New Constructions of MACs from (Tweakable) Block Ciphers

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New Constructions of MACs from (T)BCs

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 we propose four new MAC constructions based on a (tweakable) block cipher:

	stateless and deterministic	nonce-based/randomized
TBC-based	Hash-as-Tweak (HaT)	Nonce-as-Tweak (NaT)
BC-based	Hash-as-Key (HaK)	Nonce-as-Key (NaK)

- all four constructions are secure beyond the birthday bound
- TBC-based constructions are provably secure in the standard model
- BC-based constructions are provably secure in the ideal cipher model
- nonce-based constructions provide graceful security degradation with the maximal number of nonce repetitions

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Generalities

Stateless Deterministic MACs

Nonce-Based MACs

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MAC definition



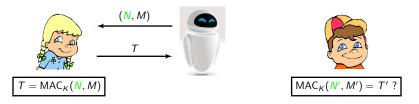
Security Definition

The adversary is allowed

- q MAC queries $T = MAC_K(N, M)$
- v verification queries (forgery attempts) (N', M', T')

and is successful if one of the verification queries (N', M', T') passes and no previous MAC query (N', M') returned T'.

MAC definition



Security Definition

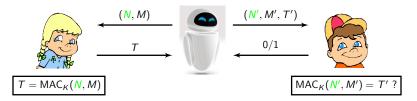
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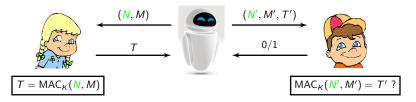
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Three types of MAC

 stateless and deterministic: MAC function only takes the key and the message as input (Variable-input-length PRF ⇒ stateless deterministic MAC)

• nonce-based:

- MAC function takes as input a non-repeating nonce N in addition to the key and the message M
- security model: nonces are chosen by the adversary, any nonce can be used at most μ times in MAC queries
- $\mu = 1$: nonce-respecting adversary
- $\mu > 1$: nonce-misusing adversary
- randomized: MAC function takes as input random coins (generated by the sender) in addition to the key and the message

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Graceful nonce-misuse security degradation

- the security of some nonce-based MACs collapses if a single nonce is used twice (e.g. GMAC)
- ideally, security should degrade gracefully in case nonces are repeated
- any BBB-secure nonce-based MAC with graceful security degradation can be turned into a BBB-secure randomized MAC by choosing *n*-bit nonces uniformly at random:

$$\mathbf{Adv}_{F}^{\mathsf{rand-MAC}}(q,v) \leq \underbrace{\frac{q^{\mu+1}}{2^{\mu(n+1)}}}_{\substack{\mu-\mathsf{multicoll.}\\\mathsf{proba.}}} + \underbrace{\mathbf{Adv}_{F}^{\mathsf{nonce-MAC}}(q,v,\mu)}_{\mathsf{small for } \mu > 1}$$

for any value of $\mu = maximal$ number of nonce repetitions.

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Building blocks: BCs and TBCs



n = block size t = tweak size

• block cipher E: for each key K, $X \mapsto E(K, X)$ is a permutation

- tweakable block cipher E: for each key K and each tweak W, $X \mapsto \widetilde{E}(K, W, X)$ is a permutation
- one can think of a keyed TBC \tilde{E}_K as an "imperfect" PRF from (n + t) bits to n bits
- if any tweak W is used at most "a few" times, E_K is close to a random (n + t)-to-n-bit function

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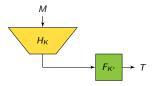
Nonce-Based MACs

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The "standard" UHF-then-PRF Construction



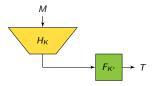
 based on a fixed-input-length PRF F and an ε-almost universal (ε-AU) hash function H:

$$\forall M \neq M', \ \Pr[K \leftarrow_{\$} \mathcal{K} : H_{\mathcal{K}}(M) = H_{\mathcal{K}}(M')] \leq \varepsilon$$

- *H* can be statistically secure (polynomial evaluation) or computationally secure (BC/TBC-based)
- most MACs are (variants of) this construction (UMAC, EMAC, OMAC, CMAC, PMAC, NMAC)

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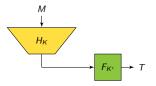
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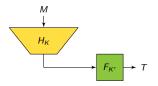


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Security of UHF-then-PRF



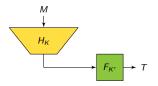
• birthday-bound-secure w.r.t. H collision probability ε

$$\mathsf{Adv}^{\mathsf{PRF}}_{F \circ H}(q) \leq rac{q^2 arepsilon}{2} + \mathsf{Adv}^{\mathsf{PRF}}_F(q)$$

- typical instantiation from a block cipher E:
 - $H \leftarrow \mathsf{CBC-MAC}[E]$ or $\mathsf{PMAC}[E]$ ($\varepsilon \simeq 2^{-n}$)
 - $F \leftarrow E$
 - \Rightarrow BB-security

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Security of UHF-then-PRF



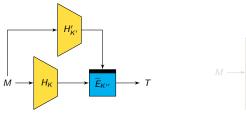
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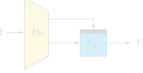
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Construction 1: Hash-as-Tweak (HaT)



Hash-as-Tweak (HaT)



Hash-then-TBC

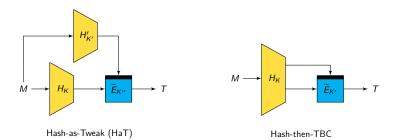
• BBB-secure assuming H and H' are ε -AU secure:

$$\mathsf{Adv}_{\mathsf{HaT}}^{\mathsf{MAC}}(q,v) \leq q^2 \varepsilon^2 + qv \varepsilon^2 + (\ldots)$$

• follow-up work: Hash-then-TBC construction [LN17], BBB-secure under more complex UHF-type properties of *H*

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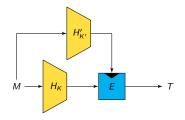
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Construction 2: Hash-as-Key (HaK)



• output transformation unkeyed \Rightarrow *H* and *H*' must be ε '-uniform:

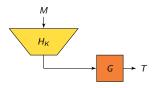
$$\forall M, \ \forall Y, \ \Pr[K \leftarrow_{\$} \mathcal{K} : H_K(M) = Y] \leq \varepsilon'$$

 BBB-secure in the ideal cipher model assuming H and H' are ε-AU and ε'-uniform:

$$\mathsf{Adv}_{\mathsf{HaK}}^{\mathsf{MAC}}(q,v) \leq q^2 \varepsilon^2 + qv \varepsilon^2 + (\ldots)$$

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The UHF-then-RO construction



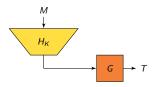
- Hash-as-Key (HaK) is a special case of the "UHF-then-RO" construction
- modeling G as a random function oracle (q_G queries), the construction is secure if H is ε -AU and ε' -uniform:

$$\mathsf{Adv}^{\mathsf{PRF}}_{\mathsf{G}\circ\mathsf{H}}(q,q_{\mathsf{G}}) \leq rac{q^2arepsilon}{2} + qq_{\mathsf{G}}arepsilon^{2}$$

• security proof under a standard assumption on G?

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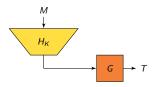
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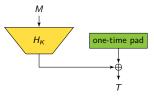
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The Wegman-Carter construction [GMS74, WC81]

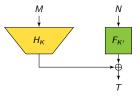


- based on an ε-almost xor-universal (ε-AXU) hash function H:
 ∀M ≠ M', ∀Y, Pr[K ←_{\$} K : H_K(M) ⊕ H_K(M') = Y] ≤ ε
- in practice, OTPs are replaced by a PRF applied to a nonce N
- *H* usually based on polynomial evaluation (GHASH, Poly1305)
- "optimal" security:

$$\mathsf{Adv}_{\mathsf{WC}}^{\mathsf{nonce}\operatorname{-MAC}}(q,v) \leq v\varepsilon + \mathsf{Adv}_{F}^{\mathsf{PRF}}(q+v)$$

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The Wegman-Carter construction [GMS74, WC81]

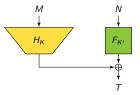


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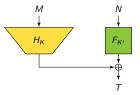


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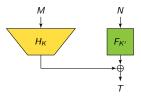


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Wegman-Carter weaknesses



- in practice, F is replaced by a block cipher
 → Wegman-Carter-Shoup (WCS) construction
- provable security drops to birthday bound [Sho96, Ber05]

$$\mathsf{Adv}^{ ext{nonce-MAC}}_{ ext{WCS}}(q,v) \leq varepsilon + rac{(q+v)^2}{2\cdot 2^n} + \mathsf{Adv}^{ ext{PRP}}_E(q+v)$$

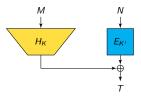
 nonce-misuse problem: a single nonce repetition can completely break security [Jou06, HP08] (esp. for polynomial hashing)

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Wegman-Carter weaknesses



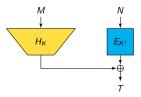
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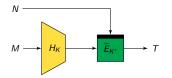
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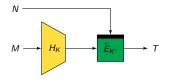
- if nonces don't repeat to often, $\tilde{E}_{K'}$ is close to a perfect PRF
- graceful security degradation with maximal nonce multiplicity μ

$$\operatorname{\mathsf{Adv}}_{\operatorname{\mathsf{NaT}}}^{\operatorname{\mathsf{nonce-MAC}}}(q,v) \leq 2(\mu-1)q\varepsilon + \mu v\varepsilon + (\ldots)$$

can be seen as a special case of the (PRF-based) WMAC construction [BC09]

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Construction 3: Nonce-as-Tweak (NaT)



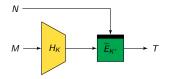
- if nonces don't repeat to often, $\widetilde{E}_{K'}$ is close to a perfect PRF
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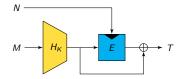
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Construction 4: Nonce-as-Key (NaK)



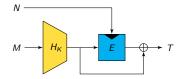
• provably secure in the ideal cipher model, assuming H is $\varepsilon\text{-AXU}$ and $\varepsilon'\text{-uniform}$

$$\mathsf{Adv}_{\mathsf{NaK}}^{\mathsf{nonce-MAC}}(q, \mathbf{v}) \leq \mu q \varepsilon + (\ldots)$$

- graceful security degradation with maximal nonce multiplicity μ
- Davies-Meyer mode required to make the output function non-invertible!

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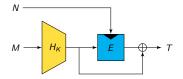
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• we proposed four new MAC constructions secure beyond the birthday bound:

	stateless and deterministic	nonce-based/randomized
TBC-based	Hash-as-Tweak (HaT)	Nonce-as-Tweak (NaT)
BC-based	Hash-as-Key (HaK)	Nonce-as-Key (NaK)

- all security proofs rely on the standard H-coefficients technique [Pat08, CS14]
- our work does not address how to construct the UHF from a BC or TBC but many existing constructions can be used (PMAC/PMAC1 [BR02, Rog04], ZHASH [IMPS17], etc.)
- Nonce-as-Tweak (NaT) used in CAESAR candidate Deoxys v1.4

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The end...

Thanks for your attention!

Comments or questions?

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New Constructions of MACs from (T)BCs

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