

Constructing Committing and Leakage-Resilient Authenticated Encryption

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Abstract. The main goal of this work is to construct authenticated encryption (AE) that is both committing and leakage-resilient. As a first approach for this we consider generic composition as a well-known method for constructing AE schemes. While the leakage resilience of generic composition schemes has already been analyzed by Barwell et al. (Asiacrypt'17), for committing security this is not the case. We fill this gap by providing a separate analysis of the generic composition paradigms with respect to committing security, giving both positive and negative results: By means of a concrete attack, we show that Encrypt-then-MAC is not committing. Furthermore, we prove that Encrypt-and-MAC is committing, given that the underlying schemes satisfy security notions we introduce for this purpose. We later prove these new notions achievable by providing schemes that satisfy them. MAC-then-Encrypt turns out to be more difficult due to the fact that the tag is not outputted alongside the ciphertext as it is done for the other two composition methods. Nevertheless, we give a detailed heuristic analysis of MAC-then-Encrypt with respect to committing security, leaving a definite result as an open task for future work. Our results, in combination with the fact that only Encrypt-then-MAC yields leakage-resilient AE schemes, show that one cannot obtain AE schemes that are both committing and leakage-resilient via generic composition. As a second approach for constructing committing and leakage-resilient AE, we develop a generic transformation that turns an arbitrary AE scheme into one that fulfills both properties. The transformation relies on a keyed function that is both binding, i.e., it is hard to find key-input pairs that result in the same output, and leakage-resilient pseudorandom.

Keywords: Authenticated Encryption · Committing Security · Leakage Resilience

1 Introduction

Authenticated encryption (AE) with associated data is the modern day version of what cryptography was historically: a method to secure the communication between two parties. Classically, secure communication is understood to entail confidentiality and authenticity. The former prevents anyone except the rightful receiver of a ciphertext to recover the message from it, while the latter ensures that the ciphertext originates indeed from the claimed sender and was not manipulated during transmission. In an AE scheme, the ciphertext is generated by encryption of the message under a context (K, N, A) , consisting of a key K , a nonce N , and associated data A . To achieve the above security goals, both the message and associated data need to be authenticated, whereas confidentiality is required only for the message.

Besides the standard security notions—confidentiality and authenticity—there are several, more advanced security notions. This encompasses, for instance, security against

related-key attacks [FKOS22] which enables the adversary to obtain ciphertexts generated by keys that exhibit a certain relation, anonymous AE [CR19] where ciphertexts have to conceal the nonce to provide anonymity of the communicating parties, leakage-resilient AE [BMOS17] where the adversary can obtain extra information via side-channels, and committing security [BH22] which prevents adversaries from finding ciphertexts that decrypt under more than one key. These advanced security notions are typically analyzed isolated and not in conjunction. However, depending on the use-case, a joint consideration of multiple security notions might be sensible. As there is little analysis on the interplay between the notions, unwanted effects might occur: While there are transformations, which one applies to an AE scheme to obtain certain security properties, concatenating them might not have the desired outcome. A successive application of two or more transformations could result in a scheme that is not secure with respect to all of the security notions, but—in the worst case—only the notion corresponding to the last transformation that was applied. This stems from the fact that these transformations are usually proven to achieve the desired security property while maintaining the standard AE security, i.e., the last transformation might subvert the additional guarantees from the previous ones. On the other hand, it is possible that a transformation achieves security with respect to additional notions besides the one it was developed for. This would make further changes to the scheme redundant and might result in unnecessary overhead. In total, deepening our understanding of the relation between advanced security notions brings various benefits with it. As we will see later, this is the case for the transformation given in [BH22]: It was designed with the goal to achieve committing security and while it does not initially achieve leakage resilience, we show that a minor tweak to it allows to achieve both.

Two areas that have gained a lot of attention are leakage resilience [BMOS17, DJS19, DEM+20, BPPS17, BGP+19, DM21, DM19, MOSW15, BGPS21] and committing security [BH22, CR22, MLGR23, KSW23, DMVA23], though they were never considered in conjunction. We focus on developing AE schemes that fulfill both properties. Firstly, having such schemes allows deployment in different scenarios even if each of it requires only one of the properties. Secondly, we think that this concrete combination of security notions has also practical relevance: Considering key-recovery attacks on embedded devices, both leakage-resilience and committing security are necessary properties. More precisely, consider an AE scheme that is either leakage-resilient or committing but not both. Using side-channel attacks, an adversary might be able to extract the secret key if the scheme is only committing secure. If the scheme is only leakage-resilient an adversary could apply a *Partitioning Oracle Attack* [LGR21] to learn the key: the adversary crafts ciphertexts that are valid for a subset of keys. If decryption succeeds, it knows that the target key is within this set and the attack continues using smaller and smaller subsets until it finds the key.

Towards the goal of developing schemes that fulfill both notions, we start by considering generic composition as a well-known method of constructing AE schemes. Here, an AE scheme is obtained by “gluing together” a symmetric encryption (SE) scheme and a message authentication code (MAC) such that security of the AE scheme follows from security of the two underlying components. There are three general methods: Encrypt-and-MAC (E&M), Encrypt-then-MAC (EtM), and MAC-then-Encrypt (MtE). A common misconception is that only EtM is secure and the other two approaches (E&M and MtE) are not. While initial work [BN00] indeed showed that only EtM is secure in general, later work [NRS14] provided a more fine-grained analysis. Here, associated data was taken into account as an input to the MAC and encryption schemes based on random IVs or nonces were considered. This led to the development of several secure AE schemes derived from the three classical composition methods: eight A-schemes that are composed of an IV-based encryption scheme and a vector-MAC; and three N-schemes which rely on nonce-based encryption for the underlying scheme and again a vector-MAC. Throughout this work, we will mainly focus on the latter schemes N1, N2, and N3, which follow the E&M, EtM, and

MtE approach, respectively. The three N-schemes have been analyzed both in the leakage setting [BMOS17] and against related-key attacks [FKOS22]. However, they have yet to be analyzed with respect to their committing security.

1.1 Contribution

We first study the committing security of generic composition.¹ We show that N2 (and EtM in general) does not achieve committing security. The fact that N2 authenticates the ciphertext together with the circumstance that colliding ciphertexts are easy to find—due to encryption schemes being reversible by design—enables a generic attack. For N1 (following E&M), we prove that committing security can be reduced to corresponding collision resistance properties of the underlying encryption and MAC.² We call these properties wCR and CR and show that they are achievable security notions by providing instances that fulfill them—namely, the symmetric encryption scheme and MAC underlying SLAE [DJS19]. To check this, we first note that SLAE follows the FGHF' construction and hence one can further break down the notions wCR and CR to the functions \mathcal{F} , \mathcal{G} , \mathcal{H} , and \mathcal{F}' . We then prove that the instantiations for these functions used in SLAE fulfill the desired properties. Our results for N3 (following MtE) are not that definite as the ones for N1 and N2: The main difficulty lies in the fact that the tag gets encrypted alongside the message, whereas for N1 and N2, the tag gets appended to the ciphertext—thus any committing attack against N1 and N2 requires identical tags whereas those against N3 do not. We give an heuristic analysis, narrowing down the possible attacks and discussing a number of common attack strategies. However, a complete analysis of MtE with respect to committing security is still an open task and left for future work. Nevertheless, we can conclude that committing and leakage-resilient AE cannot be built via generic composition, as the only leakage-resilient generic composition method is Encrypt-then-MAC [BMOS17], which we prove to be not secure with respect to committing security. As a second approach for building committing and leakage-resilient AE, we turn towards generic transformations as a way to achieve the desired security properties. We observe that none of the existing transformations from the literature are suitable for our purpose. The problem is that all of them hash the key, hence the leakage resilience of a scheme might be lost after its application if the hash function leaks information. To address this problem, we develop a generic transformation that turns an arbitrary AE scheme, a hash function, and a keyed function into an AE scheme that is both leakage-resilient and committing. At the core of the transformation is the keyed function which needs to be both pseudorandom under leakage and binding. We show existence of such a function by proving that the sponge-based function used in SLAE fulfills the binding property—pseudorandomness under leakage was already proven in [DJS19]. For the underlying AE scheme and hash function we rely on default AE security and collision-resistance.

In total, our consideration of committing security and leakage resilience of AE schemes in conjunction, yields both negative and positive results. On the negative side, our results indicate that committing security and leakage resilience do not work well together for generic composition. On the positive side, we develop a simple generic transformation that achieves both security notions, thereby meeting our goal of building committing and leakage-resilient AE.

¹We focus on the N-schemes, though it is easy to see that the results also apply to the A-schemes: In case of committing security, the difference between unique nonces and random IVs becomes obsolete as the adversary can choose them at will.

²In order to get a non-trivial bound for the symmetric encryption scheme, the message length needs to be of sufficient length (e.g., 128 bits). In light of real-world committing attacks, like the *Facebook message franking attack* [DGRW18], this is a reasonable assumption.

1.2 Related Work

Generic composition was initially introduced in [BN00] as a method to construct AE schemes and refined in [NRS14]. It is, especially from a theoretical point of view, an important method and was studied in various settings [FKOS22, BPP18, Ber23, BMOS17, KSW20].

The necessity of committing security for AE schemes is due to real-world attacks that exploit the lack thereof [DGRW18, LGR21, ADG⁺22]. The first committing security notions for AE schemes were formalized in [BH22]. Later works [CR22, MLGR23] provided a more fine-grained framework for committing security notions. Several works show committing attacks against various AE schemes: GCM/AES-GCM-SIV [BH22], GCM/OCB [CR22], CCM/EAX/SIV [MLGR23], AEZ [CFG⁺23], and the NIST LWC finalists [KSW23]. However, there are also positive results: CAU [BH22], CTX [CR22], the sponge-based NIST LWC finalists ASCON, ISAP, and SCHWAEMM [KSW23], SPONGEWRAPE [DFG23], and a sponge-based AE scheme based on SHAKE [DMVA23] were proven to be committing.

Leakage-resilient cryptography was formalized in [DP08], following the “Only Computation Leaks Information” paradigm [MR04]. Security notions for authenticated encryption incorporating leakage were developed in [BMOS17], which also analyzed the leakage resilience of generic composition, showing inherent weaknesses for Encrypt-and-MAC and MAC-then-Encrypt. Several works developed AE schemes that are designed to be leakage-resilient: ISAP [DEM⁺17, DEM⁺20], SLAE/FGHF’ [DJS19, KSW20], TEDT [BGP⁺19], ROMULUS-T [IKM⁺21], and SIVAT [BMOS17]. Furthermore, there are results concerning the leakage resilience of existing AE modes: PYJAMASK, PHOTON-BEETLE, ASCON, SPOOK, ISAP, and TEDT, are analyzed in [BBC⁺20], which shows different results regarding what parts need to be protected against leakage. Similarly, [VCS22] shows that out of the NIST LWC finalists, three modes (ASCON, ISAP, and ROMULUS-T) are advantageous when hardening their implementations against leakage. Lastly, [GPPS20] is worth highlighting, which provides a methodology that allows to analyze the leakage resilience of duplex sponges, e.g., ISAP, ASCON, GIBBON, and TEDTSPONGE—two of which were also shown to be committing.

Overall, there are many results with respect to either notion—for ASCON/ISAP even for both³ individually—we are not aware of any work explicitly targeting both of them.

2 Preliminaries

Notation. By $\{0, 1\}^*$, we denote the set of bit strings with arbitrary length. The empty bit string is written as ε . For a bit string X and an integer y , $[X]_y$ (resp. $[X]_{-y}$) denote the leftmost (resp. rightmost) y bits of X . Concatenation of bit strings X and Y is written as $X \parallel Y$. We use game-based proofs [BR06] and write $G(\mathcal{A}) \rightarrow x$, to denote that the output of game G , when played by \mathcal{A} , is x . By $\mathcal{A}^G \rightarrow x$, we denote that \mathcal{A} outputs x , when playing game G . Throughout this work, we write IV for some public, fixed initialization vector used in the constructions.

Primitives. The focus of this work is on authenticated encryption (AE) scheme with associated data, which is a pair of two algorithms (Enc, Dec) . The encryption algorithm $\text{Enc}: \mathcal{K} \times \mathcal{N} \times \mathcal{A} \times \mathcal{M} \rightarrow \mathcal{C}$ takes a key K , a nonce N , associated data A , and a message M as input, and outputs a ciphertext C . The decryption algorithm $\text{Dec}: \mathcal{K} \times \mathcal{N} \times \mathcal{A} \times \mathcal{C} \rightarrow \mathcal{M} \cup \{\perp\}$ takes a key K , a nonce N , associated data A , and a ciphertext C as input, and outputs a message M or a special symbol \perp . The key space, nonce space, associated data space, message space, and ciphertext space are denoted by the sets \mathcal{K} , \mathcal{N} , \mathcal{A} , \mathcal{M} , and \mathcal{C} , respectively. Throughout this work, we consider these sets to be bit strings of certain

³ROMULUS was also analyzed with respect to both leakage resilience and committing security [VCS22, KSW23], though for different variants (ROMULUS-N and ROMULUS-T).

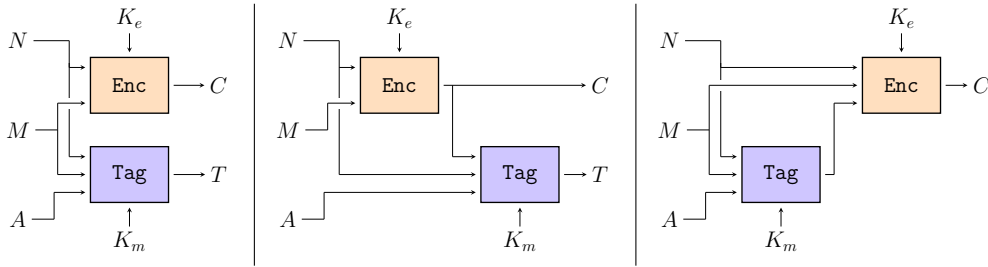


Figure 1: The AE schemes N1 (left), N2 (middle), and N3 (right) [NRS14] in terms of an underlying symmetric encryption scheme (Enc, Dec) and MAC (Tag, Ver).

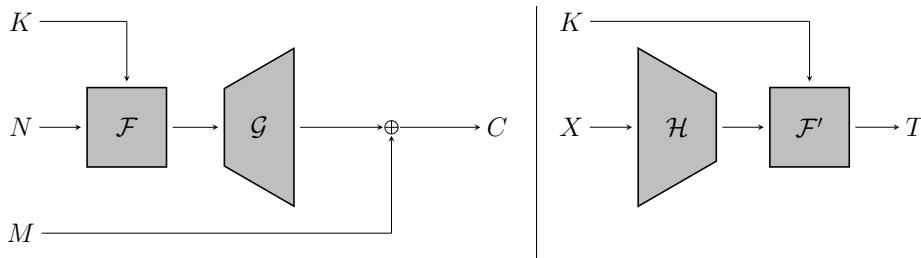


Figure 2: The symmetric encryption scheme $\text{SE}[\mathcal{F}, \mathcal{G}]$ (left), composed of a function \mathcal{F} and a pseudorandom generator \mathcal{G} , and the MAC $\text{MAC}[\mathcal{H}, \mathcal{F}']$ (right), composed of a hash function \mathcal{H} and a function \mathcal{F}' .

length, more precisely, $\mathcal{K} = \{0, 1\}^\kappa$, $\mathcal{N} = \{0, 1\}^\nu$, $\mathcal{A} = \{0, 1\}^*$, $\mathcal{M} = \{0, 1\}^*$, and $\mathcal{C} = \{0, 1\}^* \times \{0, 1\}^\tau$. We abuse notation and write either (C, T) or $C \parallel T$. The length of a message is denoted by m . *Correctness* of an AE scheme means that for any $(K, N, A, M) \in \mathcal{K} \times \mathcal{N} \times \mathcal{A} \times \mathcal{M}$, we have $\text{Dec}(K, N, A, \text{Enc}(K, N, A, M)) = M$. All schemes that we consider satisfy the *tidyness* property [NRS14]: it holds that $M = \text{Dec}(K, N, A, C)$ implies that $C = \text{Enc}(K, N, A, M)$. A symmetric encryption scheme is defined equivalently, except that there is no associated data and decryption does not return \perp . Following [MLGR23], the triple (K, N, A) is called a *context*.

A message authentication code (MAC) consists of two algorithms (Tag, Ver). The tagging algorithm $\text{Tag}: \mathcal{K} \times \mathcal{X} \rightarrow \{0, 1\}^\tau$ takes as input a key K and an element X . It returns a tag T of size $\{0, 1\}^\tau$. The verification algorithm $\text{Ver}: \mathcal{K} \times \mathcal{X} \times \{0, 1\}^\tau \rightarrow \{0, 1\}$ takes as input a key K , an element X , and a tag T and outputs 1 indicating that the input is valid, or otherwise 0. Throughout this work, we consider $\mathcal{K} = \{0, 1\}^\kappa$ and $\mathcal{X} = \{0, 1\}^*$. *Correctness* of a MAC means that for any $(K, X) \in \mathcal{K} \times \mathcal{X}$, it holds that $\text{Ver}(K, X, \text{Tag}(K, X)) = 1$.

The N-schemes [NRS14] construct an AE scheme from a symmetric encryption scheme and a MAC. Figure 1 illustrates the schemes N1, N2, and N3, while their pseudocodes are provided in Figure 15.

Sponges. Sponges are a tool to construct primitives. They rely on an n -bit state S that is constantly updated by applying a permutation $\pi: \{0, 1\}^n \rightarrow \{0, 1\}^n$ or a transformation $\rho: \{0, 1\}^n \rightarrow \{0, 1\}^n$ to it. A P-Sponge is centered around a permutation whereas a T-Sponge is centered around a transformation. In this work, we focus on the latter. In between two invocations of the permutation/transformation the sponge can *absorb* an input by XORing it to the first r bits of the state S or *squeeze* an output by outputting the first r bits of the state S . In the simplest setting—which is all we need in this work—the sponge will first absorb the whole input by constantly absorbing it r bits at a time and

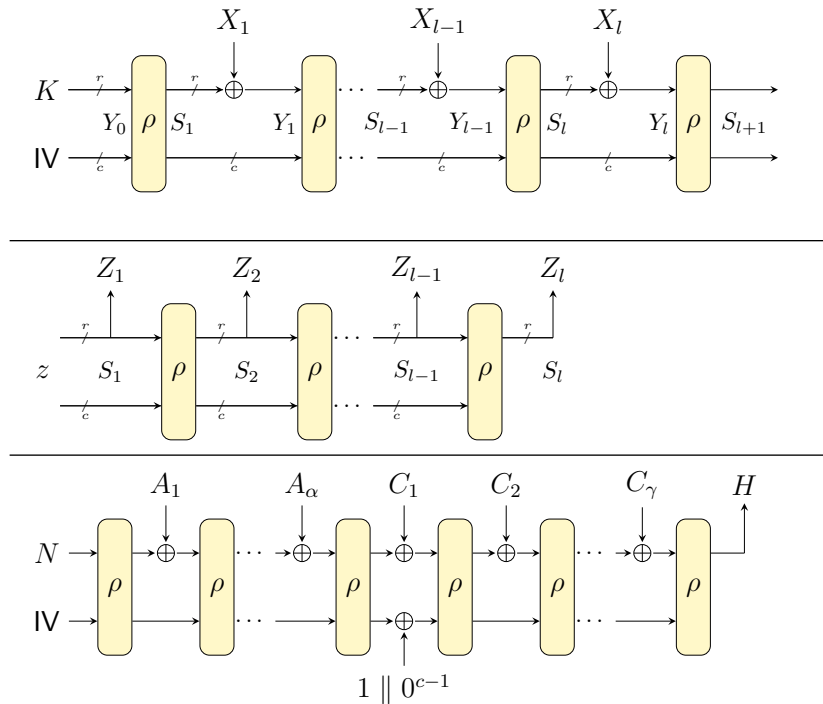


Figure 3: Illustration of the sponge-based primitives SLFUNC, SPRG, and SVHASH.

then squeeze the output r bits at a time. The capacity $c = n - r$ is the part of the state that is neither modified by the input during the absorption phase nor outputted in the squeezing phase. For the sponge-based proofs, the underlying transformation is assumed to be ideal, i.e., a random transformation to which the adversary gets oracle access.

In this work, we consider the sponge-based AE scheme SLAE [DJS19], more precisely, its underlying components. SLAE follows the generic construction FGHF' [DJS19,KS20], which constructs an AE scheme (via N2) from a symmetric encryption scheme $\text{SE}[\mathcal{F}, \mathcal{G}]$ and a MAC $\text{MAC}[\mathcal{H}, \mathcal{F}']$ (cf. Figure 2), which in turn are composed of functions \mathcal{F} and \mathcal{F}' , a PRG \mathcal{G} , and a hash function \mathcal{H} . The AE scheme SLAE is obtained by instantiating \mathcal{F}/\mathcal{F}' , \mathcal{G} , and \mathcal{H} with the sponge-based primitives SLFUNC, SPRG, and SVHASH, respectively. The primitives SLFUNC, SPRG, and SVHASH are illustrated in Figure 3, while their pseudocodes are given in Figure 17. The pseudocodes of the composed encryption scheme SLENC and the MAC SLMAC are provided in Figure 16.

3 Committing Security and Generic Composition

In this section, we analyze the committing security of the different generic composition paradigms. In Section 3.1, we analyze the three N-schemes N1, N2, and N3, given in [NRS14]. We continue with the generic encryption scheme $\text{SE}[\mathcal{F}, \mathcal{G}]$ and MAC $\text{MAC}[\mathcal{H}, \mathcal{F}']$ [DJS19,KS20] in Section 3.2, and its sponge-based instantiation in Section 3.3.

3.1 Committing Security of the N-Schemes

In this section, we analyze the committing security of N1, N2, and N3. We focus on the strongest form of committing security, which we define below. It asks the adversary to output two different contexts and messages that encrypt to the same ciphertext.

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Game CMT
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( $K, N, A, M$ ), ( $\bar{K}, \bar{N}, \bar{A}, \bar{M}$ )  $\leftarrow \mathcal{A}()$ 
if ( $K, N, A$ ) = ( $\bar{K}, \bar{N}, \bar{A}$ )
  return 0
( $C, T$ )  $\leftarrow \text{Enc}(K, N, A, M)$ 
( $\bar{C}, \bar{T}$ )  $\leftarrow \text{Enc}(\bar{K}, \bar{N}, \bar{A}, \bar{M})$ 
return (( $C, T$ ) = ( $\bar{C}, \bar{T}$ ))

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Figure 4: Security game CMT for authenticated encryption schemes.

Definition 1. Let $\text{AE} = (\text{Enc}, \text{Dec})$ be an authenticated encryption scheme and the game CMT be defined as in Figure 4. For any adversary \mathcal{A} , its CMT advantage is defined as

$$\text{Adv}_{\text{AE}}^{\text{CMT}}(\mathcal{A}) := \Pr[\text{CMT}(\mathcal{A}) \rightarrow 1].$$

3.1.1 N2 (Encrypt-then-MAC)

The following theorem shows that the N2 construction does not achieve any committing security. Due to the fact that the N2 construction authenticates the ciphertext—compared to the N1 and N3 construction which both authenticate the message—there is a generic attack exploiting the fact that colliding ciphertexts are easy to find for symmetric encryption schemes: We obtain two messages by decrypting an arbitrary ciphertext under different keys and the same nonce, and then authenticate said ciphertext, the nonce, and arbitrary associated data using some key for the MAC.

Theorem 1. *Let SE be a symmetric encryption scheme and MAC be a MAC. Let further $\text{N2}[\text{SE}, \text{MAC}]$ be the authenticated encryption scheme obtained via the N2 construction using SE and MAC. Then there exists an adversary \mathcal{A} such that*

$$\text{Adv}_{\text{N2}[\text{SE}, \text{MAC}]}^{\text{CMT}}(\mathcal{A}) = 1.$$

Proof. We construct a CMT adversary \mathcal{A} against $\text{N2}[\text{SE}, \text{MAC}]$ as shown in Figure 5. It picks an encryption key K_e , a MAC key K_m , a nonce N , associated data A , and a message M at random from the respective sets and computes the ciphertext $C \leftarrow \text{SE.Enc}(K_e, N, M)$. After sampling a different encryption key \bar{K}_e from $\mathcal{K} \setminus \{K_e\}$ at random, \mathcal{A} computes $\bar{M} \leftarrow \text{SE.Dec}(\bar{K}_e, N, C)$.⁴ Note that $\text{SE.Enc}(\bar{K}_e, N, \bar{M}) = C$ as we assume the symmetric encryption scheme to be tidy. Lastly the adversary sets $K \leftarrow (K_e, K_m)$ and $\bar{K} \leftarrow (\bar{K}_e, K_m)$, and outputs $(K, N, A, M), (\bar{K}, N, A, \bar{M})$. Then \mathcal{A} is successful as $K_e \neq \bar{K}_e$ implies $K \neq \bar{K}$ and

$$\begin{aligned}
& \text{N2}[\text{SE}, \text{MAC}].\text{Enc}(K, N, A, M) \\
&= \text{SE.Enc}(K_e, N, M) \parallel \text{MAC.Tag}(K_m, (N, A, \text{SE.Enc}(K_e, N, M))) \\
&= C \parallel \text{MAC.Tag}(K_m, (N, A, C)) \\
&= \text{SE.Enc}(\bar{K}_e, N, \bar{M}) \parallel \text{MAC.Tag}(K_m, (N, A, \text{SE.Enc}(\bar{K}_e, N, \bar{M}))) \\
&= \text{N2}[\text{SE}, \text{MAC}].\text{Enc}(\bar{K}, N, A, \bar{M}).
\end{aligned}$$

This finishes the proof. □

⁴Note that the messages M and \bar{M} might be identical which does not affect the attack as the encryption keys are guaranteed to be distinct.

Adversary \mathcal{A}

$K_e, N, M \leftarrow_s \mathcal{K} \times \mathcal{N} \times \mathcal{M}$
 $C \leftarrow \text{SE.Enc}(K_e, N, M)$
 $\bar{K}_e \leftarrow_s \mathcal{K} \setminus \{K_e\}$
 $\bar{M} \leftarrow \text{SE.Dec}(\bar{K}_e, N, C)$ // by tidyness: $C = \text{SE.Enc}(\bar{K}_e, N, \bar{M})$
 $(K_m, A) \leftarrow_s \mathcal{K} \times \mathcal{A}$
return $((K_e, K_m), N, A, M), ((\bar{K}_e, K_m), N, A, \bar{M})$

Figure 5: Our generic adversary breaking committing security for any instantiation of N2.

Game CR	Game wCR
$(K, X), (\bar{K}, \bar{X}) \leftarrow \mathcal{A}()$	$(K, N, M), (\bar{K}, \bar{N}, \bar{M}) \leftarrow \mathcal{A}()$
if $(K, X) = (\bar{K}, \bar{X})$	if $K = \bar{K} \vee (N, M) \neq (\bar{N}, \bar{M})$
return 0	return 0
$T \leftarrow \text{Tag}(K, X)$	$C \leftarrow \text{Enc}(K, N, M)$
$\bar{T} \leftarrow \text{Tag}(\bar{K}, \bar{X})$	$\bar{C} \leftarrow \text{Enc}(\bar{K}, \bar{N}, \bar{M})$
return $(T = \bar{T})$	return $(C = \bar{C})$

Figure 6: Security game CR for MACs and wCR for symmetric encryption schemes.

3.1.2 N1 (Encrypt-and-MAC)

We first define two new security notions which enable us to show committing security of N1: CR and wCR. The former requires the adversary to find a collision of a MAC, i.e., two tuples of keys and inputs that differ yet result in the same tag. The latter is similar but defined for symmetric encryption and of a more restrictive nature. Instead of asking the adversary to find any collision, it is required to find *distinct* keys and *identical* nonce-message pairs that result in the same ciphertext. While there are no tidy encryption schemes that satisfy unrestricted collision resistance—as our attack against N2 illustrates—it turns out that this restricted form is achievable as we will show later.

Definition 2. Let $\text{MAC} = (\text{Tag}, \text{Ver})$ be a message authentication code and the game CR be defined as in Figure 6. For any adversary \mathcal{A} , its CR advantage is defined as

$$\text{Adv}_{\text{MAC}}^{\text{CR}}(\mathcal{A}) := \Pr[\text{CR}(\mathcal{A}) \rightarrow 1].$$

Definition 3. Let $\text{SE} = (\text{Enc}, \text{Dec})$ be a symmetric encryption scheme and the game wCR be defined as in Figure 6. For any adversary \mathcal{A} , its wCR advantage is defined as

$$\text{Adv}_{\text{SE}}^{\text{wCR}}(\mathcal{A}) := \Pr[\text{wCR}(\mathcal{A}) \rightarrow 1].$$

Note that, while the tag length (in game CR) is fixed, the ciphertext length (in game wCR) is controlled by the adversary through the choice of the messages. Thus, for very short messages the game wCR can be won easily.

The theorem below shows that the N1 construction achieves the strongest form of committing security, i.e., CMT, given that the underlying encryption scheme and MAC achieve our new security notions wCR and CR.

Theorem 2. *Let SE be a symmetric encryption scheme and MAC be a MAC. Let further $\text{N1}[\text{SE}, \text{MAC}]$ be the authenticated encryption scheme obtained via the N1 construction using SE and MAC. Then for any adversary \mathcal{A} there exist adversaries \mathcal{B} and \mathcal{C} such that*

$$\text{Adv}_{\text{N1}[\text{SE}, \text{MAC}]}^{\text{CMT}}(\mathcal{A}) \leq \text{Adv}_{\text{SE}}^{\text{wCR}}(\mathcal{B}) + \text{Adv}_{\text{MAC}}^{\text{CR}}(\mathcal{C}).$$

Proof. Let \mathcal{A} be a CMT adversary against $\text{N1}[\text{SE}, \text{MAC}]$ and denote his output by $((K, N, A, M), (\overline{K}, \overline{N}, \overline{A}, \overline{M}))$, where $K = (K_e, K_m)$ with K_e and K_m being the encryption key and MAC key, respectively. The same for \overline{K} with encryption key \overline{K}_e and MAC key \overline{K}_m . Consider \mathbf{E} to be the event that $K_e \neq \overline{K}_e$ and $(N, M) = (\overline{N}, \overline{M})$. In the following, we abbreviate $\text{N1}[\text{SE}, \text{MAC}]$ with N1 as SE and MAC are clear from the context.

We construct a wCR adversary \mathcal{B} against SE . It runs $((K, N, A, M), (\overline{K}, \overline{N}, \overline{A}, \overline{M})) \leftarrow \mathcal{A}()$ and outputs $((K_e, N, M), (\overline{K}_e, \overline{N}, \overline{M}))$. If \mathcal{A} is successful, we obtain $(K, N, A, M) \neq (\overline{K}, \overline{N}, \overline{A}, \overline{M})$ and

$$\text{N1.Enc}(K, N, A, M) = \text{N1.Enc}(\overline{K}, \overline{N}, \overline{A}, \overline{M}). \quad (1)$$

By definition of the N1 construction, the encryption of the scheme N1 is given by

$$\text{N1.Enc}(K, N, A, M) = (\text{SE.Enc}(K_e, N, M), \text{MAC.Tag}(K_m, (N, A, M))). \quad (2)$$

Then we can conclude from Eq. (1) and Eq. (2) that

$$\text{SE.Enc}(K_e, N, M) = \text{SE.Enc}(\overline{K}_e, \overline{N}, \overline{M}).$$

Next assume that, additionally to \mathcal{A} being successful, event \mathbf{E} holds. Then adversary \mathcal{B} succeeds as $K_e \neq \overline{K}_e$ and $(N, M) = (\overline{N}, \overline{M})$, but their respective encryptions under SE agree. This yields

$$\Pr[\mathbf{E} \wedge \text{CMT}(\mathcal{A}) \rightarrow 1] \leq \Pr[\text{wCR}(\mathcal{B}) \rightarrow 1].$$

Next, we construct a CR adversary \mathcal{C} against MAC . It runs $((K, N, A, M), (\overline{K}, \overline{N}, \overline{A}, \overline{M})) \leftarrow \mathcal{A}()$ and outputs $((K_m, N, A, M), (\overline{K}_m, \overline{N}, \overline{A}, \overline{M}))$. If \mathcal{A} succeeds, we can conclude from Eq. (1) and Eq. (2) that

$$\text{MAC.Tag}(K_m, (N, A, M)) = \text{MAC.Tag}(\overline{K}_m, (\overline{N}, \overline{A}, \overline{M})).$$

Assume that additionally to \mathcal{A} being successful, event $\neg\mathbf{E}$ holds, that means either $K_e = \overline{K}_e$ or $(N, M) \neq (\overline{N}, \overline{M})$. If $(N, M) \neq (\overline{N}, \overline{M})$ holds, then $(K_m, N, A, M), (\overline{K}_m, \overline{N}, \overline{A}, \overline{M})$ are two different inputs for MAC . The same can be deduced if $K_e = \overline{K}_e$, as \mathcal{A} being successful implies that $(K, N, A, M) \neq (\overline{K}, \overline{N}, \overline{A}, \overline{M})$ and since the encryption keys agree, the difference must come from the inputs to MAC . Then adversary \mathcal{C} wins the game wCR as it outputs two different tuples that generate the same tag. Thus we obtain

$$\Pr[\neg\mathbf{E} \wedge \text{CMT}(\mathcal{A}) \rightarrow 1] \leq \mathbf{Adv}_{\text{MAC}}^{\text{CR}}(\mathcal{C}). \quad (3)$$

Combining these results we obtain

$$\begin{aligned} \mathbf{Adv}_{\text{N1}[\text{SE}, \text{MAC}]}^{\text{CMT}}(\mathcal{A}) &= \Pr[\text{CMT}(\mathcal{A}) \rightarrow 1] \\ &= \Pr[\mathbf{E} \wedge \text{CMT}(\mathcal{A}) \rightarrow 1] + \Pr[\neg\mathbf{E} \wedge \text{CMT}(\mathcal{A}) \rightarrow 1] \\ &\leq \Pr[\text{wCR}(\mathcal{B}) \rightarrow 1] + \Pr[\text{CR}(\mathcal{C}) \rightarrow 1] \\ &= \mathbf{Adv}_{\text{SE}}^{\text{wCR}}(\mathcal{B}) + \mathbf{Adv}_{\text{MAC}}^{\text{CR}}(\mathcal{C}). \end{aligned}$$

This concludes the proof. \square

3.1.3 N3 (MAC-then-Encrypt)

The core feature that differentiates N3 from the other two N -schemes is that the tag is no longer appended to the ciphertext, but instead is encrypted alongside the message. This means—at least in theory—that a valid committing attack against N3 can have $T \neq \overline{T}$ and $C = \overline{C}$ at the same time, which is impossible for both N1 and N2 . It turns out that this case is the problematic one for proving security of N3 .

We start by considering the case that the underlying encryption scheme and MAC fulfill the security properties wCR and CR security, respectively, which we defined for the

security proof of N1. While it is not clear that these security properties are fitting for N3 as well, they seem to be a good starting point—in order to prove classical security, coinciding assumptions are required for N1 and N3.

Under the assumption that the wCR and CR properties hold for SE and MAC, we can show that any CMT attack with $T = \bar{T}$ is ruled out, leaving only attacks for which $T \neq \bar{T}$ holds. This can be checked as follows: Assume for sake of contradiction that \mathcal{A} is an adversary that wins the game CMT and its outputs $((K_e, K_m), N, A, M)$ and $((\bar{K}_e, \bar{K}_m), \bar{N}, \bar{A}, \bar{M})$ fulfill $T = \bar{T}$. If $K_e = \bar{K}_e$ holds, at least one of the inputs to MAC must differ by definition of CMT. This contradicts the fact that MAC is CR-secure. If $K_e \neq \bar{K}_e$ and $(N, M) \neq (\bar{N}, \bar{M})$ holds, we also obtain a contradiction to MAC fulfilling CR security. Lastly, the case that $K_e \neq \bar{K}_e$ and $(N, M) = (\bar{N}, \bar{M})$ cannot occur either, as it would contradict the wCR security of SE.

We can further restrict the scope of possible attacks: As $T \neq \bar{T}$ must hold, SE has two different messages as input (namely $M \parallel T \neq \bar{M} \parallel \bar{T}$). By correctness, this implies that $(K_e, N) \neq (\bar{K}_e, \bar{N})$ must hold, as otherwise $\text{SE.Dec}(K_e, N, C)$ would have to equal both $M \parallel T$ and $\bar{M} \parallel \bar{T}$. This leaves us with attacks for which $T \neq \bar{T}$, i.e., $(K_m, N, A, M) \neq (\bar{K}_m, \bar{N}, \bar{A}, \bar{M})$ and $(K_e, N) \neq (\bar{K}_e, \bar{N})$, holds. While this is not enough to prove security of N3 in general, the restriction of possible attacks might aid security proofs for certain schemes. One example where this is the case, is N3[SENC, SLMAC], i.e., SLAE but built following N3 instead of N2: In Section 3.3, we will see that the scheme's underlying components fulfill wCR and CR, hence the above argument can be applied to N3[SENC, SLMAC]. This implies that any attack must contain different tags while yielding the same ciphertext. By construction of N3[SENC, SLMAC] the tag is computed as output of the function SLMAC, which is based on a random function. Therefore, it is highly unlikely that a pre-chosen tag can be hit by choosing the inputs fittingly. Furthermore, by construction of SENC, the key stream consists of several r -bit blocks generated by SPRG on input $\text{SLFUNC}(K_e, N)$. In particular, as the tag is inputted into SENC as the last message block, one needs to find $(K, N), (\bar{K}, \bar{N})$ such that the corresponding last r -bits blocks (R, \bar{R}) from the key stream satisfy $R \oplus T = \bar{R} \oplus \bar{T}$. However, both the computation of the key streams R, \bar{R} and the tags T, \bar{T} depend on the respective nonce and message. Thus after either the tag or the key stream is computed, the choices for the remaining one are heavily restricted and hence $R \oplus T = \bar{R} \oplus \bar{T}$ is unlikely to occur.

For the rest of this analysis we drop the assumptions wCR and CR and play through a number of general attack strategies.

1. A naive strategy in CMT attacks is to generate the target ciphertext C from randomly sampled (K, N, A, M) and then look for a second different input tuple $(\bar{K}, \bar{N}, \bar{A}, \bar{M})$ that encrypts to C as well. This approach is what [MLGR23] introduced as context discovery and several of the attacks against the NIST LWC finalists are of this form [KSW23]. Below, we show that context discovery attacks on the AE scheme boil down to similar attacks on the underlying encryption scheme and MAC.
 - (a) One possibility for an attack is to invert the ciphertext under \bar{K}_e and \bar{N} , which yields $\bar{M} \parallel \bar{T}$. This leaves the adversary with the task of finding \bar{K}_m and \bar{A} such that $\text{MAC}(\bar{K}_m, \bar{N}, \bar{A}, \bar{M}) = \bar{T}$. Following the context discovery notions defined for AE schemes [MLGR23], we refer to the above as a (K_m, A) -discovery attack. While there are MACs for which this is not possible (e.g. SLMAC), there are also ones that allow this attack (e.g., the MACs underlying ELEPHANT [BCDM21] and MINALPHER [STA⁺15] as well as the MAC CHASKEY [MMV⁺14]).
 - (b) Furthermore, one can try to reach the target ciphertext by first computing a second tag \bar{T} using $(\bar{K}_m, \bar{N}, \bar{A}, \bar{M})$. This leaves the task of finding \bar{K}_e such that $\text{SE.Enc}(\bar{K}_e, \bar{N}, \bar{M} \parallel \bar{T}) = C$. We call this a K_e -discovery attack. At first glance, this might look like a key recovery attack, where the adversary gets

message-ciphertext pairs. Note, however, that the adversary only needs to find a key that satisfies this property for one particular message-ciphertext pair. This differentiates it from a key recovery attack and leaves the possibility for secure scheme that allow for that—though we are not aware of such an example.

2. Another strategy is trying to produce a collision, i.e., instead of fixing a target ciphertext and trying to match it with the second tuple, one varies the inputs of SE simultaneously. As message, nonce, associated data, and MAC key already need to be chosen to compute the tag as input for the encryption scheme, the collision attack boils down to finding K_e and \bar{K}_e such that $\text{SE.Enc}(K_e, N, M \parallel T) = \text{SE.Enc}(\bar{K}_e, \bar{N}, \bar{M} \parallel \bar{T})$.

Overall, the results for N3 are of a heterogeneous nature: On the one hand, we identify a possible proof strategy for schemes with wCR and CR security, on the other hand we discuss a number of attacks. This indicates that—at least until further analysis is carried out—an individual treatment is necessary for each scheme. However, the above results might give a first indication to whether the scheme under consideration is committing.

3.2 Committing Security for Symmetric Encryption and MACs

Having established the positive results for N1, the question is whether there are any schemes that satisfy the required security notions wCR and CR. In this section we analyze the generic constructions $\text{SE}[\mathcal{F}, \mathcal{G}]$ and $\text{MAC}[\mathcal{H}, \mathcal{F}']$. We show that the wCR security of $\text{SE}[\mathcal{F}, \mathcal{G}]$ reduces to its underlying components \mathcal{F} and \mathcal{G} . Likewise, CR security of $\text{MAC}[\mathcal{H}, \mathcal{F}']$ reduces to \mathcal{H} and \mathcal{F}' . We first give the security notions required in this section, starting with the definition of collision resistance of a hash function and a PRG.

Definition 4. Let $\mathcal{H}: \{0, 1\}^* \rightarrow \{0, 1\}^w$ be a hash function with output length w . For any adversary \mathcal{A} , its CR advantage is defined as

$$\text{Adv}_{\mathcal{H}}^{\text{CR}}(\mathcal{A}) := \Pr[\mathcal{H}(X_1) = \mathcal{H}(X_2) \wedge X_1 \neq X_2 \mid (X_1, X_2) \leftarrow \mathcal{A}()].$$

Definition 5. Let $\mathcal{G}: \{0, 1\}^\sigma \rightarrow \{0, 1\}^*$ be a pseudorandom generator with associated seed space $\{0, 1\}^\sigma$. For any adversary \mathcal{A} , its CR advantage is defined as

$$\text{Adv}_{\mathcal{G}}^{\text{CR}}(\mathcal{A}) := \Pr[\mathcal{G}(z_1) = \mathcal{G}(z_2) \wedge z_1 \neq z_2 \mid (z_1, z_2) \leftarrow \mathcal{A}()].$$

Remark 1. An injective pseudorandom generator trivially is collision-resistant as no collision exists. Unlike hash functions, injectivity seems likely for PRGs as they map a short seed into a larger pseudorandom bit string. However, collision resistance is not implied by a secure PRG: take any secure PRG and hardcode two seeds $z_1 \neq z_2$ to a fixed output Z .

Next, we define the so-called binding security of a keyed function. More precisely, we give three variants of it: pbind, bind, and wbind. The first, pbind, is taken from [BH22]—note that they call this notion bind since they do not make the same distinction as we do—and requires the adversary to find two key-input pairs for which the outputs “partially” agree, i.e., on their first k bits. The second, bind, is the the same except that the whole outputs have to agree. The third, wbind, bears similarities with wCR: the adversary needs to find *distinct* key and *identical* inputs for which the outputs agree.

Definition 6. Let $F: \mathcal{K} \times \{0, 1\}^x \rightarrow \{0, 1\}^y$ be a function and the games pbind, bind, wbind be defined as in Figure 7. For any adversary \mathcal{A} , its pbind, bind, and wbind advantages are defined as

$$\text{Adv}_{F}^{\text{X}}(\mathcal{A}) := \Pr[\text{X}(\mathcal{A}) \rightarrow 1],$$

where $\text{X} \in \{\text{pbind}, \text{bind}, \text{wbind}\}$.

Game pbind	Game bind	Game wbind
$(K, X), (\overline{K}, \overline{X}) \leftarrow \mathcal{A}()$	$(K, X), (\overline{K}, \overline{X}) \leftarrow \mathcal{A}()$	$(K, X), (\overline{K}, \overline{X}) \leftarrow \mathcal{A}()$
if $(K, X) = (\overline{K}, \overline{X})$	if $(K, X) = (\overline{K}, \overline{X})$	if $K = \overline{K} \vee X \neq \overline{X}$
return 0	return 0	return 0
$Y \leftarrow F(K, X)$	$Y \leftarrow F(K, X)$	$Y \leftarrow F(K, X)$
$\overline{Y} \leftarrow F(\overline{K}, \overline{X})$	$\overline{Y} \leftarrow F(\overline{K}, \overline{X})$	$\overline{Y} \leftarrow F(\overline{K}, \overline{X})$
return $([Y]_k = [\overline{Y}]_k)$	return $(Y = \overline{Y})$	return $(Y = \overline{Y})$

Figure 7: Security games pbind, bind, and wbind.

These security notions can be ordered hierarchically with respect to their strength, namely $\text{Adv}_{\mathcal{F}}^{\text{wbind}}(\mathcal{C}) \leq \text{Adv}_{\mathcal{F}}^{\text{bind}}(\mathcal{D}) \leq \text{Adv}_{\mathcal{F}}^{\text{pbind}}(\mathcal{B})$. Details are given in Appendix B.6.

The theorem below shows that binding security of the encryption scheme $\text{SE}[\mathcal{F}, \mathcal{G}]$ reduces to binding security and collision resistance of \mathcal{F} and \mathcal{G} , respectively. The details are given in Appendix B.1.

Theorem 3. *Let $\mathcal{F}: \{0, 1\}^\kappa \times \{0, 1\}^\nu \rightarrow \{0, 1\}^\sigma$ be a function family and $\mathcal{G}: \{0, 1\}^\sigma \rightarrow \{0, 1\}^*$ be a pseudorandom generator. Then for any wCR adversary \mathcal{A} against $\text{SE}[\mathcal{F}, \mathcal{G}]$, there exists a wbind adversary \mathcal{B} against \mathcal{F} and a CR adversary \mathcal{C} against \mathcal{G} such that*

$$\text{Adv}_{\text{SE}[\mathcal{F}, \mathcal{G}]}^{\text{wCR}}(\mathcal{A}) \leq \text{Adv}_{\mathcal{F}}^{\text{wbind}}(\mathcal{B}) + \text{Adv}_{\mathcal{G}}^{\text{CR}}(\mathcal{C}).$$

The binding security of $\text{MAC}[\mathcal{H}, \mathcal{F}']$ follows from the collision resistance of \mathcal{H} and binding security of \mathcal{F}' . This is formalized in the following theorem, which is proven in Appendix B.2.

Theorem 4. *Let $\mathcal{H}: \{0, 1\}^* \rightarrow \{0, 1\}^w$ be a hash function and $\mathcal{F}': \{0, 1\}^\kappa \times \{0, 1\}^w \rightarrow \{0, 1\}^\tau$ be a function family. Then for any CR adversary \mathcal{A} against $\text{MAC}[\mathcal{H}, \mathcal{F}']$, there exists a CR adversary \mathcal{B} against \mathcal{H} and a bind adversary \mathcal{C} against \mathcal{F}' such that*

$$\text{Adv}_{\text{MAC}[\mathcal{H}, \mathcal{F}']}^{\text{CR}}(\mathcal{A}) \leq \text{Adv}_{\mathcal{H}}^{\text{CR}}(\mathcal{B}) + \text{Adv}_{\mathcal{F}'}^{\text{bind}}(\mathcal{C}).$$

The following composition theorem shows committing security of the N1 construction, when instantiating it with $\text{SE}[\mathcal{F}, \mathcal{G}]$ and $\text{MAC}[\mathcal{H}, \mathcal{F}']$ which in turn are instantiated with \mathcal{F} , \mathcal{G} , \mathcal{H} , and \mathcal{F}' . It follows by combining the previous results and is proven in Appendix B.3.

Theorem 5. *Let $\mathcal{F}: \{0, 1\}^\kappa \times \{0, 1\}^\nu \rightarrow \{0, 1\}^\sigma$, $\mathcal{F}': \{0, 1\}^\kappa \times \{0, 1\}^w \rightarrow \{0, 1\}^\tau$ be function families, $\mathcal{G}: \{0, 1\}^\sigma \rightarrow \{0, 1\}^*$ be a pseudorandom generator, and $\mathcal{H}: \{0, 1\}^* \rightarrow \{0, 1\}^w$ be a hash function. Then for any CMT adversary \mathcal{A} against $\text{N1}[\text{SE}[\mathcal{F}, \mathcal{G}], \text{MAC}[\mathcal{H}, \mathcal{F}']]$, there exists a wbind adversary \mathcal{B} against \mathcal{F} , a CR adversary \mathcal{C} against \mathcal{G} , a CR adversary \mathcal{D} against \mathcal{H} and a bind adversary \mathcal{E} against \mathcal{F}' such that*

$$\text{Adv}_{\text{N1}[\text{SE}[\mathcal{F}, \mathcal{G}], \text{MAC}[\mathcal{H}, \mathcal{F}']]}^{\text{CMT}}(\mathcal{A}) \leq \text{Adv}_{\mathcal{F}}^{\text{wbind}}(\mathcal{B}) + \text{Adv}_{\mathcal{G}}^{\text{CR}}(\mathcal{C}) + \text{Adv}_{\mathcal{H}}^{\text{CR}}(\mathcal{D}) + \text{Adv}_{\mathcal{F}'}^{\text{bind}}(\mathcal{E}).$$

3.3 An Instantiation from Sponges

Having established Theorem 5, we now give concrete bounds for the sponge-based instantiations of \mathcal{F} , \mathcal{G} , \mathcal{H} , and \mathcal{F}' . Recall that n is the size of the sponge state while c is its capacity.

The theorem below bounds the pbind, bind, and wbind advantages of the sponge-based function SLFUNC. Its proof can be found in Appendix B.4.

Theorem 6. *Let SLFUNC be the sponge-based function as displayed in Figure 3. Then for any adversary \mathcal{A} making q queries to ρ , it holds that*

$$\mathbf{Adv}_{\text{SLFUNC}}^{\text{pbind}}(\mathcal{A}) \leq \frac{q^2 - q}{2^{c+1}} + \frac{q^2 - q}{2^{k+1}} \quad \text{and} \quad \mathbf{Adv}_{\text{SLFUNC}}^{\text{wbind}}(\mathcal{A}) \leq \frac{q^2 - q}{2^{n+1}}.$$

In particular, for $k = n$ we have

$$\mathbf{Adv}_{\text{SLFUNC}}^{\text{bind}}(\mathcal{A}) \leq \frac{q^2 - q}{2^{c+1}} + \frac{q^2 - q}{2^{n+1}}.$$

Next, we give a bound on the collision-resistance of SPRG, the proof is given in Appendix B.5.

Theorem 7. *Let SPRG: $\{0, 1\}^n \rightarrow \{0, 1\}^m$ be the sponge-based pseudorandom generator as displayed in Figure 3. Then for any adversary \mathcal{A} making q queries to ρ , it holds that*

$$\mathbf{Adv}_{\text{SPRG}}^{\text{CR}}(\mathcal{A}) \leq \frac{q^2 - q}{2^{m+1}}.$$

Collision resistance of the sponge-based hash function SVHASH has been shown in [DJS19]. We recall this result below.

Theorem 8 ([DJS19]). *Let SVHASH be the hash function as displayed in Figure 3 with output length w . Then for any adversary \mathcal{A} making q queries to ρ , it holds that*

$$\mathbf{Adv}_{\text{SVHASH}}^{\text{CR}}(\mathcal{A}) \leq \frac{q(q-1)}{2^{w+1}} + \frac{q(q+2)}{2^{c-1}}.$$

Using Theorem 5 together with Theorem 6, Theorem 7, and Theorem 8, we obtain the committing security of N1[SLENC, SLMAC].

Theorem 9. *Let SLFUNC, SPRG, and SVHASH be the function family, PRG, and hash function described in Figure 3, respectively. Let further N1[SLENC, SLMAC] be the AE scheme constructed via N1 construction from SLENC and SLMAC, which in turn are constructed from SLFUNC, SPRG, and SVHASH as described in Figure 16. Then for any CMT adversary \mathcal{A} against AE, making q queries to ρ , it holds that*

$$\mathbf{Adv}_{\text{N1[SLENC, SLMAC]}}^{\text{CMT}}(\mathcal{A}) \leq \frac{q^2 - q}{2^n} + \frac{q^2 - q}{2^{m+1}} + \frac{q^2 - q}{2^{w+1}} + \frac{q^2 + 2q}{2^{c-1}} + \frac{q^2 - q}{2^{c+1}}.$$

Remark 2. Note that, in order to obtain a reasonable bound, the length of the messages outputted by \mathcal{A} should satisfy $m \geq \min\{w, c\}$. Otherwise, $\frac{q^2 - q}{2^{m+1}}$ becomes the dominant term, which can be trivial for very small m . However, this is a non-restrictive requirement, as real-world committing attacks [DGRW18] usually have this property.

4 Committing Security and Leakage Resilience

In this section, we develop a generic transformation that turns an arbitrary AE scheme into an AE scheme that is both leakage-resilient and committing. We start with the required background on leakage-resilient security notions in Section 4.1 followed by the transformation in Section 4.2.

Game LAE	oracle $\text{Enc}(N, A, M)$	oracle $\text{Dec}(N, A, C)$								
$b \leftarrow_{\$} \{0, 1\}$	$C \leftarrow \text{Enc}(K, N, A, M)$	if $b = 0$								
$K \leftarrow_{\$} \mathcal{K}$	if $b = 0$	return \perp								
$b' \leftarrow \mathcal{A}^{\text{Enc,LEnc,Dec,LDec}}()$	return $\bar{C} \leftarrow_{\$} \{0, 1\}^{ C }$	$M \leftarrow \text{Dec}(K, N, A, C)$								
return $(b' = b)$	return C	return M								
<table style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 33%; border-bottom: 1px solid black; padding: 5px;">oracle $\text{LEnc}(N, A, M, L)$</td> <td style="width: 33%; border-bottom: 1px solid black; padding: 5px;">oracle $\text{LDec}(N, A, C, L)$</td> </tr> <tr> <td style="padding: 5px;">$A \leftarrow L(K, N, A, M)$</td> <td style="padding: 5px;">$A \leftarrow L(K, N, A, C)$</td> </tr> <tr> <td style="padding: 5px;">$C \leftarrow \text{Enc}(K, N, A, M)$</td> <td style="padding: 5px;">$M \leftarrow \text{Dec}(K, N, A, C)$</td> </tr> <tr> <td style="padding: 5px;">return (C, A)</td> <td style="padding: 5px;">return (M, A)</td> </tr> </table>			oracle $\text{LEnc}(N, A, M, L)$	oracle $\text{LDec}(N, A, C, L)$	$A \leftarrow L(K, N, A, M)$	$A \leftarrow L(K, N, A, C)$	$C \leftarrow \text{Enc}(K, N, A, M)$	$M \leftarrow \text{Dec}(K, N, A, C)$	return (C, A)	return (M, A)
oracle $\text{LEnc}(N, A, M, L)$	oracle $\text{LDec}(N, A, C, L)$									
$A \leftarrow L(K, N, A, M)$	$A \leftarrow L(K, N, A, C)$									
$C \leftarrow \text{Enc}(K, N, A, M)$	$M \leftarrow \text{Dec}(K, N, A, C)$									
return (C, A)	return (M, A)									

Figure 8: Security game LAE.

4.1 Leakage Security Notions

For the leakage model, we use [BMOS17] which is based on [DP08], following the “Only Computation Leaks Information” assumption [MR04]. In this model, the adversary obtains challenge oracles that do not leak—representing the goal of the adversary—and leakage oracles that do leak—representing the power of the adversary to obtain side-channel leakage. For the leakage oracles, the adversary can choose a leakage function from some predetermined set of leakage functions. Alongside the output of the functionality that the leakage oracle represents, the adversary receives the evaluation of the leakage function. In case the scheme is composed of different components, the leakage of the composed scheme is the composition of the leakage from the individual components, i.e., for a primitive C composed of A and B , the leakage set of C is $\mathcal{L}_C = \mathcal{L}_A \times \mathcal{L}_B$ for \mathcal{L}_A and \mathcal{L}_B the leakage sets of A and B , respectively. An assumption that we are making is that comparison of values is leak-free, for instance, when a given tag is compared with the correct, recomputed tag. This assumption is made for SLAE and its generic construction FGHF' [DJS19, KS20]. Methods to achieve this are presented in [DM21].

Our target is LAE security as defined in [BMOS17]. In the notion, the adversary gets four oracles: Two challenge oracles which either implement the real encryption and decryption or their idealized counterparts, i.e., outputting random ciphertext (for the encryption oracle) and rejecting any query (for the decryption oracle). In addition, the adversary gets two leakage oracles, one for encryption and one for decryption, which always implement the real algorithm. The leakage oracle takes a leakage function as additional input whose output models the side-channel leakage that the adversary receives. Classical security for AE schemes is obtained by discarding the leakage oracles for the adversary. The security notion is formalized below.

Definition 7 (LAE Security). Let $\text{AE} = (\text{Enc}, \text{Dec})$ be an authenticated encryption scheme with associated data and the game LAE be as defined in Figure 8. For any nonce-respecting adversary \mathcal{A} that never forwards or repeats queries to or from the oracles Enc and Dec and only makes encryption and decryption queries containing leakage functions in the set \mathcal{L}_{AE} , describing the leakage sets for authenticated encryption, its corresponding LAE advantage is given by

$$\mathbf{Adv}_{\text{AE}}^{\text{LAE}}(\mathcal{A}, \mathcal{L}_{\text{AE}}) := |\Pr[\mathcal{A}^{\text{LAE}} \Rightarrow 1 \mid b = 1] - \Pr[\mathcal{A}^{\text{LAE}} \Rightarrow 1 \mid b = 0]|.$$

In addition to LAE security, we need LPRF security which corresponds to the standard PRF security enhanced with leakage: The adversary gets a challenge oracle, which implements either the real function or a random function. On top of that, the adversary gets a leakage oracle, which always implements the real function that also returns leakage,

based on the leakage function queried by the adversary. The definition of LPRF security is given below.

Definition 8 (LPRF Security). Let $F: \mathcal{K} \times \mathcal{X} \rightarrow \mathcal{Y}$ be a function family indexed by \mathcal{K} over the domain \mathcal{X} and let the game LPRF be as defined in Figure 9. For any adversary \mathcal{A} that never forwards or repeats queries to or from the oracle F and only queries leakage functions in the set \mathcal{L}_F , describing the leakage set for the function, its corresponding LPRF advantage is given by

$$\text{Adv}_{\mathbb{F}}^{\text{LPRF}}(\mathcal{A}, \mathcal{L}_F) := |\Pr[\mathcal{A}^{\text{LPRF}} \Rightarrow 1 \mid b = 1] - \Pr[\mathcal{A}^{\text{LPRF}} \Rightarrow 1 \mid b = 0]|.$$

Game LPRF	oracle $F(X)$	oracle $LF(X, L)$
$b \leftarrow_{\$} \{0, 1\}$	if $b = 0$	$A \leftarrow L(K, X)$
$K \leftarrow_{\$} \mathcal{K}$	return $Y \leftarrow_{\$} \mathcal{Y}$	$Y \leftarrow F(K, X)$
$b' \leftarrow \mathcal{A}^{F, LF}()$	else	return (Y, A)
return $(b' = b)$	return $F(K, X)$	

Figure 9: Security game LPRF.

4.2 A Generic Transformation

Our results so far show that one can construct committing authenticated encryption via generic composition, more precisely by following the Encrypt-and-MAC paradigm. However, our analysis also revealed that the Encrypt-then-MAC approach can never yield committing authenticated encryption. This presents a stark contrast to the results that are known in the realm of leakage-resilient AE schemes via generic composition: Barwell et al. [BMOS17] showed that only the Encrypt-then-MAC paradigm yields leakage-resilient AE schemes whereas the other two approaches suffer from inherent weaknesses. The key problem is that in both Encrypt-and-MAC and MAC-then-Encrypt, adversaries can obtain decryption leakage even for invalid ciphertexts, as the ciphertext needs to be decrypted in order to be validated. In contrast, Encrypt-then-MAC schemes can validate the ciphertext *before* decrypting it, thereby guaranteeing that decryption can leak only for valid ciphertexts.

In total, our results on the committing security of the generic composition methods combined with the existing ones on their leakage-resilience, expose that we cannot build AE schemes with both properties from generic composition. On our quest for committing and leakage-resilient AE schemes, we hence turn towards transformations that achieve the security notions.

To the best of our knowledge, there are two transformations that achieve CMT security: the combination of UtC and HtE from [BH22] and the CTX construction from [CR22]. Other transformations PaddingZeros, KeyHashing, and CAU-C1 [BH22] only achieve weaker forms of committing security.

Both constructions are shown to achieve CMT security while maintaining the security of the underlying AE scheme.⁵ Here, however, security is to be understood only with respect to classical AE security. Thus, when applying the transformation to any AE scheme that achieves LAE security, it is unclear whether the resulting scheme still achieves LAE security. Note that both transformations feed the key K as input into a hash function H . If the hash function is not leakage-resilient, the adversary might be able to learn the key which would render the scheme insecure. In particular, we are not aware of any

⁵Note that [BH22] also provides a transformation RtC that maintains nonce-misuse resistance.

$\text{UTC}^*[\text{H}, \text{F}, \text{AE}].\text{Enc}(K, N, A, M)$	$\text{UTC}^*[\text{H}, \text{F}, \text{AE}].\text{Dec}(K, N, A, (P^*, C, T))$
$X \leftarrow \text{H}(N, A)$	$X \leftarrow \text{H}(N, A)$
$(P, K') \leftarrow \text{F}(K, X)$	$(P, K') \leftarrow \text{F}(K, X)$
$(C, T) \leftarrow \text{Enc}(K', N, A, M)$	if $P^* \neq P$
return (P, C, T)	return \perp
	return $\text{Dec}(K', N, A, (C, T))$

Figure 10: Our modified transform UTC^* .

leakage-resilient hash function. While sponge constructions can achieve leakage resilience by reducing the rate to a minimum [DEM⁺17, DEM⁺20, DJS19], for hash functions such a change seems impractical.

This raises the question whether there are other transformations without this drawback. In the following we answer this question in the affirmative: We give a modified version of the transformation from [BH22] which transforms an arbitrary AE scheme (even without any leakage resilience) into an AE scheme that is both leakage-resilient and achieves CMT security. The transformation is shown in Figure 10. It is as simple as the one in [BH22] and imposes the same ciphertext expansion. First, the nonce N and the associated data A are hashed together. The resulting hash value is fed into a keyed function F that uses the key K and outputs a commitment P and a session key K' . Finally, the message is encrypted using K' and the resulting ciphertext is outputted together with the commitment P .

In the theorem below, we show that: (1) if H is a collision-resistant hash function and F is a partially binding function, then the AE scheme $\text{UTC}^*[\text{H}, \text{F}, \text{AE}]$, resulting from the transformation, achieves CMT security and (2) if H is a collision-resistant hash function, F is a leakage-resilient pseudorandom function, and AE is a secure AE scheme, then the AE scheme $\text{UTC}^*[\text{H}, \text{F}, \text{AE}]$ achieves LAE security. At the core lies the underlying function F , which needs to achieve both pbind and LPRF security—for the other components, we require only standard security properties.

Theorem 10. *Let AE be an authenticated encryption scheme, $\text{F}: \mathcal{K} \times \{0, 1\}^x \rightarrow \{0, 1\}^k \times \mathcal{K}$ be a function, and $\text{H}: \{0, 1\}^* \rightarrow \{0, 1\}^x$ be a hash function with associated leakage sets \mathcal{L}_{AE} , \mathcal{L}_{F} , and \mathcal{L}_{H} , respectively. Let further $\text{UTC}^*[\text{H}, \text{F}, \text{AE}]$ be the authenticated encryption scheme resulting from H , F , and AE via the modified UtC transformation (cf. Figure 10) with associated leakage set $\mathcal{L} = \mathcal{L}_{\text{H}} \times \mathcal{L}_{\text{F}} \times \mathcal{L}_{\text{AE}}$. Then for any adversary \mathcal{A}_0 there exist adversaries \mathcal{B}_0 and \mathcal{C}_0 , such that*

$$\text{Adv}_{\text{UTC}^*[\text{H}, \text{F}, \text{AE}]}^{\text{CMT}}(\mathcal{A}_0) \leq \text{Adv}_{\text{F}}^{\text{pbind}}(\mathcal{B}_0) + \text{Adv}_{\text{H}}^{\text{CR}}(\mathcal{C}_0),$$

and for any nonce-respecting adversary \mathcal{A}_1 , making q queries to its challenge oracles, there exist adversaries \mathcal{B}_1 , \mathcal{C}_1 , and \mathcal{D} , such that

$$\text{Adv}_{\text{UTC}^*[\text{H}, \text{F}, \text{AE}]}^{\text{LAE}}(\mathcal{A}_1, \mathcal{L}) \leq \text{Adv}_{\text{F}}^{\text{LPRF}}(\mathcal{B}_1, \mathcal{L}_{\text{F}}) + 2\text{Adv}_{\text{H}}^{\text{CR}}(\mathcal{C}_1) + q\text{Adv}_{\text{AE}}^{\text{AE}}(\mathcal{D}).$$

Proof. We start by showing the first part of the statement. The proof uses the games G and $\overline{\text{G}}$ described in Figure 11. The former is game CMT instantiated with the scheme $\text{UTC}^*[\text{F}, \text{AE}, \text{H}]$ that is composed of the function F , the AE scheme AE , and the hash function H . The latter game is similar, except that the adversary loses if its outputs constitute a collision in the hash function H . By a game hopping argument, we have

$$\begin{aligned} \text{Adv}_{\text{UTC}^*[\text{H}, \text{F}, \text{AE}]}^{\text{CMT}}(\mathcal{A}_0) &= \Pr[\text{G}(\mathcal{A}_0) \rightarrow 1] \\ &\leq |\Pr[\text{G}(\mathcal{A}_0) \rightarrow 1] - \Pr[\overline{\text{G}}(\mathcal{A}_0) \rightarrow 1]| + \Pr[\overline{\text{G}}(\mathcal{A}_0) \rightarrow 1]. \end{aligned}$$

The games \mathbf{G} and $\boxed{\mathbf{G}}$ are identical until \mathbf{Bad} , i.e., a collision of \mathbf{H} , occurs. We construct \mathcal{C}_0 that runs \mathcal{A}_0 to obtain (K, N, A, M) , $(\overline{K}, \overline{N}, \overline{A}, \overline{M})$ and simply outputs (N, A) , $(\overline{N}, \overline{A})$. It then holds that

$$|\Pr[\mathbf{G}(\mathcal{A}_0) \rightarrow 1] - \Pr[\boxed{\mathbf{G}}(\mathcal{A}_0) \rightarrow 1]| \leq \Pr[\mathbf{Bad}] = \mathbf{Adv}_H^{\text{CR}}(\mathcal{C}_0).$$

Let \mathcal{A} be an adversary winning the game $\boxed{\mathbf{G}}$. This means that \mathcal{A} outputs $(K, N, A, M) \neq (\overline{K}, \overline{N}, \overline{A}, \overline{M})$, which fulfill

$$\begin{aligned} \text{UTC}^*[\mathbf{H}, \mathbf{F}, \mathbf{AE}].\text{Enc}(K, N, A, M) &= ([\mathbf{F}(K, \mathbf{H}(N, A))]_k, C) \\ &= ([\mathbf{F}(\overline{K}, \mathbf{H}(\overline{N}, \overline{A}))]_k, \overline{C}) \\ &= \text{UTC}^*[\mathbf{H}, \mathbf{F}, \mathbf{AE}].\text{Enc}(\overline{K}, \overline{N}, \overline{A}, \overline{M}). \end{aligned}$$

We construct adversary \mathcal{B}_0 which runs \mathcal{A}_0 and outputs $(K, \mathbf{H}(N, A))$ and $(\overline{K}, \mathbf{H}(\overline{N}, \overline{A}))$. Using the above, we get that \mathcal{B}_0 's output satisfies $[\mathbf{F}(K, \mathbf{H}(N, A))]_k = [\mathbf{F}(\overline{K}, \mathbf{H}(\overline{N}, \overline{A}))]_k$. It remains to argue that its output is valid, i.e., $\mathbf{F}(K, \mathbf{H}(N, A)) \neq \mathbf{F}(\overline{K}, \mathbf{H}(\overline{N}, \overline{A}))$. In case that \mathcal{A}_0 's output satisfies $K \neq \overline{K}$, this holds trivially. In the case that \mathcal{A}_0 's output satisfies $K = \overline{K}$ it must hold that $(N, A) \neq (\overline{N}, \overline{A})$ and $\mathbf{H}(N, A) \neq \mathbf{H}(\overline{N}, \overline{A})$, as otherwise \mathcal{A}_0 would not be an adversary winning the game $\boxed{\mathbf{G}}$. Thus, in both cases, we have that \mathcal{B}_0 's output is valid and conclude with

$$\Pr[\boxed{\mathbf{G}}(\mathcal{A}_0) \rightarrow 1] = \mathbf{Adv}_F^{\text{pbind}}(\mathcal{B}_0).$$

Collecting the above finishes the first part of the proof.

Next, we prove the second part of the statement. For this we consider a sequence of games \mathbf{G}_0 , $\boxed{\mathbf{G}_0}$, \mathbf{G}_1 , \mathbf{G}_2 , and \mathbf{G}_3 (see Figure 12). Game \mathbf{G}_0 (respectively \mathbf{G}_3) is the game LAE with secret bit fixed to 1 (respectively 0). $\boxed{\mathbf{G}_0}$ is similar to \mathbf{G}_0 , except that queries constituting a collision in the hash function are rejected. Game \mathbf{G}_1 equals $\boxed{\mathbf{G}_0}$, up to the fact that the step $(P, K') \leftarrow \mathbf{F}(K, \mathbf{H}(N, A))$ is replaced by $(P, K') \leftarrow \mathbf{F}_1(K, \mathbf{H}(N, A))$ for some random function \mathbf{F}_1 . In \mathbf{G}_2 this is further changed to $(P, K') \leftarrow \mathbf{F}_2(K, N, A)$ for some random function \mathbf{F}_2 . Throughout all games, the leakage oracles remain the same. The choice of \mathbf{G}_0 and \mathbf{G}_3 allows the following computation

$$\begin{aligned} \mathbf{Adv}_{\text{UTC}^*[\mathbf{H}, \mathbf{F}, \mathbf{AE}]}^{\text{LAE}}(\mathcal{A}_1) &= |\Pr[\mathcal{A}_1^{\text{LAE}} \Rightarrow 1 \mid b = 1] - \Pr[\mathcal{A}_1^{\text{LAE}} \Rightarrow 1 \mid b = 0]| \\ &= |\Pr[\mathcal{A}_1^{\mathbf{G}_0} \Rightarrow 1] - \Pr[\mathcal{A}_1^{\mathbf{G}_3} \Rightarrow 1]| \\ &\leq |\Pr[\mathcal{A}_1^{\mathbf{G}_0} \Rightarrow 1] - \Pr[\mathcal{A}_1^{\boxed{\mathbf{G}_0}} \Rightarrow 1]| + |\Pr[\mathcal{A}_1^{\boxed{\mathbf{G}_0}} \Rightarrow 1] - \Pr[\mathcal{A}_1^{\mathbf{G}_1} \Rightarrow 1]| \\ &\quad + |\Pr[\mathcal{A}_1^{\mathbf{G}_1} \Rightarrow 1] - \Pr[\mathcal{A}_1^{\mathbf{G}_2} \Rightarrow 1]| + |\Pr[\mathcal{A}_1^{\mathbf{G}_2} \Rightarrow 1] - \Pr[\mathcal{A}_1^{\mathbf{G}_3} \Rightarrow 1]|. \end{aligned}$$

Note that for all game hops in the rest of the proof, the leakage Λ_{AE} of the AE scheme AE and the leakage $\Lambda_{\mathbf{H}}$ of the hash function \mathbf{H} will be computed locally by the respective reduction. In the following, we consider this computations as implicitly given. Similarly, the computation of $\Lambda_{\mathbf{F}}$ will be conducted locally with the exception being the game hop from $\boxed{\mathbf{G}_0}$ to \mathbf{G}_1 , where the reduction uses its own leakage oracle from the game LPRF. We start by giving a bound for the first summand. The games \mathbf{G}_0 and $\boxed{\mathbf{G}_0}$ are identical until \mathbf{Bad} , i.e., a collision of \mathbf{H} , occurs. We construct \mathcal{C}_1 that outputs the tuples (N, A) , $(\overline{N}, \overline{A})$ with which \mathcal{A}_1 triggered \mathbf{Bad} . It then holds that

$$|\Pr[\mathcal{A}_1^{\mathbf{G}_0} \Rightarrow 1] - \Pr[\mathcal{A}_1^{\boxed{\mathbf{G}_0}} \Rightarrow 1]| \leq \Pr[\mathbf{Bad}] = \mathbf{Adv}_H^{\text{CR}}(\mathcal{C}_1).$$

To bound the second summand, we construct the following LPRF adversary \mathcal{B}_1 against \mathbf{F} : For queries (N, A, M) to Enc by \mathcal{A}_1 , the adversary \mathcal{B}_1 computes $\mathbf{H}(N, A)$ locally and then invokes its own challenge oracle \mathbf{F} on $\mathbf{H}(N, A)$ to obtain (P, K') . \mathcal{B}_1 then computes

$\text{AE.Enc}(K', N, A, M) = C$ locally and sends (P, C) back to \mathcal{A}_1 . Queries $(N, A, (P^*, C))$ to Dec are answered similarly: \mathcal{B}_1 computes $H(N, A)$ and invokes F on $H(N, A)$ to obtain (P, K') . If $P^* \neq P$, it returns \perp and otherwise $M \leftarrow \text{AE.Dec}(K', N, A, C)$ is computed and M sent to \mathcal{A}_1 .

For queries $(N, A, M, L = (L_H, L_F, L_{AE}))$ to the leakage oracle LEnc , \mathcal{B}_1 computes $H(N, A)$ locally. Then it invokes its own leakage oracle $\text{LF}(H(N, A), L_F)$ and obtains Λ_F and (P, K') . Lastly, the adversary \mathcal{B}_1 computes $C = \text{AE.Enc}(K', N, A, M)$ and sends (P, C) and $(\Lambda_H, \Lambda_F, \Lambda_{AE})$ back to \mathcal{A}_1 . Queries $(N, A, (P^*, C), L)$ to LDec are handled similarly: \mathcal{B}_1 follows the same steps to obtain $H(N, A)$, Λ_F , and (P, K') . If $P^* \neq P$ it returns \perp , otherwise it computes $M \leftarrow \text{AE.Dec}(K', N, A, C)$ and sends M and $(\Lambda_{AE}, \Lambda_H, \Lambda_F)$ back to \mathcal{A}_1 .

We have defined \mathcal{B}_1 such that it perfectly simulates $\boxed{\mathcal{G}_0}$ or \mathcal{G}_1 —depending on the value of the secret bit—for \mathcal{A}_1 . In particular, note that both games return \perp in case the adversary triggers a hash collision with its queries. This guarantees that \mathcal{B}_1 makes no forbidden queries, i.e., it never queries the same value to its challenge oracle twice.⁶ Therefore, we can conclude

$$\begin{aligned} |\Pr[\mathcal{A}_1^{\boxed{\mathcal{G}_0}} \Rightarrow 1] - \Pr[\mathcal{A}_1^{\mathcal{G}_1} \Rightarrow 1]| &= |\Pr[\mathcal{B}_1^{\text{LPRF}} \Rightarrow 1 \mid b = 1] - \Pr[\mathcal{B}_1^{\text{LPRF}} \Rightarrow 1 \mid b = 0]| \\ &= \mathbf{Adv}_F^{\text{LPRF}}(\mathcal{B}_1, \mathcal{L}_F). \end{aligned}$$

Next, we bound the game hop between \mathcal{G}_1 and \mathcal{G}_2 . Since in both \mathcal{G}_1 and \mathcal{G}_2 the pair (P, K') is sampled randomly, adversary \mathcal{A}_1 can not distinguish \mathcal{G}_1 and \mathcal{G}_2 except if there is a collision of the hash function. Then, the encryption oracle (or the decryption oracle, respectively) of \mathcal{G}_1 outputs \perp , whereas for \mathcal{G}_2 this is not the case. Then we can construct \mathcal{C}_1 that outputs the tuples $(N, A), (\bar{N}, \bar{A})$ with which \mathcal{A}_1 triggered Bad , i.e., a hash collision. Hence, we obtain

$$|\Pr[\mathcal{A}_1^{\mathcal{G}_1} \Rightarrow 1] - \Pr[\mathcal{A}_1^{\mathcal{G}_2} \Rightarrow 1]| \leq \Pr[\text{Bad}] = \mathbf{Adv}_H^{\text{CR}}(\mathcal{C}_1).$$

Lastly, we bound the game hop between \mathcal{G}_2 and \mathcal{G}_3 . Due to the fact that UTC^* uses different session keys—computed from the context—for the underlying AE scheme AE, we cannot simply reduce to the security of AE. To accommodate for that, we do a hybrid argument over the distinct session keys.⁷ For this, we define a sequence of hybrid games $\mathcal{H}_0, \dots, \mathcal{H}_q$, which are described in Figure 13. Here, q denotes the number of distinct (N, A) -pairs that \mathcal{A}_1 queries to either Enc or Dec. In \mathcal{H}_i , the first i distinct (N, A) -pairs are answered as in \mathcal{G}_3 , while the remaining queries are handled as in \mathcal{G}_2 . Observe that $\mathcal{H}_0 = \mathcal{G}_2$ and $\mathcal{H}_q = \mathcal{G}_3$, which yields

$$\begin{aligned} |\Pr[\mathcal{A}_1^{\mathcal{G}_1} \Rightarrow 1] - \Pr[\mathcal{A}_1^{\mathcal{G}_2} \Rightarrow 1]| &= |\Pr[\mathcal{A}_1^{\mathcal{H}_0} \Rightarrow 1] - \Pr[\mathcal{A}_1^{\mathcal{H}_q} \Rightarrow 1]| \\ &\leq \sum_{i=1}^q |\Pr[\mathcal{A}_1^{\mathcal{H}_{i-1}} \Rightarrow 1] - \Pr[\mathcal{A}_1^{\mathcal{H}_i} \Rightarrow 1]|. \end{aligned}$$

For each $i = 1, \dots, q$, we construct an AE adversary \mathcal{D}_i to bound the game hop between \mathcal{H}_{i-1} and \mathcal{H}_i . First, the adversary \mathcal{D}_i samples a key K to simulate the oracles LEnc , and LDec for \mathcal{A}_1 . If a pair of nonce and associated data is queried twice, special care is applied to ensure that the same session key is used. More precisely, after a pair of nonce and associated data (N, A) is queried for the first time, the computed key commitment P and session-key K' are stored and reused for further queries containing (N, A) .

For $(N_1, A_1), \dots, (N_q, A_q)$ the q distinct pairs of nonce and associated data, \mathcal{D}_i proceeds as follows: If the j -the query, for $j \leq i$, is a query to Enc, \mathcal{D}_i samples (P_j, C_j) randomly and

⁶Rather than repeating a query, \mathcal{B}_1 will simply return \perp to \mathcal{A}_1 .

⁷In [BH22], the same problem occurs, though they resolve this using multi-user security [BT16].

Games G and $\boxed{\mathsf{G}}$

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( $K, N, A, M$ ), ( $\bar{K}, \bar{N}, \bar{A}, \bar{M}$ )  $\leftarrow \mathcal{A}()$ 
if ( $K, N, A$ ) = ( $\bar{K}, \bar{N}, \bar{A}$ )
  return 0
if ( $N, A$ )  $\neq$  ( $\bar{N}, \bar{A}$ )  $\wedge$   $\mathsf{H}(N, A) = \mathsf{H}(\bar{N}, \bar{A})$ 
  Bad  $\leftarrow$  true
  return 0
( $P, C, T$ )  $\leftarrow$   $\mathsf{UTC}^*[\mathsf{H}, \mathsf{F}, \mathsf{AE}].\mathsf{Enc}(K, N, A, M)$ 
( $\bar{P}, \bar{C}, \bar{T}$ )  $\leftarrow$   $\mathsf{UTC}^*[\mathsf{H}, \mathsf{F}, \mathsf{AE}].\mathsf{Enc}(\bar{K}, \bar{N}, \bar{A}, \bar{M})$ 
return ( $(P, C, T) = (\bar{P}, \bar{C}, \bar{T})$ )

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Figure 11: Games G and $\boxed{\mathsf{G}}$ used in the proof of Theorem 10.

sends it to \mathcal{A}_1 . If it is a query to Dec , it returns \perp to \mathcal{A}_1 . If the i -th query is a query to Enc , i.e., of the form (N_i, A_i, M_i) , \mathcal{D}_i invokes its own encryption oracle on (N_i, A_i, M_i) to obtain C_i , which is sent to \mathcal{A}_1 together with a randomly sampled P_i . If it is a query to Dec , i.e., of the form $(N_i, A_i, (P_i^*, C))$, a random pair (P^*, K') is sampled. If $P_i^* \neq P_i$, \perp is returned, otherwise \mathcal{D}_i invokes its own decryption oracle on (K'_i, N_i, A_i, C_i) . If the j -th query, for $j \geq i$, is a query to Enc , (P_j, K'_j) is sampled randomly and $\mathsf{AE.Enc}(K'_j, N_j, A_j, M_j)$ is computed locally. Then (P_j, C_j) is returned to \mathcal{A}_1 . If it is a query to Dec , i.e., of the form $(N_i, A_i, (P_i^*, C))$, a random pair (P^*, K') is sampled. If $P_i^* \neq P_i$, \perp is returned, otherwise $\mathsf{AE.Dec}(K', N, A, C)$ is computed locally.

For each query $(N, A, M, L = (L_H, L_F, L_{\mathsf{AE}}))$ to LEnc , \mathcal{D}_i computes $X = \mathsf{H}(N, A)$, $(P, K') = \mathsf{F}(K, X)$, $L_F(K, X)$, and $C = \mathsf{AE.Enc}(K', N, A, M)$ locally. It sends (P, C) and $(L_H, L_F, L_{\mathsf{AE}})$ to \mathcal{A}_1 . Queries to LDec are handled analogously with C being used instead of M . Note, however, that $P^* = P$ needs to be checked as it was done for queries to Dec .

We observe that \mathcal{D}_i simulates H_{i-1} and H_i for the secret bit being 1 and 0, respectively. Note further that \mathcal{D}_i queries a nonce N to its encryption oracles (either challenge or leakage) if and only if \mathcal{A} queries N to its encryption oracles. Thus the nonce-respecting property of \mathcal{D}_i follows from \mathcal{A} being nonce-respecting. Furthermore, we observe that any encryption/decryption query by \mathcal{D}_i stems from a query by \mathcal{A} . If any of the queries by \mathcal{D}_i would be prohibited, we would immediately get that \mathcal{A} made queries that are forbidden. Thus, we can conclude

$$\begin{aligned} |\Pr[\mathcal{A}_1^{\mathsf{H}_{i-1}} \Rightarrow 1] - \Pr[\mathcal{A}_1^{\mathsf{H}_i} \Rightarrow 1]| &= |\Pr[\mathcal{D}_i^{\mathsf{AE}} \Rightarrow 1 \mid b = 1] - \Pr[\mathcal{D}_i^{\mathsf{AE}} \Rightarrow 1 \mid b = 0]| \\ &= \mathbf{Adv}_{\mathsf{AE}}^{\mathsf{AE}}(\mathcal{D}_i). \end{aligned}$$

We define \mathcal{D} to be the adversary that picks i from $\{1, \dots, q\}$ randomly and then acts like \mathcal{D}_i . By a standard hybrid argument, we get

$$|\Pr[\mathcal{A}_1^{\mathsf{G}_2} \Rightarrow 1] - \Pr[\mathcal{A}_1^{\mathsf{G}_3} \Rightarrow 1]| \leq \sum_{i=1}^q |\Pr[\mathcal{A}_1^{\mathsf{H}_{i-1}} \Rightarrow 1] - \Pr[\mathcal{A}_1^{\mathsf{H}_i} \Rightarrow 1]| \leq q \mathbf{Adv}_{\mathsf{AE}}^{\mathsf{AE}}(\mathcal{D}).$$

In total, we have shown

$$\mathbf{Adv}_{\mathsf{UTC}^*[\mathsf{F}, \mathsf{AE}, \mathsf{H}]}^{\mathsf{LAE}}(\mathcal{A}_1, \mathcal{L}_{\mathsf{AE}}) \leq \mathbf{Adv}_{\mathsf{F}}^{\mathsf{LPRF}}(\mathcal{B}_1, \mathcal{L}_{\mathsf{F}}) + 2\mathbf{Adv}_{\mathsf{H}}^{\mathsf{CR}}(\mathcal{C}_1) + q \mathbf{Adv}_{\mathsf{AE}}^{\mathsf{AE}}(\mathcal{D}).$$

This finishes the proof. \square

<p>Games G_0, G_1, G_2, G_3</p> <p>$b \leftarrow_s \{0, 1\}$</p> <p>$K \leftarrow_s \mathcal{K}$</p> <p>$S_1, S_2 \leftarrow \emptyset$</p> <p>$b' \leftarrow \mathcal{A}^{\text{Enc, Dec, LEnc, LDec}}()$</p> <p>return ($b' = b$)</p>	<p>oracle $\text{Enc}(N, A, M)$ in G_0</p> <hr/> <p>$X \leftarrow H(N, A)$</p> <p>if $X \in S_1 \wedge (N, A) \notin S_2$</p> <p style="padding-left: 20px;">Bad \leftarrow true</p> <p style="padding-left: 20px;">return \perp</p> <p>$S_1 \leftarrow S_1 \cup \{X\}$</p> <p>$S_2 \leftarrow S_2 \cup \{(N, A)\}$</p> <p>$(P, K') \leftarrow F(K, X)$</p> <p>$C \leftarrow \text{AE.Enc}(K', N, A, M)$</p> <p>return ($P, C$)</p> <p>oracle $\text{Enc}(N, A, M)$ in G_1</p> <hr/> <p>$X \leftarrow H(N, A)$</p> <p>if $X \in S_1 \wedge (N, A) \notin S_2$</p> <p style="padding-left: 20px;">Bad \leftarrow true</p> <p style="padding-left: 20px;">return \perp</p> <p>$S_1 \leftarrow S_1 \cup \{X\}$</p> <p>$S_2 \leftarrow S_2 \cup \{(N, A)\}$</p> <p>$(P, K') \leftarrow F_1(K, X)$</p> <p>$C \leftarrow \text{AE.Enc}(K', N, A, M)$</p> <p>return ($P, C$)</p> <p>oracle $\text{Enc}(N, A, M)$ in G_2</p> <hr/> <p>$(P, K') \leftarrow F_2(N, A)$</p> <p>$C \leftarrow \text{AE.Enc}(K', N, A, M)$</p> <p>return ($P, C$)</p> <p>oracle $\text{Enc}(N, A, M)$ in G_3</p> <hr/> <p>$(P, K') \leftarrow F_2(K, N, A)$</p> <p>$C \leftarrow F_3(K', N, A, M)$</p> <p>return ($P, C$)</p>	<p>oracle $\text{Dec}(N, A, (P^*, C))$ in G_0</p> <hr/> <p>$X \leftarrow H(N, A)$</p> <p>if $X \in S_1 \wedge (N, A) \notin S_2$</p> <p style="padding-left: 20px;">Bad \leftarrow true</p> <p style="padding-left: 20px;">return \perp</p> <p>$S_1 \leftarrow S_1 \cup \{X\}$</p> <p>$S_2 \leftarrow S_2 \cup \{(N, A)\}$</p> <p>$(P, K') \leftarrow F(K, X)$</p> <p>if $P^* \neq P$</p> <p style="padding-left: 20px;">return \perp</p> <p>return $\text{AE.Dec}(K', N, A, C)$</p> <p>oracle $\text{Dec}(N, A, (P^*, C))$ in G_1</p> <hr/> <p>$X \leftarrow H(N, A)$</p> <p>if $X \in S_1 \wedge (N, A) \notin S_2$</p> <p style="padding-left: 20px;">Bad \leftarrow true</p> <p style="padding-left: 20px;">return \perp</p> <p>$S_1 \leftarrow S_1 \cup \{X\}$</p> <p>$S_2 \leftarrow S_2 \cup \{(N, A)\}$</p> <p>$(P, K') \leftarrow F_1(K, X)$</p> <p>if $P^* \neq P$</p> <p style="padding-left: 20px;">return \perp</p> <p>return $\text{AE.Dec}(K', N, A, C)$</p> <p>oracle $\text{Dec}(N, A, (P^*, C))$ in G_2</p> <hr/> <p>$(P, K') \leftarrow F_2(K, N, A)$</p> <p>if $P^* \neq P$</p> <p style="padding-left: 20px;">return \perp</p> <p>return $\text{AE.Dec}(K', N, A, C)$</p> <p>oracle $\text{Dec}(N, A, (P^*, C))$ in G_3</p> <hr/> <p>return \perp</p>
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Figure 12: Games $G_0, G_1,$ and G_2 used in the proof of Theorem 10. The leakage oracles are shown in Figure 14.

Game H_i	oracle $\text{Enc}(N, A, M)$ in H_i	oracle $\text{Dec}(N, A, (P^*, C))$ in H_i
$c \leftarrow 0$	$S \leftarrow S \cup \{(N, A)\}$	$S \leftarrow S \cup \{(N, A)\}$
$b \leftarrow_s \{0, 1\}$	if $\#S \leq i$	if $\#S \leq i$
$K \leftarrow_s \mathcal{K}$	$(P, C) \leftarrow_s \{0, 1\}^* \times \{0, 1\}^m$	$M \leftarrow \perp$
$S \leftarrow \emptyset$	else	else
$b' \leftarrow \mathcal{A}^{\text{Enc, Dec, LEnc, LDec}}()$	if $p[N, A] = \perp$	if $p[N, A] = \perp$
return $(b' = b)$	$p[N, A] \leftarrow_s \{0, 1\}^\kappa$	$p[N, A] \leftarrow_s \{0, 1\}^\kappa$
	$(P, K') \leftarrow p[N, A]$	$(P, K') \leftarrow p[N, A]$
	$C \leftarrow \text{AE.Enc}(K', N, A, M)$	if $P^* \neq P$
	return (P, C)	$M \leftarrow \perp$
		$M \leftarrow \text{AE.Dec}(K', N, A, C)$
		return M

Figure 13: Hybrid games H_i used in the proof of Theorem 10. The leakage oracles are shown in Figure 14. By $p[\cdot, \cdot]$, we denote a table, with each entry initially set to \perp . Note that we do not use the table to generate (P, C) in the first if-branch of Enc but instead also sample a fresh tuple. This is no problem as our adversary is nonce-respecting, meaning that every query will result in a new entry of the table anyway.

oracle $\text{LEnc}(N, A, M, (L_H, L_F, L_{\text{AE}}))$	oracle $\text{LDec}(N, A, (P^*, C), (L_H, L_F, L_{\text{AE}}))$
$X \leftarrow H(N, A)$	$X \leftarrow H(N, A)$
$(P, K') \leftarrow F(K, X)$	$(P, K') \leftarrow F(K, X)$
$C \leftarrow \text{AE.Enc}(K', N, A, M)$	if $P^* \neq P$
$\Lambda_H \leftarrow L_H(N, A)$	return \perp
$\Lambda_F \leftarrow L_F(K, X)$	$M \leftarrow \text{AE.Dec}(K', N, A, C)$
$\Lambda_{\text{AE}} \leftarrow L_{\text{AE}}(K', N, A, M)$	$\Lambda_H \leftarrow L_H(N, A)$
return $(C, (\Lambda_H, \Lambda_F, \Lambda_{\text{AE}}))$	$\Lambda_F \leftarrow L_F(K, X)$
	$\Lambda_{\text{AE}} \leftarrow L_{\text{AE}}(K', N, A, C)$
	return $(M, (\Lambda_H, \Lambda_F, \Lambda_{\text{AE}}))$

Figure 14: The leakage oracles LEnc and LDec used in the proof of Theorem 10. These oracles are shared across all games G_0, \dots, G_3 and H_0, \dots, H_q .

5 Conclusion and Instantiation/Implementation Aspects

Our analysis reveals that the generic composition paradigms are not suitable for constructing AE schemes that are simultaneously committing and leakage-resilient. However, we identify another way to obtain such schemes by means of a generic transformation. The latter can be applied to any secure AE scheme, i.e., it does not require any committing or leakage resilience guarantees on the scheme to begin with. In particular, this allows to apply the UTC^* transformation to AE schemes built from generic composition without needing the underlying symmetric encryption scheme and MAC to fulfill binding or leakage resilience properties. While we just require standard AE security for the scheme that is to be transformed, the transformation uses a function F that needs to be partially binding and an LPRF. A possible instantiation for this is the sponge-based function SLFUNC (cf. Figure 3) which was shown to be an LPRF in [DJS19] and binding in Theorem 6. Note that, in order to obtain a good bound on the LPRF security, the rate r needs to be very small and is typically set to 1. Further, for any practical instantiation, one needs to choose a concrete non-invertible permutation for ρ . Following [DJS19], a candidate can be obtained using KECCAK-P : define $\rho(x) = \text{KECCAK-P}(x) \oplus x$, where the additional XOR ensures non-invertibility. An alternative candidate is the tagging algorithm of the leakage-resilient MAC given in [BMOS17]⁸ which is an LPRF but has yet to be analyzed with respect to its binding security. Bellare and Hoang [BH22] provide a construction of a binding function which they call “Counter-then-XOR” (CTX). The CTX construction, which relies on a block-cipher, is also an alternative but not yet analyzed in the leakage setting.

Coming back to SLAE, which was used as an example throughout this work, we can now provide a committing and leakage-resilient variant: This is achieved by applying the UTC^* transformation, using SVHASH and SLFUNC , to SLAE, where $\rho(x) = \text{KECCAK-P}(x) \oplus x$ as described above. While SLAE is leakage-resilient to start with, due to a very small rate in the underlying function SLFUNC , this is not a necessary prerequisite for applying the UTC^* transformation. Thus, it is even possible to use SLAE with a bigger rate in SLFUNC as input to UTC^* , while the SLFUNC instance used in the transformation deploys $r = 1$ to ensure the leakage-resilient guarantees.

Finally, recall that we assume the comparison of values to be leak-free. This assumption is crucial for Theorem 10, when the given P^* is compared with the recomputed P . Any implementation of UTC^* needs to make sure that this assumption is not violated, e.g., by hardening this step with proper counter measures like masking [CJRR99]. Otherwise, the results can be misused, as was the case in [USS⁺20], which used the FGHF' construction [DJS19, KS20] but did not take into account the leak-free assumption—this was pointed out in [BMPS21]. Dobraunig and Mennink [DM21] also provide methods on how to achieve this assumption, which are often readily available in the implementation anyway.

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⁸This MAC is inspired by the one given in [MOSW15], which, while achieving unpredictability, is not pseudorandom in the leakage setting (LPRF). This makes it unsuitable for the UTC^* transformation.

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A Additional Background

The pseudocode for the N-schemes is given in Figure 15. Figure 16 provides the pseudocode of the sponge-based encryption scheme SLENC and MAC SLMAC in terms of their underlying components SLFUNC, SPRG, and SVHASH, whose pseudocodes are presented in Figure 17.

$\text{Enc}(K, N, A, M)$ in N1	$\text{Enc}(K, N, A, M)$ in N2	$\text{Enc}(K, N, A, M)$ in N3
$(K_e, K_m) \leftarrow K$	$(K_e, K_m) \leftarrow K$	$(K_e, K_m) \leftarrow K$
$C \leftarrow \text{Enc}^S(K_e, N, M)$	$C_e \leftarrow \text{Enc}^S(K_e, N, M)$	$T \leftarrow \text{Tag}(K_m, N, A, M)$
$T \leftarrow \text{Tag}(K_m, N, A, M)$	$T \leftarrow \text{Tag}(K_m, N, A, C)$	$C \leftarrow \text{Enc}^S(K_e, N, M \parallel T)$
return (C, T)	return (C, T)	return C
$\text{Dec}(K, N, A, (C, T))$ in N1	$\text{Dec}(K, N, A, (C, T))$ in N2	$\text{Dec}(K, N, A, C)$ in N3
$(K_e, K_m) \leftarrow K$	$(K_e, K_m) \leftarrow K$	$(K_e, K_m) \leftarrow K$
$M \leftarrow \text{Dec}^S(K_e, N, C)$	if $\text{Ver}(K_m, N, A, C, T) = 0$	$M \parallel T \leftarrow \text{Dec}^S(K_e, N, C)$
if $\text{Ver}(K_m, N, A, M, T) = 0$	return \perp	if $\text{Ver}(K_m, N, A, M, T) = 0$
return \perp	$M \leftarrow \text{Dec}^S(K_e, N, C)$	return \perp
return M	return M	return M

Figure 15: Pseudocode of N1 (left), N2 (middle), and N3 (right) in terms of a symmetric encryption scheme ($\text{Enc}^S, \text{Dec}^S$) and a MAC (Tag, Ver).

$\text{SLENC-Enc}(K_e, N, M)$	$\text{SLMAC-Tag}(K_m, N, A, C)$
$z \leftarrow \text{SLFUNC}(K_e, N)$	$H \leftarrow \text{SVHASH}(N, A, C)$
$C \leftarrow \text{SPRG}(z, M) \oplus M$	$T \leftarrow \text{SLFUNC}(K_m, H)$
return C	return $[T]_\tau$
$\text{SLENC-Dec}(K_e, N, C)$	$\text{SLMAC-Ver}(K_m, N, A, C, T)$
$z \leftarrow \text{SLFUNC}(K_e, N)$	$H \leftarrow \text{SVHASH}(N, A, C)$
$M \leftarrow \text{SPRG}(z, C) \oplus C$	$\bar{T} \leftarrow \text{SLFUNC}(K_m, H)$
return M	if $\bar{T} \neq T$
	return \perp
	return \top

Figure 16: Pseudocode of the encryption scheme $\text{SLENC} = (\text{SLENC-Enc}, \text{SLENC-Dec})$ and the MAC $\text{SLMAC} = (\text{SLMAC-Tag}, \text{SLMAC-Ver})$ in terms of the sponge-based primitives SLFUNC , SPRG , and SVHASH .

B Full Proofs

B.1 Proof of Theorem 3

Proof. Let \mathcal{A} be a wCR adversary against $\text{SE}[\mathcal{F}, \mathcal{G}]$ with output $((K, N, M), (\bar{K}, \bar{N}, \bar{M}))$. We define E to be the event that $\mathcal{F}(K, N) = \mathcal{F}(\bar{K}, \bar{N})$.

Firstly, we construct a wbind adversary \mathcal{B} against \mathcal{F} . It runs $((K, N, M), (\bar{K}, \bar{N}, \bar{M})) \leftarrow \mathcal{A}()$ and outputs $((K, N), (\bar{K}, \bar{N}))$. If \mathcal{A} is successful, we have both $K \neq \bar{K}$ and $(N, M) = (\bar{N}, \bar{M})$. Next assume that additionally to \mathcal{A} being successful, event E holds, that means $\mathcal{F}(K, N) = \mathcal{F}(\bar{K}, \bar{N})$. Then adversary \mathcal{B} is successful in game wbind, as $K \neq \bar{K}$ and $N = \bar{N}$, but they map to the same element under \mathcal{F} . Hence we have shown

$$\Pr[\text{E} \wedge \text{wCR}(\mathcal{A}) \rightarrow 1] \leq \Pr[\text{wbind}(\mathcal{B}) \rightarrow 1].$$

Secondly, we construct a CR adversary \mathcal{C} against \mathcal{G} . It runs $((K, N, M), (\bar{K}, \bar{N}, \bar{M})) \leftarrow \mathcal{A}()$ and outputs $(\mathcal{F}(K, N), \mathcal{F}(\bar{K}, \bar{N}))$. If \mathcal{A} is successful, then $K \neq \bar{K}$ and $(N, M) = (\bar{N}, \bar{M})$, and $\text{SE}[\mathcal{F}, \mathcal{G}].\text{Enc}(K, N, M) = \text{SE}[\mathcal{F}, \mathcal{G}].\text{Enc}(\bar{K}, \bar{N}, \bar{M})$. By definition of $\text{SE}[\mathcal{F}, \mathcal{G}]$ the latter is equivalent to $\mathcal{G}(\mathcal{F}(K, N)) \oplus M = \mathcal{G}(\mathcal{F}(\bar{K}, \bar{N})) \oplus \bar{M}$. As $M = \bar{M}$, this implies that $\mathcal{G}(\mathcal{F}(K, N)) = \mathcal{G}(\mathcal{F}(\bar{K}, \bar{N}))$. Next assume that additionally to \mathcal{A} being successful, event $\neg \text{E}$ holds, that means $\mathcal{F}(K, N) \neq \mathcal{F}(\bar{K}, \bar{N})$. Then adversary \mathcal{C} is successful, as he has found a collision for \mathcal{G} . Thus we obtain

$$\Pr[\neg \text{E} \wedge \text{wCR}(\mathcal{A}) \rightarrow 1] \leq \Pr[\text{CR}(\mathcal{C}) \rightarrow 1].$$

In total, one can conclude

$$\begin{aligned} \text{Adv}_{\text{SE}[\mathcal{F}, \mathcal{G}]}^{\text{wCR}}(\mathcal{A}) &= \Pr[\text{wCR}(\mathcal{A}) \rightarrow 1] \\ &= \Pr[\text{E} \wedge \text{wCR}(\mathcal{A}) \rightarrow 1] + \Pr[\neg \text{E} \wedge \text{wCR}(\mathcal{A}) \rightarrow 1] \\ &\leq \Pr[\text{wbind}(\mathcal{B}) \rightarrow 1] + \Pr[\text{CR}(\mathcal{C}) \rightarrow 1] \\ &= \text{Adv}_{\mathcal{F}}^{\text{wbind}}(\mathcal{B}) + \text{Adv}_{\mathcal{G}}^{\text{CR}}(\mathcal{C}), \end{aligned}$$

which finishes the proof. \square

B.2 Proof of Theorem 4

Proof. Let \mathcal{A} be a CR adversary against $\text{MAC}[\mathcal{H}, \mathcal{F}']$ with output $((K, X), (\bar{K}, \bar{X}))$ and let E be the event that $K = \bar{K}$ and $\mathcal{H}(X) = \mathcal{H}(\bar{X})$.

SLFUNC(K, X)	SPRG(z, L)	SVHASH(N, A, C)
$X_1, \dots, X_l \xleftarrow{r} X$	$l \leftarrow \lceil \frac{L}{r} \rceil$	$A_1, \dots, A_\alpha \xleftarrow{r} \text{pad}_{10^*}(A, r)$
$Y \leftarrow K \parallel \text{IV}$	$Z \leftarrow \varepsilon$	$C_1, \dots, C_\gamma \xleftarrow{r} \text{pad}_{10^*}(C, r)$
$S \leftarrow \rho(Y)$	$S \leftarrow z$	$Y \leftarrow N \parallel \text{IV}$
for $i = 1, \dots, l$	$Z \leftarrow Z \parallel \lceil S \rceil_r$	$S \leftarrow \rho(Y)$
$Y \leftarrow (\lceil S \rceil_r \oplus X_i) \parallel \lfloor S \rfloor_c$	for $i = 1, \dots, l-1$	for $i = 1, \dots, \alpha$
$S \leftarrow \rho(Y)$	$S \leftarrow \rho(S)$	$Y \leftarrow (\lceil S \rceil_r \oplus A_i) \parallel \lfloor S \rfloor_c$
return S	$Z \leftarrow Z \parallel \lceil S \rceil_r$	$S \leftarrow \rho(Y)$
	return $\lceil Z \rceil_L$	$S \leftarrow \lceil S \rceil_r \parallel (\lfloor S \rfloor_c \oplus (1 \parallel 0^{c-1}))$
		for $i = 1, \dots, \gamma$
		$Y \leftarrow (\lceil S \rceil_r \oplus C_i) \parallel \lfloor S \rfloor_c$
		$S \leftarrow \rho(Y)$
		$H \leftarrow \lceil S \rceil_w$
		return H

Figure 17: Pseudocode of the sponge-based function SLFUNC, pseudorandom generator SPRG, and hash function SVHASH, constructed from a random transformation $\rho: \{0, 1\}^n \rightarrow \{0, 1\}^n$, where $n = r + c$.

Firstly, we construct a CR adversary \mathcal{B} against \mathcal{H} . It runs $((K, X), (\overline{K}, \overline{X})) \leftarrow \mathcal{A}()$ and outputs (X, \overline{X}) . If \mathcal{A} is successful, we know in particular that $(K, X) \neq (\overline{K}, \overline{X})$. Next assume that additionally to \mathcal{A} being successful, event E holds, that means $K = \overline{K}$ and $\mathcal{H}(X) = \mathcal{H}(\overline{X})$. Thus adversary \mathcal{B} is successful as X, \overline{X} are different but map to the same element under \mathcal{H} . Hence we have shown

$$\Pr[\text{E} \wedge \text{CR}(\mathcal{A}) \rightarrow 1] \leq \Pr[\text{CR}(\mathcal{B}) \rightarrow 1].$$

Secondly, we construct a bind adversary \mathcal{C} against \mathcal{F}' . It runs $((K, X), (\overline{K}, \overline{X})) \leftarrow \mathcal{A}()$ and outputs $((K, \mathcal{H}(X)), (\overline{K}, \mathcal{H}(\overline{X})))$. If \mathcal{A} is successful, then $(K, X) \neq (\overline{K}, \overline{X})$ and $\text{MAC}[\mathcal{H}, \mathcal{F}'].\text{Tag}(K, X) = \text{MAC}[\mathcal{H}, \mathcal{F}'].\text{Tag}(\overline{K}, \overline{X})$. By definition of $\text{MAC}[\mathcal{H}, \mathcal{F}']$ the latter is equivalent to $\mathcal{F}'(K, \mathcal{H}(X)) = \mathcal{F}'(\overline{K}, \mathcal{H}(\overline{X}))$. If additionally to \mathcal{A} being successful, event $\neg \text{E}$ holds, we know that either $K \neq \overline{K}$ or $\mathcal{H}(X) \neq \mathcal{H}(\overline{X})$. Therefore adversary \mathcal{C} is successful, because $(K, \mathcal{H}(X)) \neq (\overline{K}, \mathcal{H}(\overline{X}))$ and $\mathcal{F}'(K, \mathcal{H}(X)) = \mathcal{F}'(\overline{K}, \mathcal{H}(\overline{X}))$. This yields

$$\Pr[\neg \text{E} \wedge \text{CR}(\mathcal{A}) \rightarrow 1] \leq \Pr[\text{bind}(\mathcal{C}) \rightarrow 1]$$

and in total we can conclude

$$\begin{aligned} \text{Adv}_{\text{MAC}[\mathcal{H}, \mathcal{F}']}^{\text{CR}}(\mathcal{A}) &= \Pr[\text{CR}(\mathcal{A}) \rightarrow 1] \\ &= \Pr[\text{E} \wedge \text{CR}(\mathcal{A}) \rightarrow 1] + \Pr[\neg \text{E} \wedge \text{CR}(\mathcal{A}) \rightarrow 1] \\ &\leq \Pr[\text{CR}(\mathcal{B}) \rightarrow 1] + \Pr[\text{bind}(\mathcal{C}) \rightarrow 1] \\ &= \text{Adv}_{\mathcal{H}}^{\text{CR}}(\mathcal{B}) + \text{Adv}_{\mathcal{F}'}^{\text{bind}}(\mathcal{C}). \end{aligned}$$

This finishes the proof. □

B.3 Proof of Theorem 5

Proof. Consider a CMT adversary \mathcal{A} against $\text{N1}[\text{SE}[\mathcal{F}, \mathcal{G}], \text{MAC}[\mathcal{H}, \mathcal{F}']]$. By Theorem 2, there exist adversaries \mathcal{A}_1 and \mathcal{A}_2 such that

$$\text{Adv}_{\text{N1}[\text{SE}[\mathcal{F}, \mathcal{G}], \text{MAC}[\mathcal{H}, \mathcal{F}']]}^{\text{CMT}}(\mathcal{A}) \leq \text{Adv}_{\text{SE}[\mathcal{F}, \mathcal{G}]}^{\text{wCR}}(\mathcal{A}_1) + \text{Adv}_{\text{MAC}[\mathcal{H}, \mathcal{F}']}^{\text{CR}}(\mathcal{A}_2).$$

Applying [Theorem 3](#) for adversary \mathcal{A}_1 , then yields adversaries \mathcal{B} and \mathcal{C} such that

$$\mathbf{Adv}_{\text{SE}[\mathcal{F}, \mathcal{G}]}^{\text{wCR}}(\mathcal{A}_1) \leq \mathbf{Adv}_{\mathcal{F}}^{\text{wbind}}(\mathcal{B}) + \mathbf{Adv}_{\mathcal{G}}^{\text{CR}}(\mathcal{C}).$$

Analogously, [Theorem 4](#) for adversary \mathcal{A}_2 gives adversaries \mathcal{D} and \mathcal{E} such that

$$\mathbf{Adv}_{\text{MAC}[\mathcal{H}, \mathcal{F}']}^{\text{CR}}(\mathcal{A}_2) \leq \mathbf{Adv}_{\mathcal{H}}^{\text{CR}}(\mathcal{D}) + \mathbf{Adv}_{\mathcal{F}'}^{\text{bind}}(\mathcal{E}).$$

Combining these results shows the claim. \square

B.4 Proof of [Theorem 6](#)

Proof. Let \mathcal{A} be a pbind adversary against SLFUNC with output $((K, N), (\bar{K}, \bar{N}))$. For the proof we will refer to the different states of the sponge as S_i and Y_i as shown in [Figure 3](#) (upper part). We show that the probability for \mathcal{A} to win is bounded above by the probability that for different inputs, the respective outputs of ρ collide in the first k bits (we call this a k -collision) or in the last c bits (this is referred to as an inner collision). For this we define C to be the event that there are $Y \neq \bar{Y}$ such that $[\rho(Y)]_k = [\rho(\bar{Y})]_k$ or $[\rho(Y)]_c = [\rho(\bar{Y})]_c$ for all states Y and \bar{Y} occurring during the evaluation of the tuples outputted by \mathcal{A} . Then we can split up the probability of \mathcal{A} winning the game pbind as follows

$$\Pr[\text{pbind}(\mathcal{A}) \rightarrow 1] = \Pr[\text{C} \wedge \text{pbind}(\mathcal{A}) \rightarrow 1] + \Pr[\neg \text{C} \wedge \text{pbind}(\mathcal{A}) \rightarrow 1]. \quad (4)$$

As a next step we show that $\Pr[\neg \text{C} \wedge \text{pbind}(\mathcal{A}) \rightarrow 1] = 0$. For this consider E to be the event that $N \neq \bar{N}$ and observe that

$$\begin{aligned} \Pr[\neg \text{C} \wedge \text{pbind}(\mathcal{A}) \rightarrow 1] &= \Pr[\text{E} \wedge \neg \text{C} \wedge \text{pbind}(\mathcal{A}) \rightarrow 1] \\ &\quad + \Pr[\neg \text{E} \wedge \neg \text{C} \wedge \text{pbind}(\mathcal{A}) \rightarrow 1]. \end{aligned} \quad (5)$$

We proceed by showing that both summands in the above equation are zero.

First we show $\Pr[\text{E} \wedge \neg \text{C} \wedge \text{pbind}(\mathcal{A}) \rightarrow 1] = 0$. We assume that $\neg \text{C}$ holds, hence we know in particular that for all $i \in \{0, \dots, l\}$ with $Y_i \neq \bar{Y}_i$ it holds that $[\rho(Y_i)]_k \neq [\rho(\bar{Y}_i)]_k$ and $[\rho(Y_i)]_c \neq [\rho(\bar{Y}_i)]_c$. As \mathcal{A} is successful, we know that $(K, N) \neq (\bar{K}, \bar{N})$ and $[S_{l+1}]_k = \text{SLFUNC}(K, N) = \text{SLFUNC}(\bar{K}, \bar{N}) = [\bar{S}_{l+1}]_k$. Furthermore E holds, which implies that $N \neq \bar{N}$. We distinguish the following two cases:

1. $K \neq \bar{K}$: In this case, we have $Y_0 = K \neq \bar{K} = \bar{Y}_0$, hence we obtain that $[\rho(Y_0)]_c \neq [\rho(\bar{Y}_0)]_c$ since C holds. This implies that $Y_1 \neq \bar{Y}_1$, because $[Y_1]_c = [\rho(Y_0)]_c \neq [\rho(\bar{Y}_0)]_c = [\bar{Y}_1]_c$. Repeating this argument for all $i \in \{1, \dots, l-1\}$ yields $Y_i \neq \bar{Y}_i$.
2. $K = \bar{K}$: In this case, we use the fact that $N \neq \bar{N}$ implies the existence of a smallest $m \in \{1, \dots, l\}$ with $N_m \neq \bar{N}_m$. Since the keys we start with are the same and $N_i = \bar{N}_i$ holds for all $i < m$, we can deduce that $S_m = \bar{S}_m$. Then $N_m \neq \bar{N}_m$ yields $Y_m \neq \bar{Y}_m$. Therefore we obtain $[\rho(Y_m)]_c \neq [\rho(\bar{Y}_m)]_c$ since C holds, which implies that $[Y_{m+1}]_c = [\rho(Y_m)]_c \neq [\rho(\bar{Y}_m)]_c = [\bar{Y}_{m+1}]_c$. Thus in particular it holds that $Y_{m+1} \neq \bar{Y}_{m+1}$ and repeating this argument for all $i \in \{m+1, \dots, l-1\}$ shows $Y_i \neq \bar{Y}_i$.

For both cases, we have shown that $Y_l \neq \bar{Y}_l$. Hence, since C holds, we can deduce that $[S_{l+1}]_k = [\rho(Y_l)]_k \neq [\rho(\bar{Y}_l)]_k = [\bar{S}_{l+1}]_k$, which contradicts the assumption that \mathcal{A} is successful. Therefore the probability $\Pr[\text{E} \wedge \neg \text{C} \wedge \text{pbind}(\mathcal{A}) \rightarrow 1]$ must be zero.

Next we show that also $\Pr[\neg \text{E} \wedge \neg \text{C} \wedge \text{pbind}(\mathcal{A}) \rightarrow 1] = 0$. For this, note that event C is composed of the event that there is a k -collision, denoted by C_k , and the event that there

is an inner collision, denoted by C_c . More precisely, we have $C = C_k \vee C_c$, which implies that $\neg C = \neg C_k \wedge \neg C_c$ holds. Using this, we obtain that

$$\begin{aligned} \Pr[\neg E \wedge \neg C \wedge \text{pbind}(\mathcal{A}) \rightarrow 1] &= \Pr[\neg E \wedge \neg C_k \wedge \neg C_c \wedge \text{pbind}(\mathcal{A}) \rightarrow 1] \\ &\leq \Pr[\neg E \wedge \neg C_k \wedge \text{pbind}(\mathcal{A}) \rightarrow 1] \end{aligned} \quad (6)$$

and hence it suffices to show $\Pr[\neg E \wedge \neg C_k \wedge \text{pbind}(\mathcal{A}) \rightarrow 1] = 0$, which will be done in the following.

Since \mathcal{A} wins game **bind**, we can deduce that $(K, N) \neq (\bar{K}, \bar{N})$ and $[S_{l+1}]_k = \text{SLFUNC}(K, N) = \text{SLFUNC}(\bar{K}, \bar{N}) = [\bar{S}_{l+1}]_k$. By assumption event $\neg E$ holds, that means $N = \bar{N}$, which in turn implies that $K \neq \bar{K}$. By construction of **SLFUNC**, we have $Y_0 = K \neq \bar{K} = \bar{Y}_0$ and hence $[\rho(Y_0)]_k \neq [\rho(\bar{Y}_0)]_k$ as $\neg C_k$ holds. Then we know in particular that $S_1 = \rho(Y_0) \neq \rho(\bar{Y}_0) = \bar{S}_1$. By assumption, we have $N = \bar{N}$ and thus obtain

$$Y_1 = S_1 \oplus (N_1 \parallel 0^c) \neq \bar{S}_1 \oplus (\bar{N}_1 \parallel 0^c) = \bar{Y}_1,$$

where $N_1 = [N]_r$ and $\bar{N}_1 = [\bar{N}]_r$. This puts us in the same situation we started with and by repeating the above argument for all $i \in \{1, \dots, l-1\}$, we get $Y_l \neq \bar{Y}_l$ and hence $[S_{l+1}]_k = [\rho(Y_l)]_k \neq [\rho(\bar{Y}_l)]_k = [\bar{S}_{l+1}]_k$. This contradicts the assumption that \mathcal{A} is a successful adversary hence the probability that \mathcal{A} wins the game **pbind** and simultaneously $\neg E$ and $\neg C_k$ hold is zero. Hence we have shown

$$\Pr[\neg E \wedge \neg C_k \wedge \text{pbind}(\mathcal{A}) \rightarrow 1] = 0, \quad (7)$$

which proves by Eq. (6), that also $\Pr[\neg E \wedge \neg C \wedge \text{pbind}(\mathcal{A}) \rightarrow 1] = 0$. Note that for this part of the proof, we split up C into C_k and C_c to emphasize that we need just the absence of k -collisions (i.e., $\neg C_k$) to show $\Pr[\neg E \wedge \neg C \wedge \text{pbind}(\mathcal{A}) \rightarrow 1] = 0$. This will become relevant later in the proof when the bound for the **wbind** advantage is proven.

As both summands in Eq. (5) were shown to be zero, Eq. (4) simplifies to

$$\Pr[\text{pbind}(\mathcal{A}) \rightarrow 1] = \Pr[C \wedge \text{pbind}(\mathcal{A}) \rightarrow 1] \leq \Pr[C].$$

For an adversary \mathcal{A} with q queries to the random transformation ρ , the probability to find a k -collision is

$$\sum_{j=1}^{q-1} \frac{j2^{n-k}}{2^n} = \sum_{j=1}^{q-1} \frac{j}{2^k} = \frac{q^2 - q}{2^{k+1}}$$

and the probability to find an inner collision is

$$\sum_{j=1}^{q-1} \frac{j2^{n-c}}{2^n} = \sum_{j=1}^{q-1} \frac{j}{2^c} = \frac{q^2 - q}{2^{c+1}}.$$

As C is the event that there is either a k -collision or an inner collision, we obtain

$$\text{Adv}_{\text{SLFUNC}}^{\text{wbind}}(\mathcal{A}) = \Pr[\text{pbind}(\mathcal{A}) \rightarrow 1] \leq \Pr[C] = \frac{q^2 - q}{2^{k+1}} + \frac{q^2 - q}{2^{c+1}},$$

which proves the first part of the theorem.

From this we can easily derive the bound for the **pbind** advantage, as for $k = n$ it holds that game **pbind** equals game **bind** and thus

$$\text{Adv}_{\text{SLFUNC}}^{\text{bind}}(\mathcal{A}) = \text{Adv}_{\text{SLFUNC}}^{\text{pbind}}(\mathcal{A}) \leq \frac{q^2 - q}{2^{c+1}} + \frac{q^2 - q}{2^{n+1}}.$$

It is left to prove the bound for the advantage of a wbind adversary \mathcal{A} . Note that for such an \mathcal{A} we have $k = n$ and the event \mathbf{E} can never occur. The latter is the case, as $K \neq \overline{K}$, $N = \overline{N}$, and $S_{l+1} = \overline{S}_{l+1}$ has to hold for the output of \mathcal{A} , otherwise \mathcal{A} loses game pbind . Therefore it holds that

$$\begin{aligned} \Pr[\text{pbind}(\mathcal{A}) \rightarrow 1] &= \Pr[\mathbf{E} \wedge \text{pbind}(\mathcal{A}) \rightarrow 1] + \Pr[\neg \mathbf{E} \wedge \text{pbind}(\mathcal{A}) \rightarrow 1] \\ &= \Pr[\neg \mathbf{E} \wedge \text{pbind}(\mathcal{A}) \rightarrow 1]. \end{aligned}$$

As before, we let \mathbf{C}_n be the event that there is a n -collision, i.e., that there are two different inputs such that the respective outputs of ρ collide. Then we obtain

$$\begin{aligned} \Pr[\neg \mathbf{E} \wedge \text{pbind}(\mathcal{A}) \rightarrow 1] &= \Pr[\neg \mathbf{E} \wedge \neg \mathbf{C}_n \wedge \text{pbind}(\mathcal{A}) \rightarrow 1] + \Pr[\neg \mathbf{E} \wedge \mathbf{C}_n \wedge \text{pbind}(\mathcal{A}) \rightarrow 1] \\ &\leq \Pr[\neg \mathbf{E} \wedge \neg \mathbf{C}_n \wedge \text{pbind}(\mathcal{A}) \rightarrow 1] + \Pr[\mathbf{C}_n] \\ &= \Pr[\mathbf{C}_n], \end{aligned}$$

where the last equality holds by Eq. (7) for $k = n$. Putting together the above results, and using the bound that was computed for the probability of n -collisions, yields

$$\text{Adv}_{\text{SLFUNC}}^{\text{wbind}}(\mathcal{A}) = \Pr[\text{pbind}(\mathcal{A}) \rightarrow 1] = \Pr[\neg \mathbf{E} \wedge \text{pbind}(\mathcal{A}) \rightarrow 1] \leq \Pr[\mathbf{C}_n] = \frac{q^2 - q}{2^{n+1}}.$$

This finishes the proof of the theorem. \square

B.5 Proof of Theorem 7

Proof. For sake of simplicity, we assume that m is a multiple of the rate r and we set $l = \frac{m}{r}$. Finding a collision for SPRG equals finding distinct states $z_1 \neq z_2$ that agree on their outer state (first r bits) for l invocations of ρ . It holds that

$$\begin{aligned} \text{Adv}_{\text{SPRG}}^{\text{CR}}(\mathcal{A}) &= \Pr \left[[z_1]_r = [z_2]_r \wedge [\rho^1(z_1)]_r = [\rho^1(z_2)]_r \right. \\ &\quad \left. \wedge \dots \wedge [\rho^l(z_1)]_r = [\rho^l(z_2)]_r \mid z_1, z_2 \leftarrow \mathcal{A}^\rho() \right]. \end{aligned}$$

We define events $\mathbf{E}_0, \mathbf{E}_1, \dots, \mathbf{E}_l$, where \mathbf{E}_i equals $[\rho^i(z_1)]_r = [\rho^i(z_2)]_r$, for $z_1, z_2 \leftarrow \mathcal{A}^\rho()$. Thus

$$\begin{aligned} \text{Adv}_{\text{SPRG}}^{\text{CR}}(\mathcal{A}) &= \Pr[\mathbf{E}_0 \wedge \mathbf{E}_1 \wedge \dots \wedge \mathbf{E}_l] \\ &\leq \Pr[\mathbf{E}_1 \wedge \dots \wedge \mathbf{E}_l] \\ &= \Pr[\mathbf{E}_1] \cdot \Pr[\mathbf{E}_2 \mid \mathbf{E}_1] \cdot \dots \cdot \Pr[\mathbf{E}_l \mid \mathbf{E}_1 \wedge \dots \wedge \mathbf{E}_{l-1}] \\ &= \Pr[\mathbf{E}_1] \cdot \prod_{i=2}^l \Pr[\mathbf{E}_i \mid \mathbf{E}_1 \wedge \dots \wedge \mathbf{E}_{i-1}]. \end{aligned}$$

Bounding event \mathbf{E}_1 is a simple counting argument. Since \mathcal{A} makes q queries to ρ , let \mathbf{X}_i be the event that the i -th query to ρ triggers \mathbf{E}_1 . It holds that

$$\Pr[\mathbf{E}_1] \leq \sum_{i=1}^q \Pr[\mathbf{X}_i] = \sum_{i=1}^q \frac{(i-1)2^c}{2^n} = \sum_{i=1}^q \frac{i-1}{2^r} = \frac{q^2 - q}{2^{r+1}}.$$

Note that only the probability for \mathbf{E}_1 depends on q as \mathcal{A} can only influence the outcome of the first application of ρ with his queries. For the remaining events ($\mathbf{E}_2, \dots, \mathbf{E}_l$), the fact that ρ is a random function yields that the events are independent from one another which gives for all $i \in \{2, \dots, l\}$

$$\Pr[\mathbf{E}_i \mid \mathbf{E}_1 \wedge \dots \wedge \mathbf{E}_{i-1}] = \Pr[\mathbf{E}_i] \leq \frac{1}{2^r}.$$

Collecting the above finally provides

$$\mathbf{Adv}_{\text{SPRG}}^{\text{CR}}(\mathcal{A}) \leq \Pr[\mathbf{E}_1] \cdot \prod_{i=2}^l \Pr[\mathbf{E}_i \mid \mathbf{E}_1 \wedge \dots \wedge \mathbf{E}_{i-1}] \leq \frac{q^2 - q}{2^{r+1}} \cdot \prod_{i=2}^l \frac{1}{2^r} = \frac{q^2 - q}{2^{m+1}}.$$

This finishes the proof. \square

B.6 Hierarchy of Binding Notions

The following theorem describes the relation between the different binding notions.

Theorem 11. *Let $F: \mathcal{K} \times \{0, 1\}^x \rightarrow \{0, 1\}^y$ be a function. Then for any adversary \mathcal{A} there exists an adversary \mathcal{B} such that*

$$\mathbf{Adv}_F^{\text{bind}}(\mathcal{A}) \leq \mathbf{Adv}_F^{\text{pbind}}(\mathcal{B})$$

and for any adversary \mathcal{C} there exists an adversary \mathcal{D} such that

$$\mathbf{Adv}_F^{\text{wbind}}(\mathcal{C}) \leq \mathbf{Adv}_F^{\text{bind}}(\mathcal{D}).$$

Proof. For the first part, we consider a bind adversary \mathcal{A} against F and construct a pbind adversary \mathcal{B} against F . It runs $((K, X), (\overline{K}, \overline{X})) \leftarrow \mathcal{A}$ and outputs $((K, X), (\overline{K}, \overline{X}))$. If \mathcal{A} succeeds then $(K, X) \neq (\overline{K}, \overline{X})$ and $F(K, X) = F(\overline{K}, \overline{X})$. The latter implies in particular that $\lceil Y_1 \rceil_l = \lceil Y_2 \rceil_l$ for $Y_i \leftarrow F(K_i, X_i)$. Thus \mathcal{B} is also successful in game pbind.

For the second part, let \mathcal{C} be a wbind adversary against F and construct a bind adversary \mathcal{D} against F . It runs $((K, X), (\overline{K}, \overline{X})) \leftarrow \mathcal{C}$ and outputs $((K, X), (\overline{K}, \overline{X}))$. If \mathcal{C} succeeds then $K \neq \overline{K}$ and $F(K, X) = F(\overline{K}, \overline{X})$. Note that the first condition implies in particular that $(K, X) \neq (\overline{K}, \overline{X})$ and hence \mathcal{D} is successful as well. \square