Key Committing Security of AEZ and More

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*6: Strativia, *7: Mitsubishi Electric Corporation

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AEAD: Authenticated Encryption with Associated Data

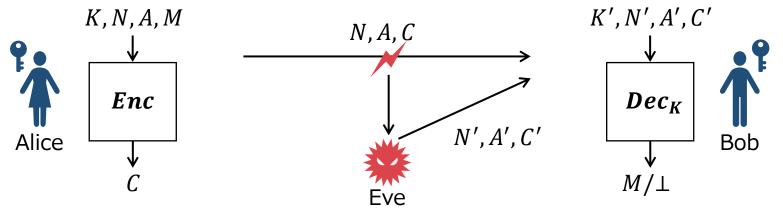
- Symmetric key cryptosystem to provide privacy & authenticity [Rog02]
 K: key, *N*: nonce, *M*: plaintext, *A*: associated data (AD), *C*: ciphertext (including tag)
 - Encryption: Enc(K, N, A, M) = C

Decryption: Dec(K, N, A, C) = M when inputs are authentic, otherwise returns \bot

Security

Basic: privacy & authenticity

Advanced: nonce-misuse/decryption-misuse resistant, **Key Committing Security**



Key committing security (KCS) for AEAD

KCS: guarantee that ciphertext is a commitment of K

- Evaluated by collision resistance of Enc
- Adversary chooses K
- Standard security notions (PRIV/AUTH) do not capture KCS
- Increased demand by attacks exploiting non-KC-secure AEAD
 - Attack on message franking [DGRW18]: message receiver cannot report delivered picture as abuse
 - Partitioning oracle attack [LGR21]:

narrowing down the range of the passwords stored in servers

- Other attacks: SFrame [IIM21], Subscribe with Google [ADG+22], …
- Ongoing NIST accordion cipher project includes KCS as one example of desired security

Definitions for KCS

◆ We follow the definitions by Bellare and Hoang [BH22]

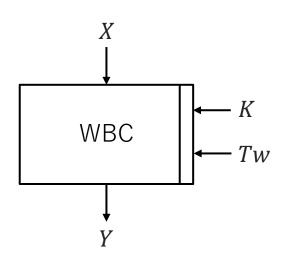
- Other related definitions: Complete Robustness [FOR17], sender/receiver binding [GLR17], Context discovery [MLGR23], ···
- An adversary is computationally hard to find two inputs of *Enc* that have the same ciphertext under:
 - CMT-1: different keys
 - CMT-3: different (K, N, A) pairs
 - CMT-4: different (*K*, *N*, *A*, *M*) pairs
 - CMT-3 is equivalent to CMT-4 [BH22]

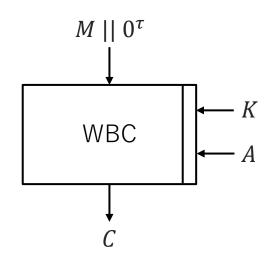
Encode-then-Encipher via Wide-block cipher

- (Tweakable) Wide block cipher (WBC)
 - IN: secret key, plaintext w/ variable length, and tweak w/ variable length
 - OUT: ciphertext w/ same length as plaintext
 - WBC itself is not AEAD, but it can be converted to AEAD by Encode-then-Encipher

Encode-then-Encipher (EtE) [BR00]

- underlying primitive: WBC
- Enc: encode an input message (ex. append/prepend 0^{τ}) and encipher with a WBC
- Dec: decipher ciphertext and check whether deciphered string follows the encoding rule → If it is OK, return decoded string





Security of EtE

EtE is Robust AE; resists nonce misuse and decryption misuse

No KCS analysis on concrete EtE schemes

Existing studies focus on NAE and MRAE

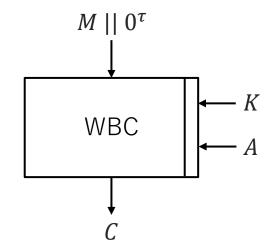
• GCM, CCM, ChaCha20-Poly1305, SIV, GCM-SIV, …

 Ideal: τ-bit KCS when assuming WBC is an ideal cipher (IC) and C is long enough [GLR17]

- Generic CMT-1/4 attack: $O(2^{\tau})$
- Try decryption with fixed C and distinct (K, A) until the decrypted value has 0^{τ}

In practice: WBC is not behaving as IC (built on smaller primitives)

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Our results

We study key committing security of

■ AEZ [HKR15] … Popular AEAD with lots of cryptanalysis, and CAESAR 3rd round candidate

Zero-appending is specified

EtE-Adiantum [CB18] ··· Adiantum: Designed by Google, widely deployed in actual devices

• Prepend and append with zeros

EtE-HCTR2 [CHB21] ···· HCTR2: deployed in Android file-based encryption

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Scheme	CMT-1 A	CMT-1 P	CMT-4 (A & P)	Proof
general AEZ	$O(2^{n/2})$	(not specified)	O(1)	n/2 (Sect. 7.1)
full-spec AEZ	2^{27}	(not specified)	O(1)	_
$\operatorname{EtE}\operatorname{-}\operatorname{Adiantum}$	$O(2^{n/2})$	$O(2^{n/2})$	O(1)	n/2 (Sect. 7.2)
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 $n = \tau$, *n* is input/output size of underlying BC

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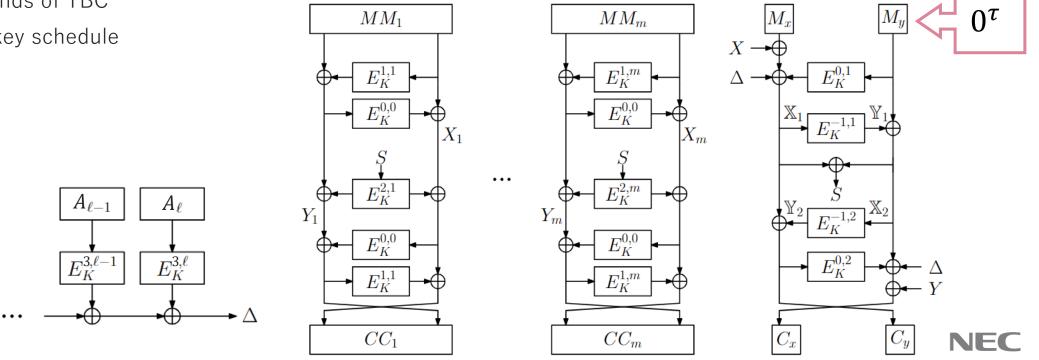
AEZ [Hoang, Krovetz, Rogaway@EC15]

EtE using *n*-bit TBC $E_K^{i,j}$

- Encodes M by concatenating 0^{τ} at the end of M ($\tau \leq n, M_y$ includes 0^{τ})
- Enciphering way changes depending on input length (including $0^\tau)$
- Input length \geq 256 bits: AEZ-core (Fig.; our target), otherwise: AEZ-tiny (out of scope)
- AEZ-core: 4 or 5-round Feistel with PHASH-like AD processing
- Proof-then-prune strategy: proving its security assuming TBC is TPRP then pruning TBC cost
 - Reducing # rounds of TBC
 - Using simpler key schedule

 A_1

 $E_{K}^{3,1}$



CMT-4 attack on AEZ

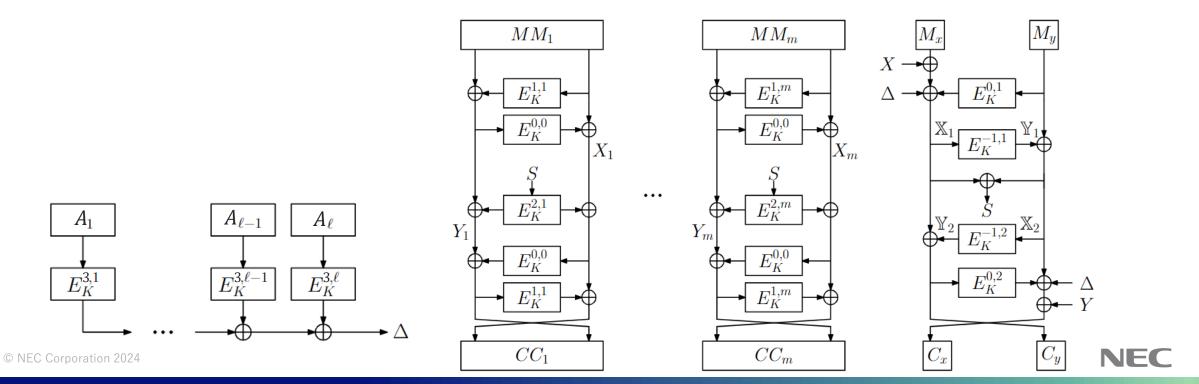
Recall: CMT-4 adv. tries to find distinct (K, N, A, M), (K', N', A', M') s.t. Enc(K, N, A, M) = Enc(K', N', A', M')

Assuming (K, N, M) = (K', N', M')

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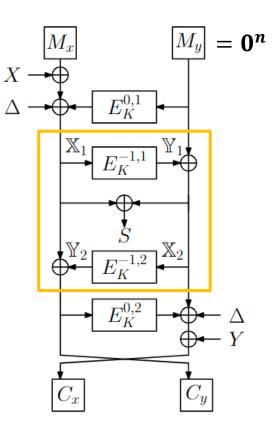
Adv. wins if it invokes a collision of Δ for distinct A, A'

It is easy since adv. knows K, K', and it can invert TBC $\Rightarrow O(1)$ CMT-4 attack



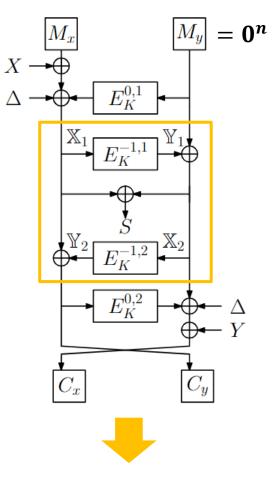
CMT-1 attack & proof on general AEZ ($\tau = n$)

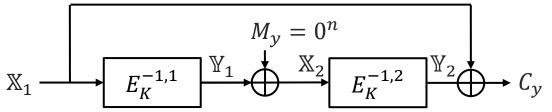
- ◆ General AEZ: assuming the ideal TBC
- \diamond Strategy: focusing on \square in the last Feistel i.e., C_{y} collision
 - Once getting C_y collision, it is easy to get collisions on other ciphertexts (omit the details)



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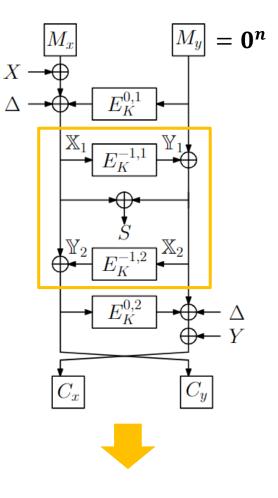
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 - can be viewed as Davies-Meyer (DM) construction

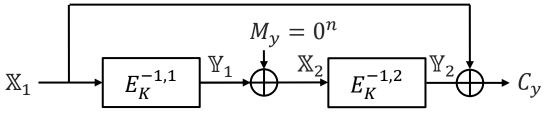




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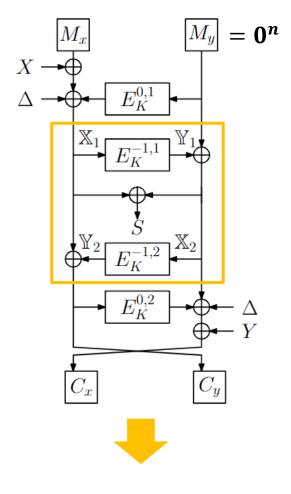
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 - As in the usual DM, a coll. Attack works in $O(2^{n/2})$
 - Search (X_1, Y_2) and (X'_1, Y'_2) s.t. $X_1 \oplus X'_1 = Y_2 \oplus Y'_2$

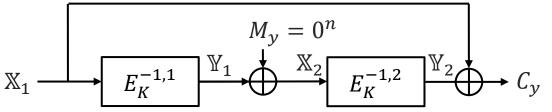




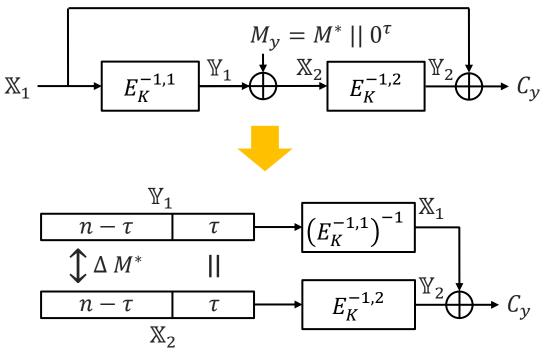
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 - Search (X_1, Y_2) and (X'_1, Y'_2) s.t. $X_1 \oplus X'_1 = Y_2 \oplus Y'_2$
 - Also, we can prove that it is tight
 - Bellare and Hoang prove DM's collision resistance in IC model. Ours is almost the same. [BH22]
 - We have two consecutive TBCs, but it is not a problem.





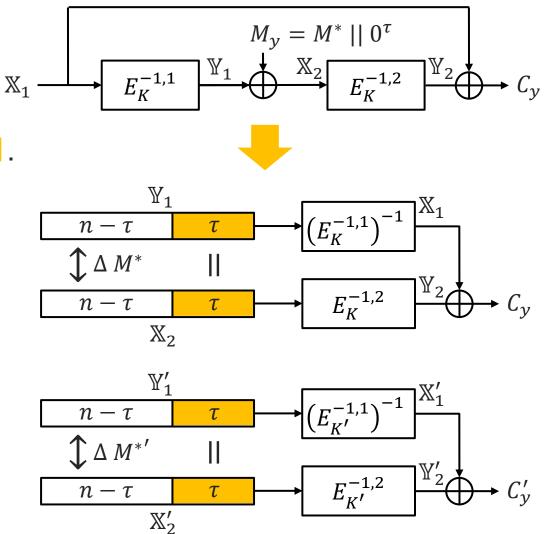
- \blacklozenge Reduce C_y coll. to a generalized birthday problem
 - $\bullet \tau < n \Rightarrow M_y = M^* \mid\mid 0^\tau$
 - DM-like const. becomes the sum of 2 TBCs, where $lsb_{\tau}(\mathbb{Y}_1) = lsb_{\tau}(\mathbb{X}_2)$ must hold



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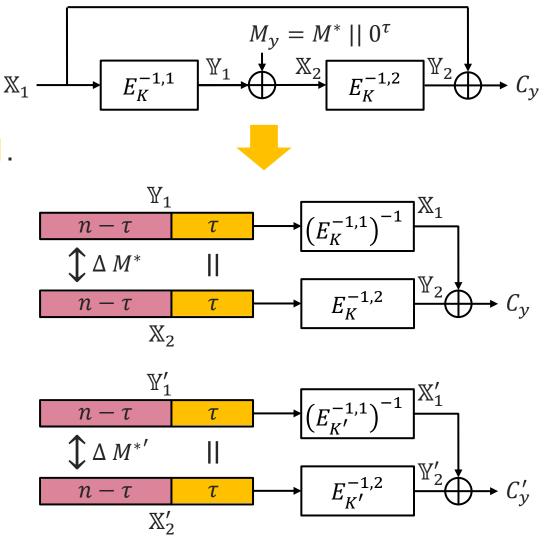
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- Pick up any distinct keys K, K' and fix values in _____.



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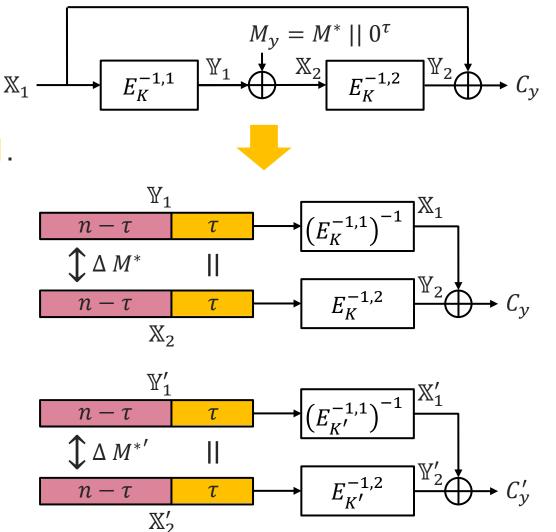
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- Search X_1, Y_2, X'_1, Y'_2 s.t. $X_1 \oplus Y_2 \oplus X'_1 \oplus Y'_2 = 0$ by changing values in \square .
 - Diff. can be canceled by M^*
- \Rightarrow Generalized birthday problem with 4 lists



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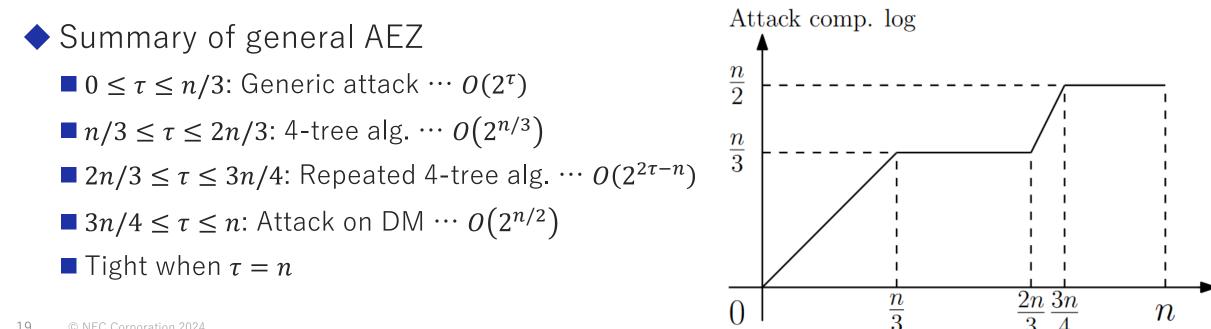
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 - Diff. can be canceled by M^*
- \Rightarrow Generalized birthday problem with 4 lists
- Solution: *k*-tree algorithm (k = 4)
 - Comp. : $O(2^{n/3})$ but each list needs $2^{n/3}$ elements
 - Possible when $\tau \leq 2n/3$



 \diamond When we cannot prepare enough values for $\mathbb{X}_1, \mathbb{Y}_2, \mathbb{X}'_1, \mathbb{Y}'_2, \mathbb{Y$ the success of 4-tree alg. becomes probabilistic.

- Repeat 4-tree alg. with less elements of each list until success
- 4-tree alg. with $O(2^{n-\tau})$ elements: success prob. is $O(2^{2n-3\tau})$
- Comp.: $O(2^{n-\tau}) \times O(2^{3\tau-2n}) = O(2^{2\tau-n})$

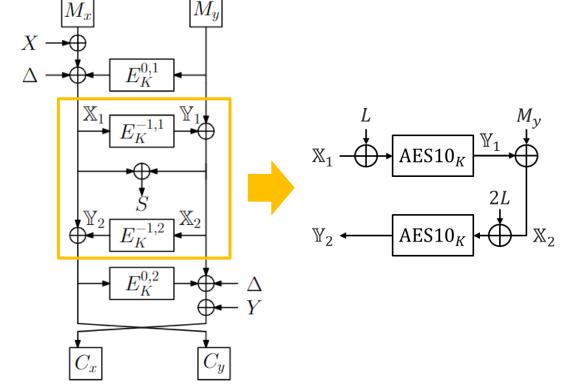


CMT-1 attack on full-spec AEZ

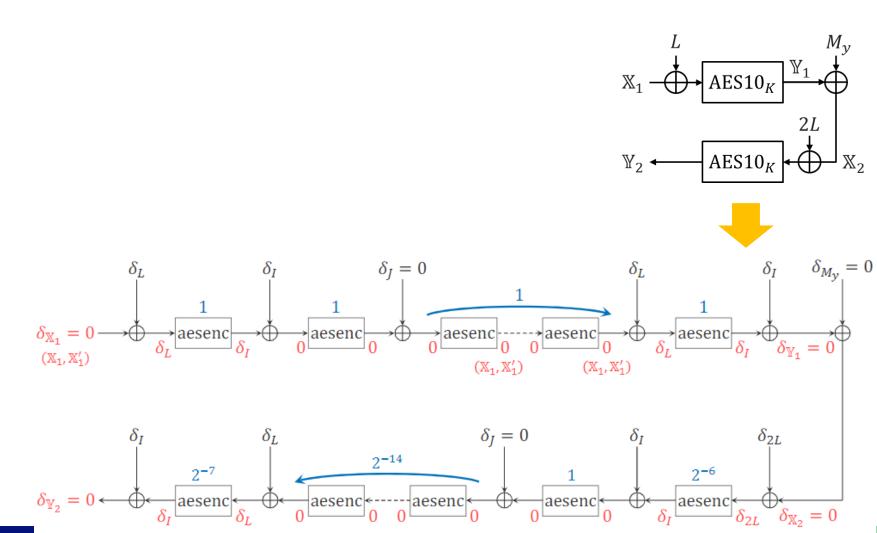
Full-spec AEZ: TBC follows the full specification of AEZ
 Same strategy as the general AEZ attack: focusing on ______i.e., C_v collision

◆ TBC: XE-style TBC using AES10
■ Assuming |K| = 384 (default), and L || I || J ↓ A
■ $E_K^{-1,i}(X) = AES10_K(X \oplus i \cdot L)$ ■ AES10: 10-round AES, but ..
■ Last round has MixColumns, unlike usual AES

Round subkeys: (I, J, L, I, J, L, I, J, L, I)



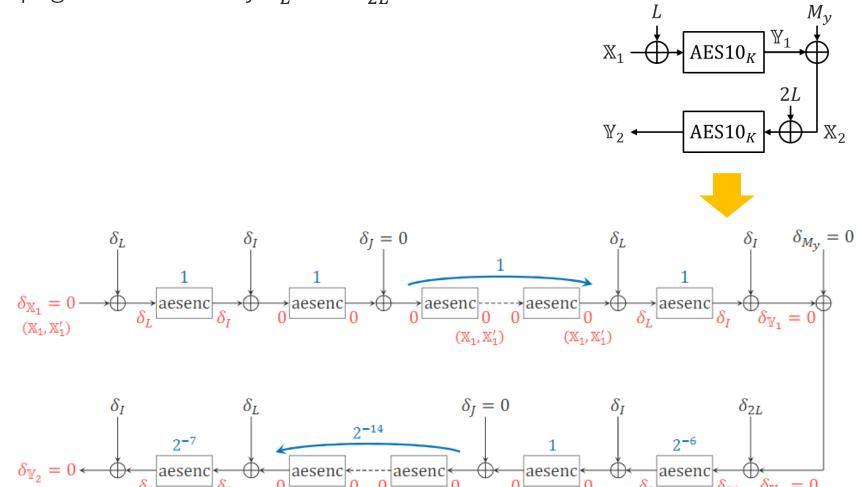
♦ Find K = I || J || L, K' = I' || J' || L', s.t. $(\delta_{X_1}, \delta_{Y_1}, \delta_{X_2}, \delta_{Y_2}) = (0, 0, 0, 0) (\delta_{X_1} = X_1 \oplus X'_1)$



 $\textbf{Find } K = I \mid \mid J \mid \mid L, \ K' = I' \mid \mid J' \mid \mid L', \ \textbf{s.t.} \left(\delta_{\mathbb{X}_1}, \delta_{\mathbb{Y}_1}, \delta_{\mathbb{X}_2}, \delta_{\mathbb{Y}_2} \right) = (0, 0, 0, 0) \quad (\delta_{\mathbb{X}_1} = \mathbb{X}_1 \oplus \mathbb{X}_1')$

Set $\delta_{X_1} = 0$, and set δ_L so that δ_L and δ_{2L} have only 1 active S-box

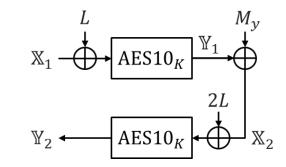
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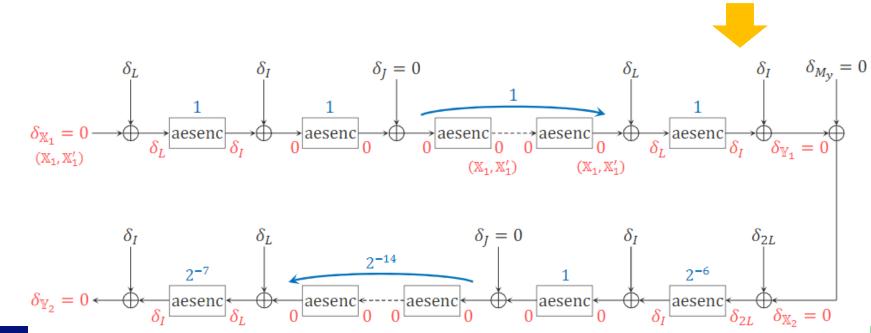


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Set *J*, *J*' so that **3rd aesenc outputs go back to** X_1, X'_1 (here, $\delta_J = 0$)



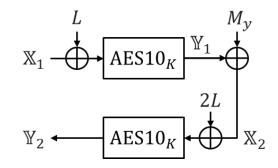


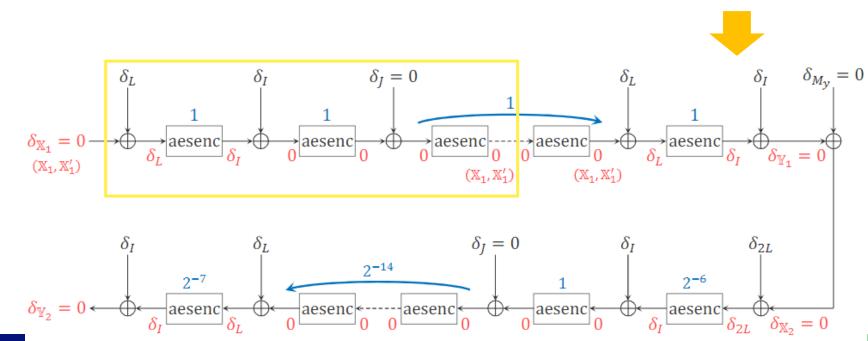
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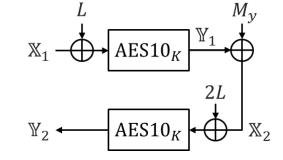
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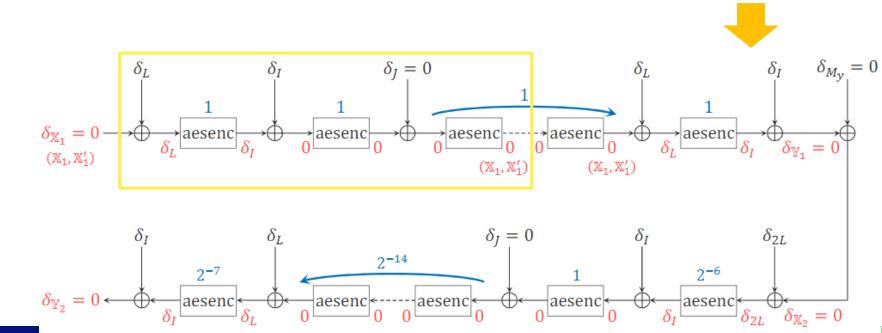
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• Set
$$\delta_{M_y} = 0 \to \delta_{\mathbb{X}_2} = \delta_{\mathbb{Y}_1} = 0$$



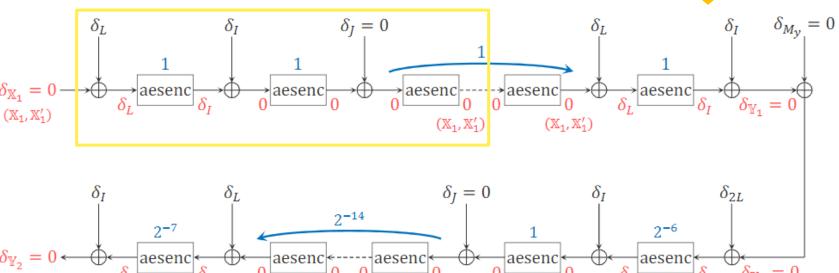


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• Set
$$\delta_{M_y} = 0 o \delta_{\mathbb{X}_2} = \delta_{\mathbb{Y}_1} = 0$$

- 2nd AES10: event of $\delta_{\mathbb{Y}_2} = 0$ is probabilistic, but only 1 active S-box per one aesenc
- attack comp. : $\leq 2^{28}$
- actual comp. : 2²⁷



 $AES10_{K}$

AES10_k

 \mathbb{Y}_2

2L

Conclusion

First key-committing analysis on concrete EtE schemes

For Adiantum/HCTR2 : (we omit here, but) a small detail that has little impact on the standard model security can significantly impact KCS, which makes some cases difficult to analyze.

Scheme	CMT-1 A	CMT-1 P	CMT-4 (A & P)	Proof
general AEZ	$O(2^{n/2})$	(not specified)	O(1)	n/2 (Sect. 7.1)
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EtE-HCTR2	$O(2^{n/2})$	$O(2^{n/2})$	O(1)	

Future work

Analysis of AEZ-tiny and other EtE

Thank you!

We appreciate anonymous reviewers for their insightful comments!

Appendix

Ref.

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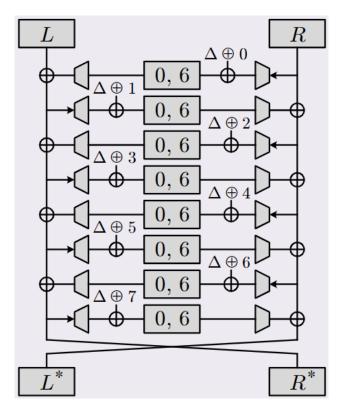
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AEZ-tiny

Input length less than 256 bits: AEZ-tiny

- Feistel with a minimum of 8 rounds
- Number of steps varies depending on input lengthFig: [HKR15]



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Once getting C_y collision, other ciphertext blocks are easy to collide
 Verification is OK if M_y is zeros

- \square CC₁, ..., CC_m can be any value because they are irrelevant to M_y , C_y
- **To invoke** C_x collision, we manipulate Δ
- $\blacksquare \Delta$ can be any value like CMT-4 attack

