Key Committing Security of AEZ and More

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AEAD: Authenticated Encryption with Associated Data

◆ Symmetric key cryptosystem to provide privacy & authenticity [Rog02] \blacksquare K: key, N: nonce, M: plaintext, A: associated data (AD), C: ciphertext (including tag) **E**ncryption: $Enc(K, N, A, M) = C$

■ Decryption: $Dec(K, N, A, C) = M$ when inputs are authentic, otherwise returns \perp

◆ Security

■ Basic: privacy & authenticity

■ Advanced: nonce-misuse/decryption-misuse resistant, **Key Committing Security**

Key committing security (KCS) for AEAD

\blacklozenge KCS: guarantee that ciphertext is a commitment of K

- \blacksquare Evaluated by collision resistance of Enc
- \blacksquare Adversary chooses K
- Standard security notions (PRIV/AUTH) do not capture KCS
- ◆ Increased demand by attacks exploiting non-KC-secure AEAD
	- Attack on message franking [DGRW18]: message receiver cannot report delivered picture as abuse
	- Partitioning oracle attack [LGR21]:

narrowing down the range of the passwords stored in servers

- \blacksquare Other attacks: SFrame [IIM21], Subscribe with Google [ADG+22], \cdots
- Ongoing NIST accordion cipher project includes KCS as one example of desired security

Definitions for KCS

◆ We follow the definitions by Bellare and Hoang [BH22]

- Other related definitions: Complete Robustness [FOR17], sender/receiver binding [GLR17], Context discovery [MLGR23], …
- \blacklozenge An adversary is computationally hard to find two inputs of Enc that have the same ciphertext under:
	- CMT-1: different keys
	- \blacksquare CMT-3: different (K, N, A) pairs
	- \blacksquare CMT-4: different (K, N, A, M) pairs
	- CMT-3 is equivalent to CMT-4 [BH22]

Encode-then-Encipher via Wide-block cipher

- ◆ (Tweakable) Wide block cipher (WBC)
	- \blacksquare IN: secret key, plaintext w/ variable length, and tweak w/ variable length
	- OUT: ciphertext w/ same length as plaintext
	- WBC itself is not AEAD, but it can be converted to AEAD by Encode-then-Encipher

◆ Encode-then-Encipher (EtE) [BR00]

- underlying primitive: WBC
- **Enc:** encode an input message (ex. append/prepend 0^{τ}) and encipher with a WBC
- Dec: decipher ciphertext and check whether deciphered string follows the encoding rule \rightarrow If it is OK, return decoded string

Security of EtE

◆ EtE is Robust AE; resists nonce misuse and decryption misuse

◆ No KCS analysis on concrete EtE schemes

■ Existing studies focus on NAE and MRAE

• GCM, CCM, ChaCha20-Poly1305, SIV, GCM-SIV, …

 \blacklozenge Ideal: τ -bit KCS when assuming WBC is an ideal cipher (IC) and C is long enough $[GLR17]$

Generic CMT-1/4 attack: $O(2^{\tau})$

 \blacksquare Try decryption with fixed C and distinct (K, A) until the decrypted value has 0^{τ}

◆ In practice: WBC is not behaving as IC **(built on smaller primitives)**

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Our results

◆ We study key committing security of

■ AEZ [HKR15] … Popular AEAD with lots of cryptanalysis, and CAESAR 3rd round candidate

• Zero-appending is specified

■ EtE-Adiantum [CB18] … Adiantum: Designed by Google, widely deployed in actual devices

• Prepend and append with zeros

■ EtE-HCTR2 [CHB21] … HCTR2: deployed in Android file-based encryption

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AEZ [Hoang, Krovetz, Rogaway@EC15]

\blacksquare EtE using *n*-bit TBC $E_K^{i,j}$

- Encodes *M* by concatenating 0^{τ} at the end of *M* ($\tau \le n$, M_{y} includes 0^{τ})
- Enciphering way changes depending on input length (including $0^{\tau})$
- Input length \geq 256 bits: AEZ-core (Fig.; our target), otherwise: AEZ-tiny (out of scope)
- AEZ-core: 4 or 5-round Feistel with PHASH-like AD processing
- Proof-then-prune strategy: proving its security assuming TBC is TPRP then pruning TBC cost
	- Reducing # rounds of TBC
	- Using simpler key schedule

CMT-4 attack on AEZ

 \blacklozenge Recall: CMT-4 adv. tries to find distinct (K, N, A, M) , (K', N', A', M') s.t. $Enc(K, N, A, M) = Enc(K', N', A', M')$

Assuming $(K, N, M) = (K', N', M')$

 \blacksquare Adv. wins if it invokes a collision of Δ for distinct A, A'

■ It is easy since adv. knows K, K' , and it can invert TBC \Rightarrow $O(1)$ CMT-4 attack

CMT-1 attack & proof on general AEZ $(\tau = n)$

- ◆ General AEZ: assuming the ideal TBC
- \blacklozenge Strategy: focusing on \blacksquare in the last Feistel i.e., $\mathcal{C}_{\mathcal{V}}$ collision
	- \blacksquare Once getting C_y collision, it is easy to get collisions on other ciphertexts (omit the details)

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• Search (X_1, Y_2) and (X'_1, Y'_2) s.t. $X_1 \oplus X'_1 = Y_2 \oplus Y'_2$

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	- \blacksquare Also, we can prove that it is tight
		- Bellare and Hoang prove DM's collision resistance in IC model. Ours is almost the same. [BH22]
		- We have two consecutive TBCs, but it is not a problem.

- \blacklozenge Reduce C_v coll. to a generalized birthday problem
	- $\blacksquare \tau$ < $n \Rightarrow M_y = M^* \parallel 0^\tau$
	- DM-like const. becomes the sum of 2 TBCs, where $\text{lsb}_{\tau}(\mathbb{Y}_1) = \text{lsb}_{\tau}(\mathbb{X}_2)$ must hold

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- ⇒ Generalized birthday problem with 4 lists
- ◆ Solution: k -tree algorithm $(k = 4)$
	- \blacksquare Comp. : $O(2^{n/3})$ but each list needs $2^{n/3}$ elements
	- \blacksquare Possible when $\tau \leq 2n/3$

◆ When we cannot prepare enough values for X_1, Y_2, X'_1, Y'_2 , the success of 4-tree alg. becomes probabilistic.

- Repeat 4-tree alg. with less elements of each list until success
- 4-tree alg. with $O(2^{n-\tau})$ elements: success prob. is $O(2^{2n-3\tau})$
- Comp.: $O(2^{n-\tau}) \times O(2^{3\tau-2n}) = O(2^{2\tau-n})$

CMT-1 attack on full-spec AEZ

◆ Full-spec AEZ: TBC follows the full specification of AEZ

 \blacklozenge Same strategy as the general AEZ attack: focusing on \Box i.e., $\mathcal{C}_{\mathbf{v}}$ collision

◆ TBC: XE-style TBC using AES10 128 Assuming $|K| = 384$ (default), and $L || I || J$ \boldsymbol{K} $E_K^{-1,i}(X) = \text{AES10}_K(X \oplus i \cdot L)$ $\overline{E_K^{-1,1}}$ ■ AES10: 10-round AES, but ... ■ Last round has MixColumns, unlike usual AES $\begin{bmatrix} E_K^{-1,2} \end{bmatrix}$ \blacksquare Round subkeys: $(I, J, L, I, J, L, I, J, L, I)$ $E_K^{0,2}$

◆ Find $K = I || J || L$, $K' = I' || J' || L'$, s.t. $(\delta_{X_1}, \delta_{Y_1}, \delta_{X_2}, \delta_{Y_2}) = (0, 0, 0, 0)$ $(\delta_{X_1} = X_1 \oplus X_1')$

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 \blacksquare Set $\delta_{\mathbb{X}_1} = 0$, and set δ_L so that δ_L and δ_{2L} have only 1 active S-box

■ Set δ_I to cancel out diff. propagation caused by δ_L and δ_{2L}

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- 2^{nd} *AES*10: event of $\delta_{\mathbb{Y}_2} = 0$ is probabilistic, but only 1 active S-box **per one aesenc**
- attack comp. : $\leq 2^{28}$
- actual comp.: 2²⁷

 $AES10_K$

 $AES10_K$

 \mathbb{Y}_2

2L

Conclusion

◆ First key-committing analysis on concrete EtE schemes

■ For Adiantum/HCTR2 : (we omit here, but) a small detail that has little impact on the standard model security can significantly impact KCS, which makes some cases difficult to analyze.

◆ Future work

■ Analysis of AEZ-tiny and other EtE

Thank you!

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Appendix

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AEZ-tiny

◆ Input length less than 256 bits: AEZ-tiny

- Feistel with a minimum of 8 rounds
- Number of steps varies depending on input length

 \blacksquare Fig: [HKR15]

 \blacklozenge Once getting C_v collision, other ciphertext blocks are easy to collide \blacksquare Verification is OK if M_v is zeros

- \blacksquare CC_1 , ..., CC_m can be any value because they are irrelevant to M_v , C_v
- \blacksquare To invoke C_x collision, we manipulate Δ
- \triangle can be any value like CMT-4 attack

