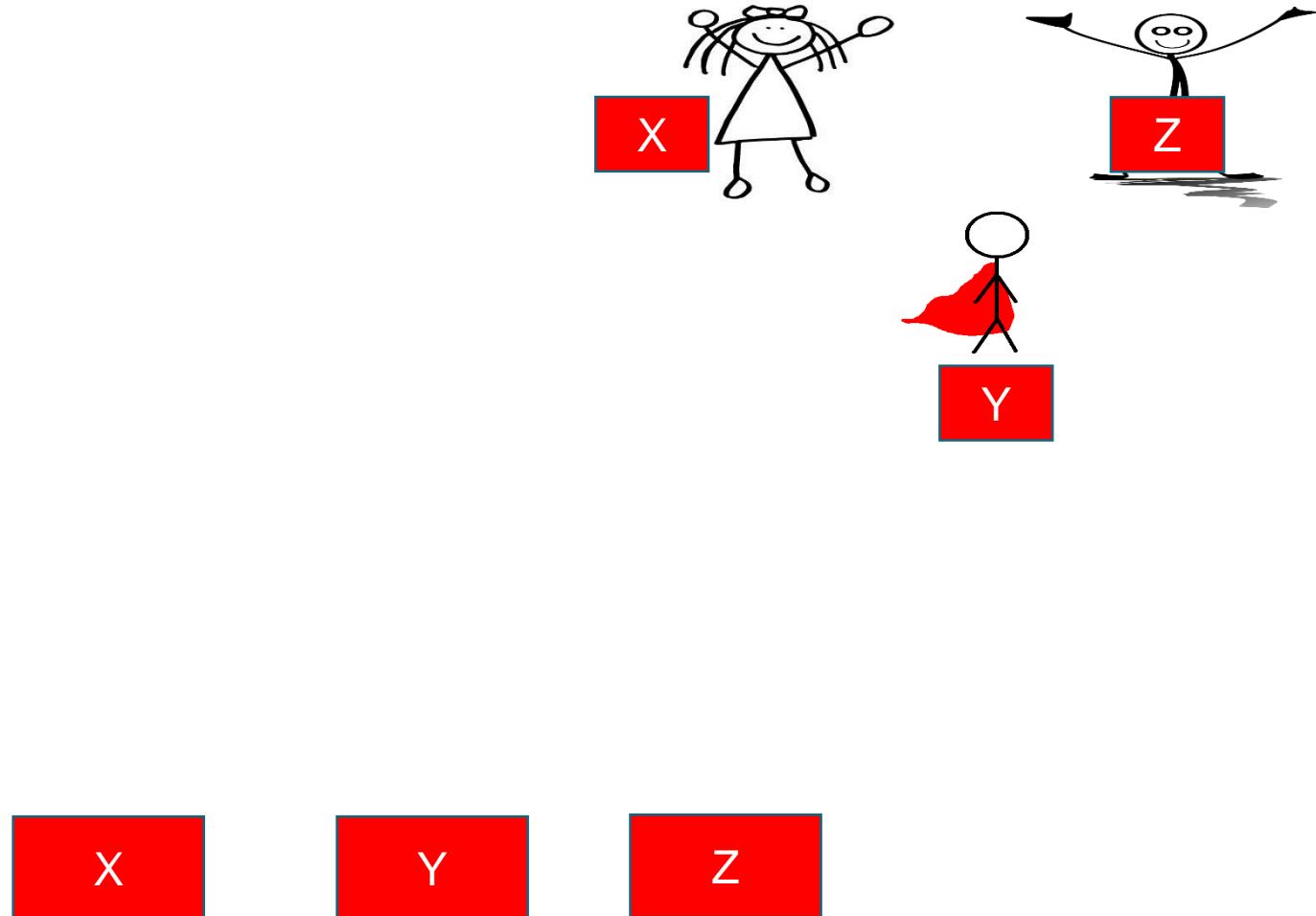


**Use Triples.**

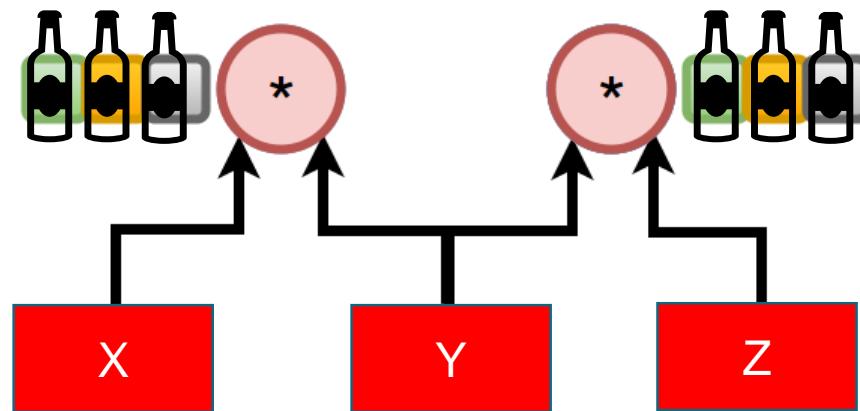
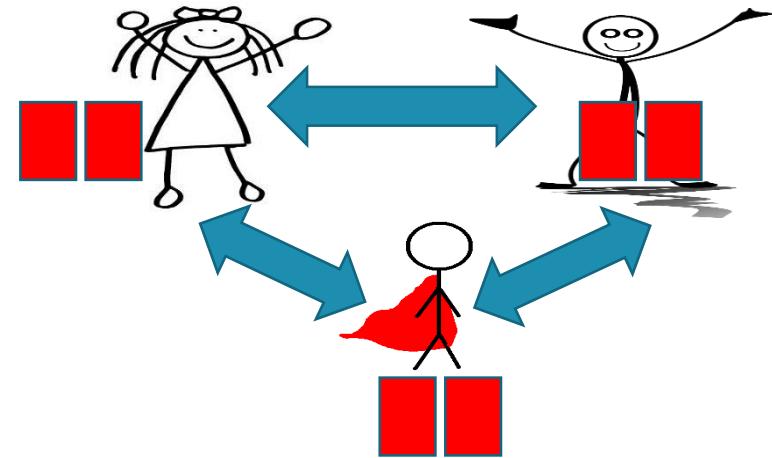
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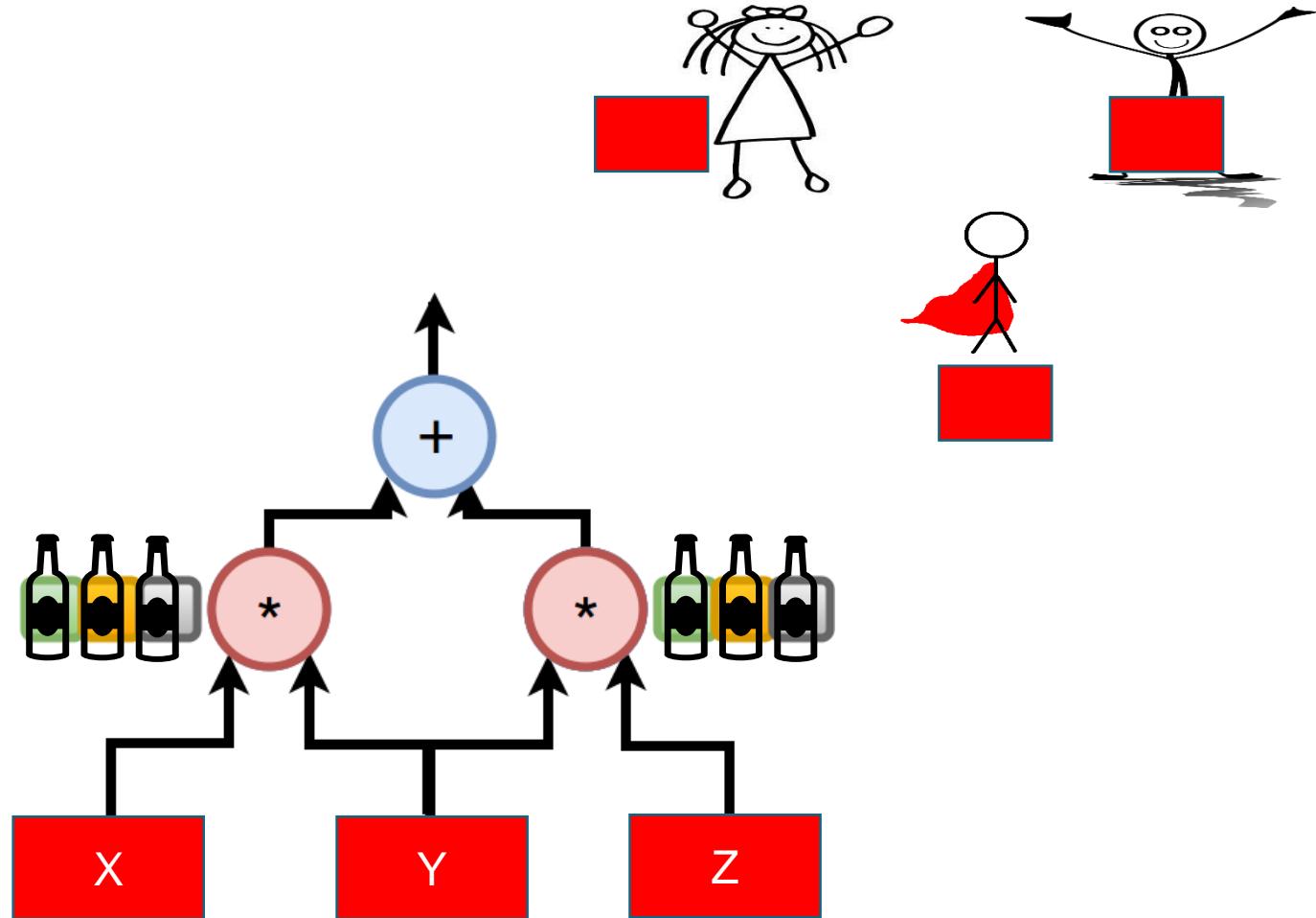
# MPC Circuit Evaluation



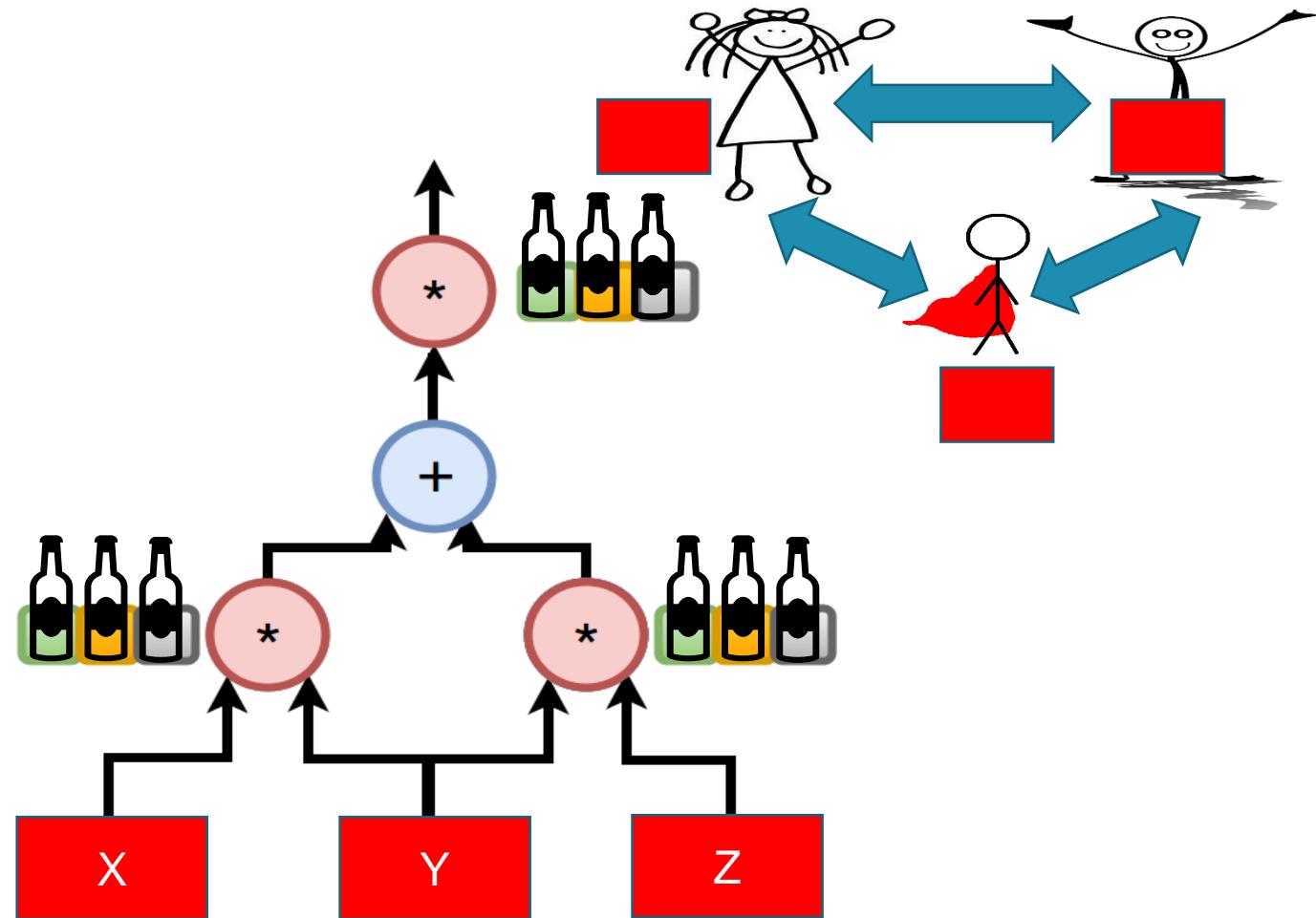
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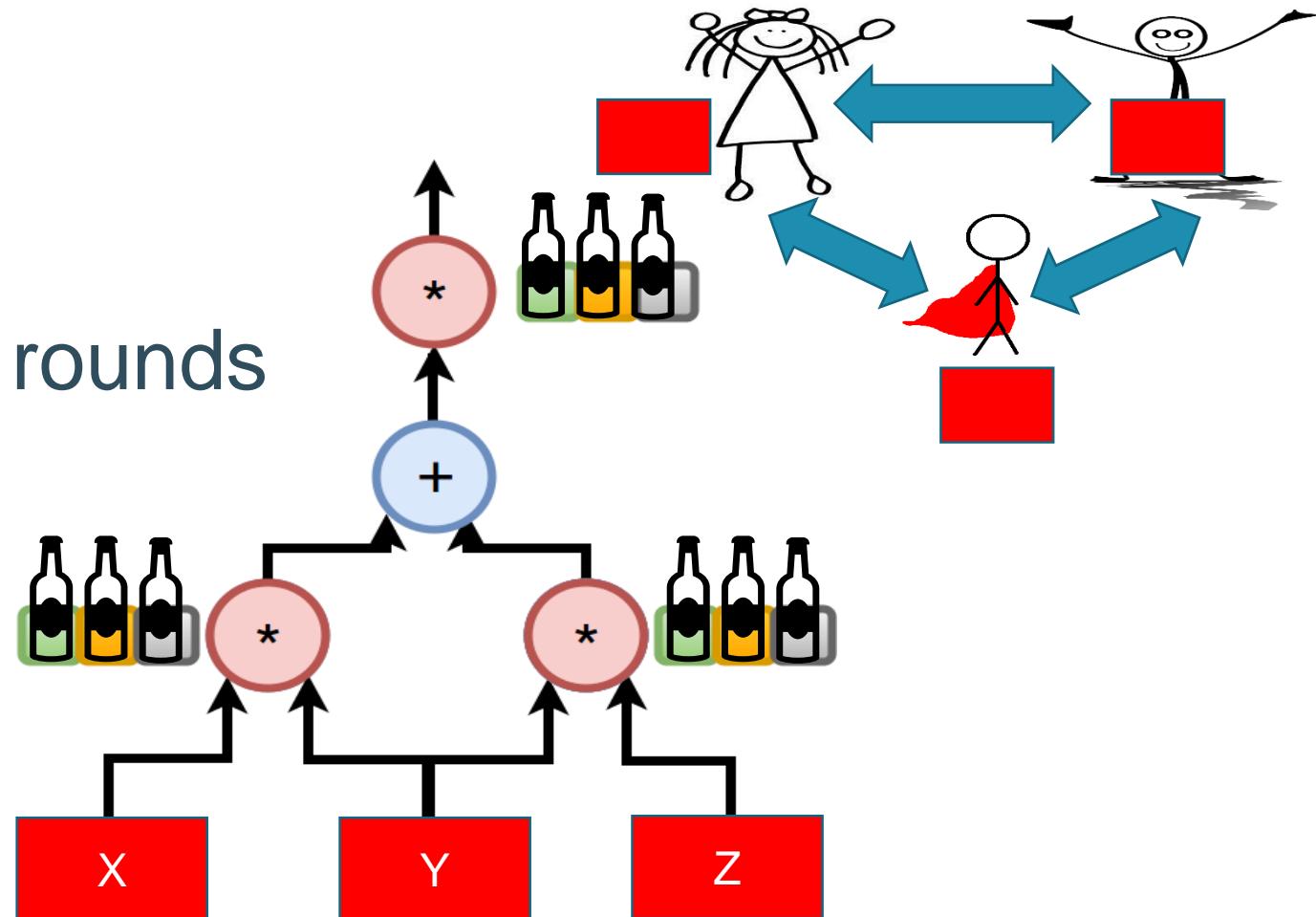


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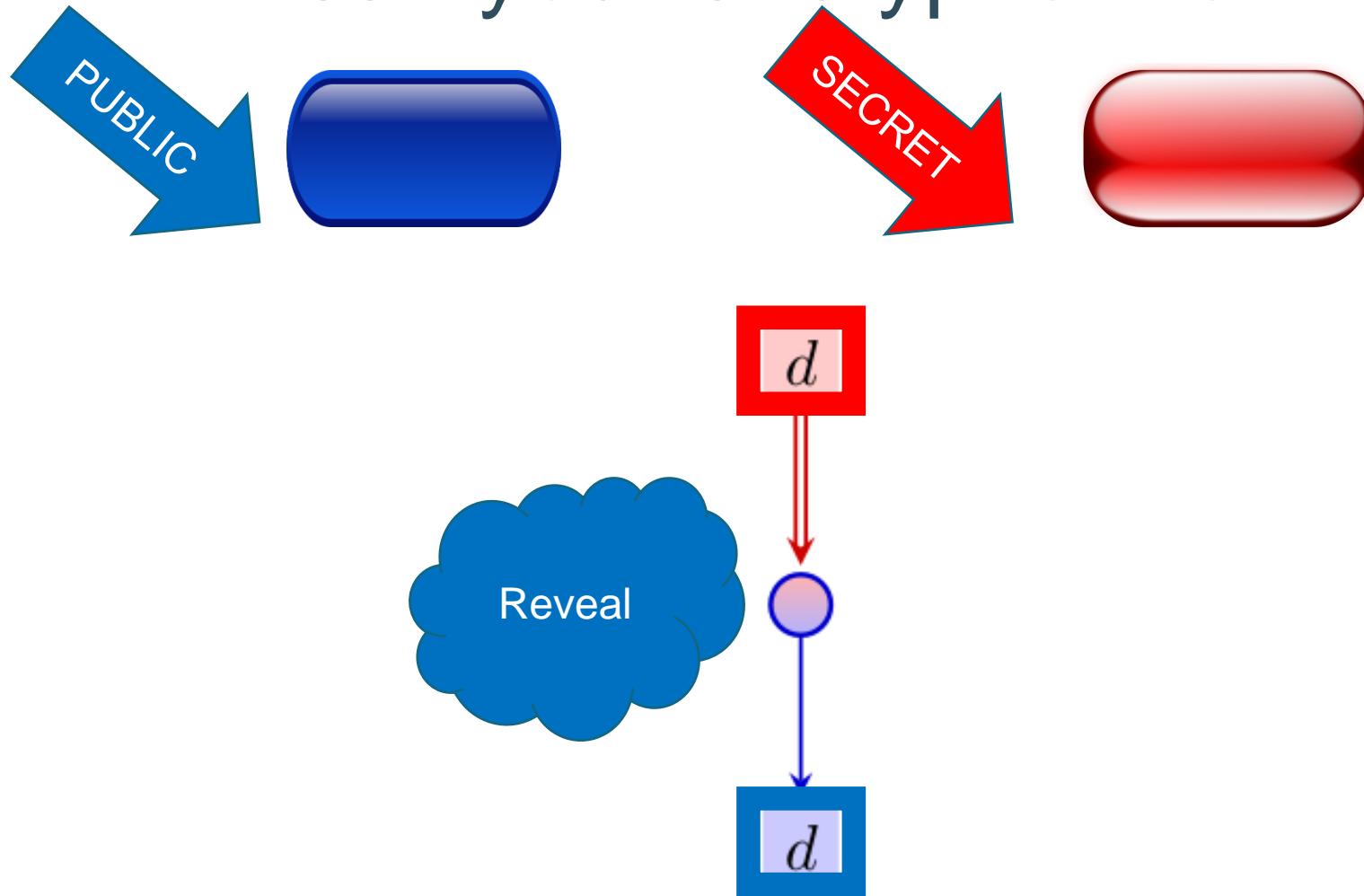


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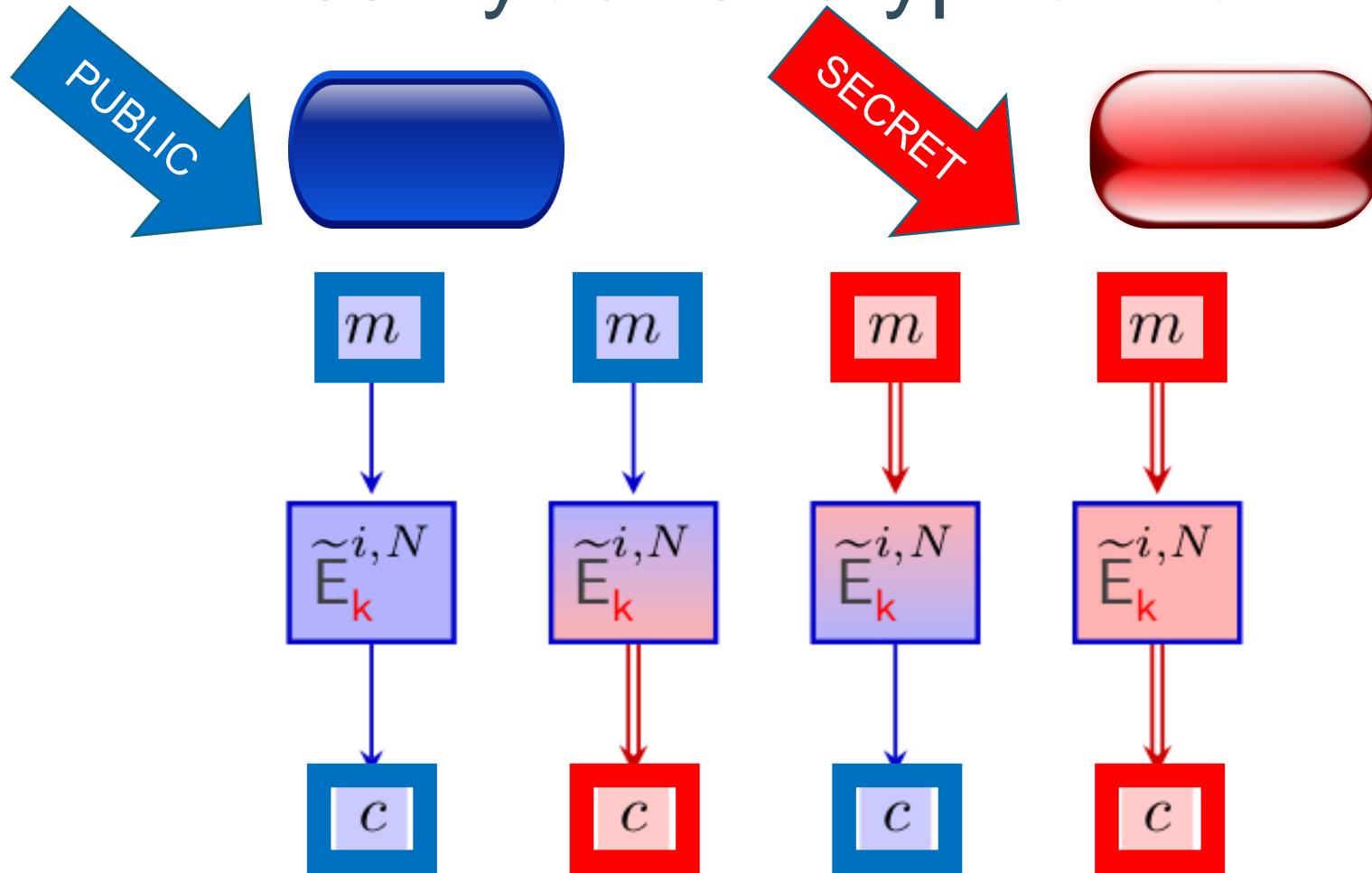
3 triples.  
2 comm. rounds



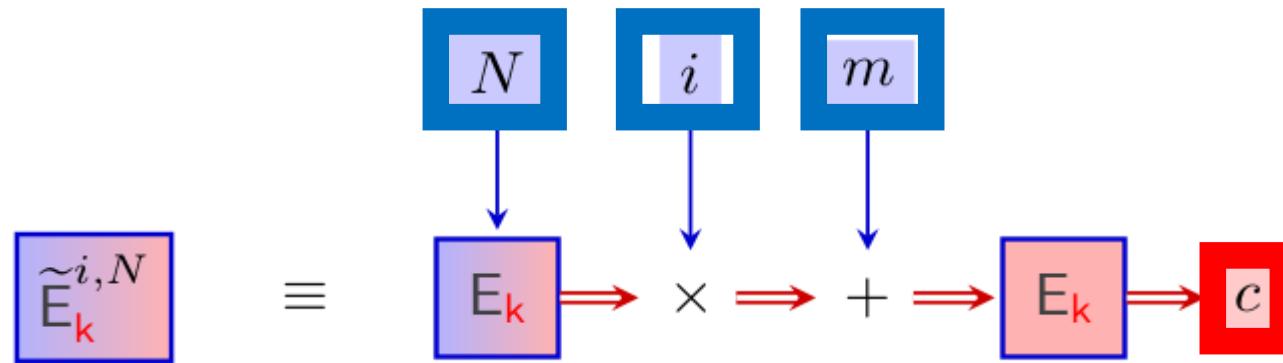
# Tweak your encryption to MPC



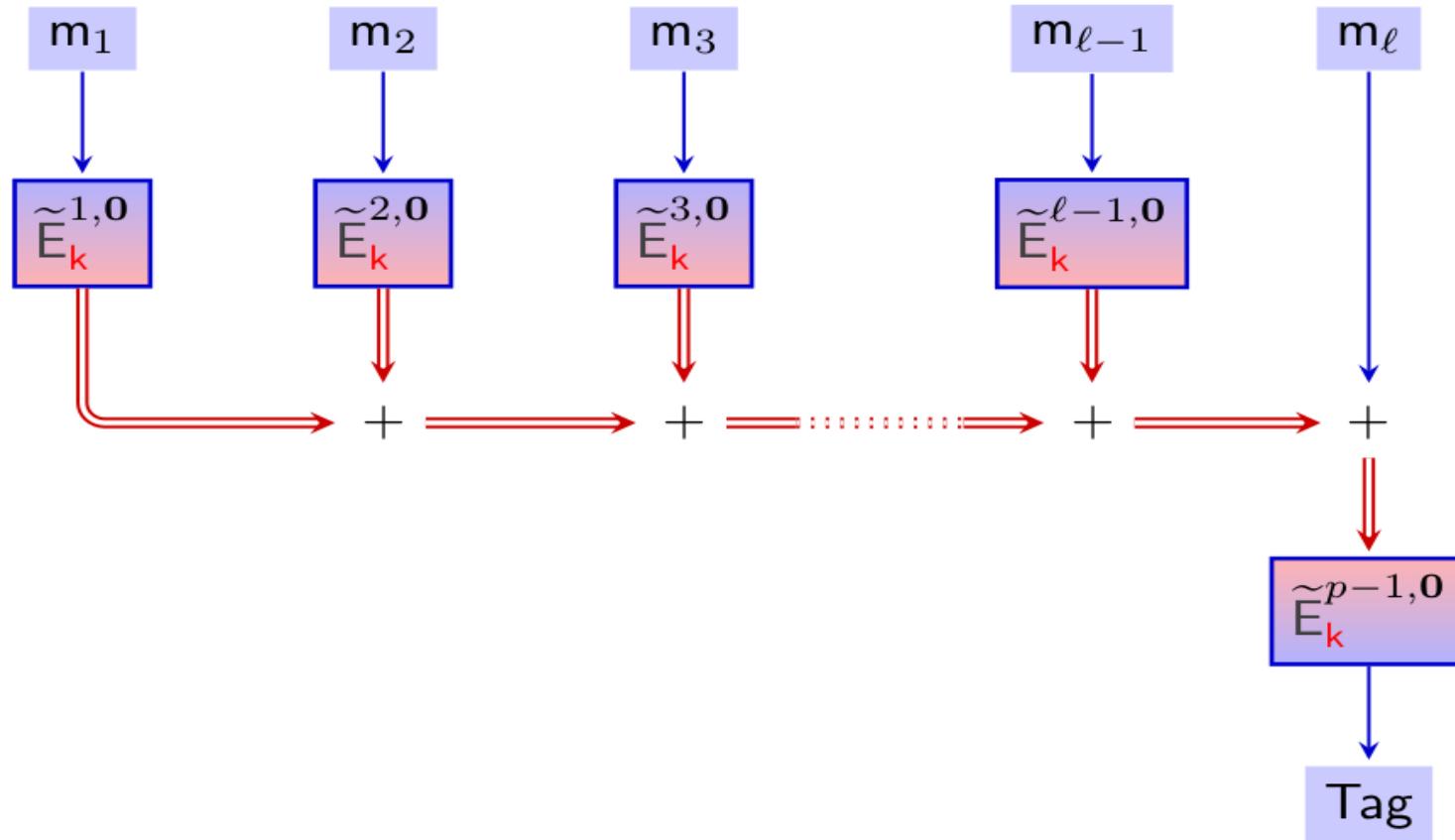
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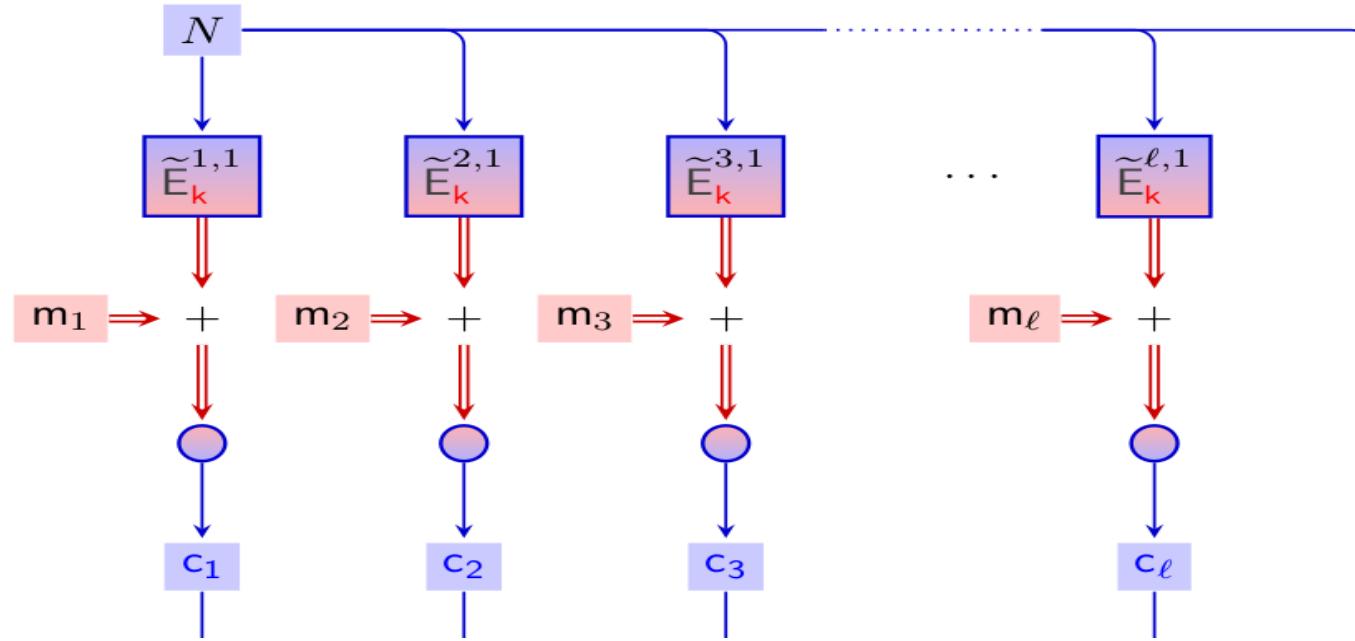
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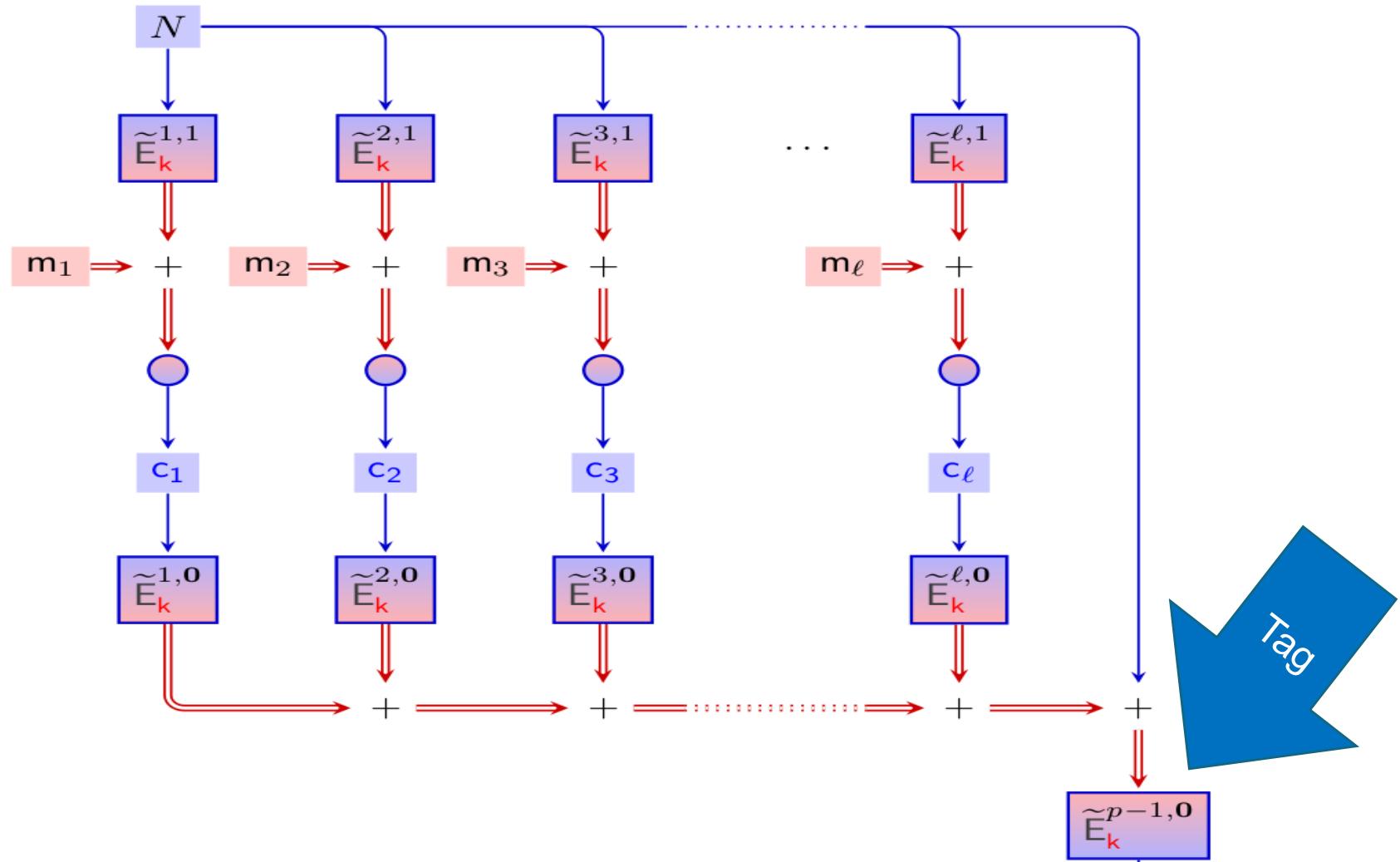
# How-to compute PMAC



# Let's do AE with CTR+pPMAC



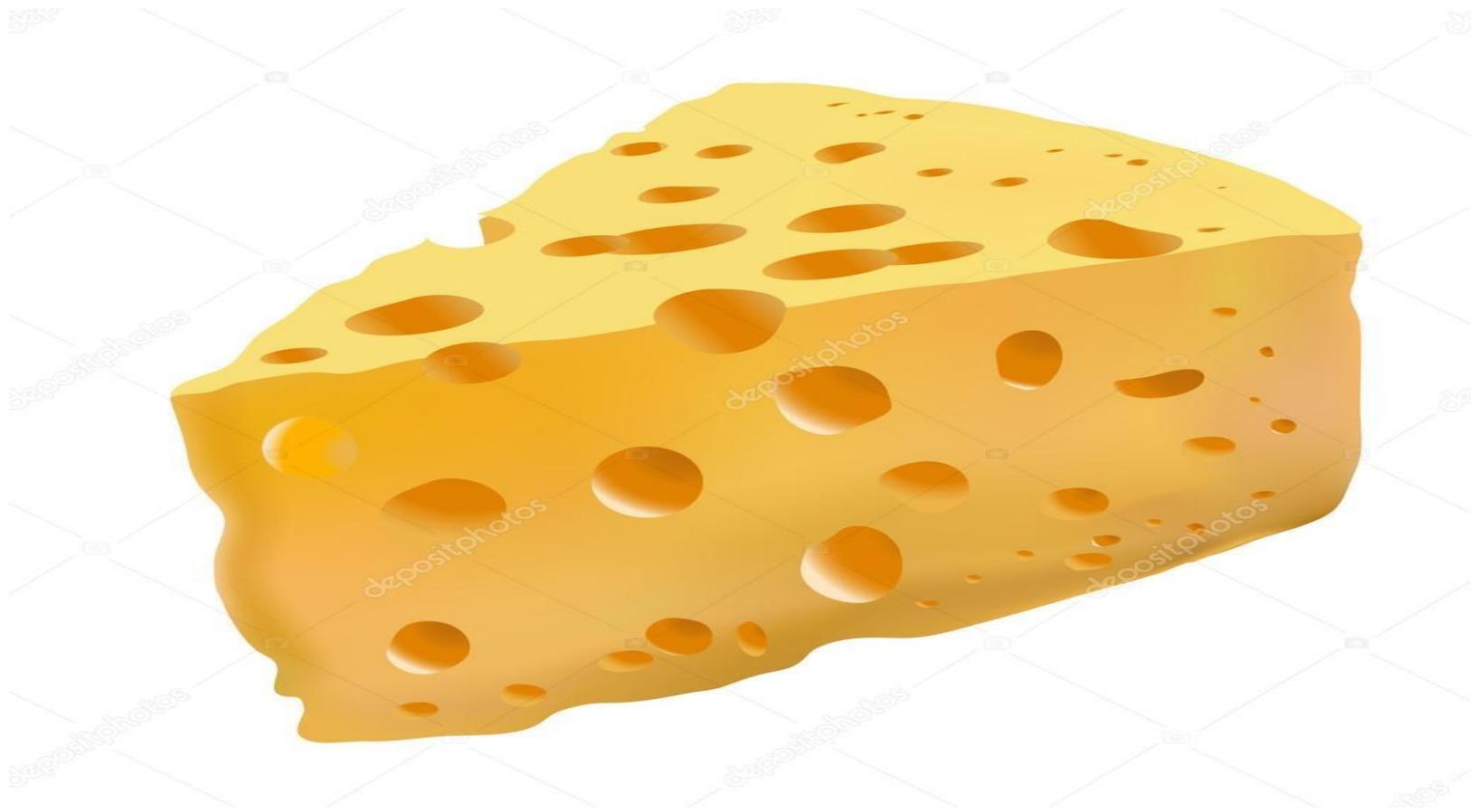
# Let's do AE with CTR+pPMAC



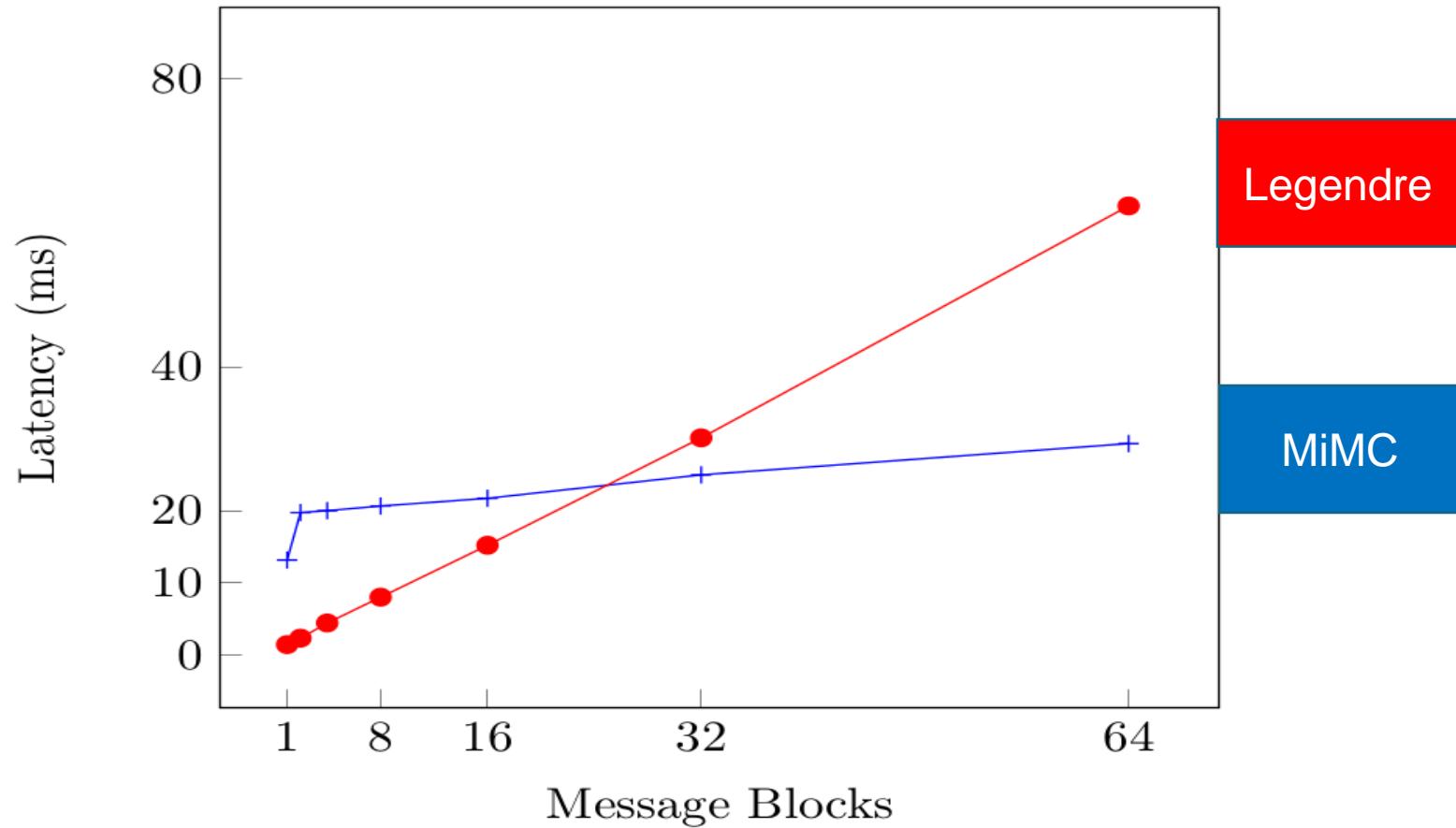
# When ideal meets real



# When ideal meets real – surprise!



# When ideal meets real – surprise!



# Other competitive modes

PRF	Mode	Online cost	
		Rounds (Enc/Dec)	Openings
Leg	CTR+pPMAC	7/6	$768 \cdot \ell + \ell$
MiMC	CTR+pPMAC	221/147	$146 \cdot \ell + \ell + 1$
Leg	CTR+HtMAC	5/4	$384 \cdot (\ell + 1) + \ell$
MiMC	CTR+HtMAC	148/75	$73 \cdot (\ell + 1) + \ell + 1$
Leg	OTR	6/9	$384 \cdot (\ell + 128) + \ell$
MiMC	OTR	220/295	$73 \cdot (\ell + 2) + \ell + 1$

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# Some open problems

- Preprocessing scales linearly in terms of number of message blocks - roughly  $n$  PRFs for  $n$  messages.
- Number of rounds of a cipher vs. multiplicative depth in MPC.

# Thank you!

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- Questions?